

# The $H_0$ Olympics: a fair ranking of proposed models

Guillermo Franco Abellán

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Based on:

arXiv:2102.12498 (PRD in press)

arXiv:2008.09615 (PRD in press)

arXiv:2009.10733 PRD 103 (2020)

arXiv:2107.10291, submitted to Physics Reports



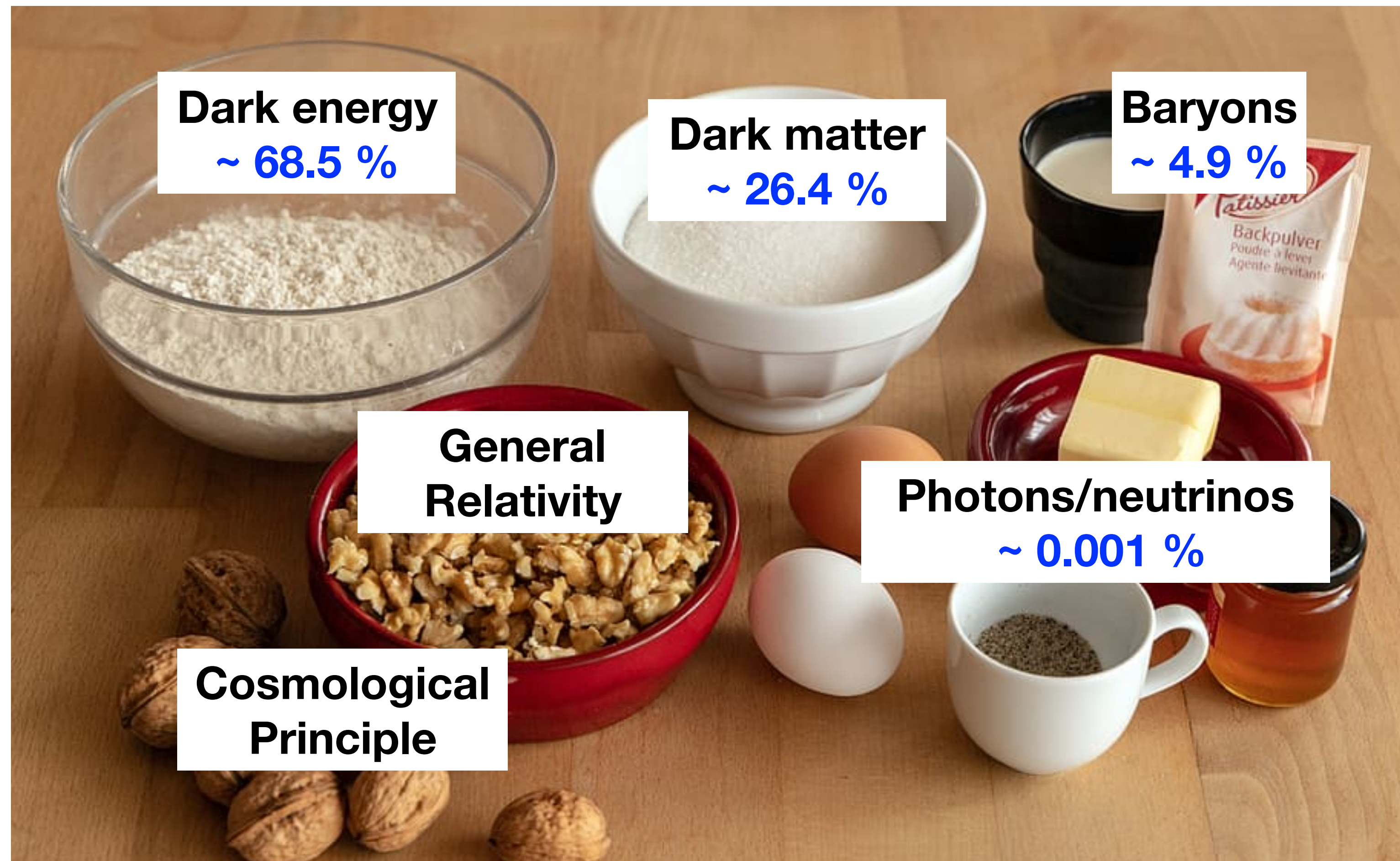


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- I. Cosmic concordance and discordance
- II. The  $H_0$  Olympics: quantifying the success of a resolution
- III. Explaining the  $S_8$  tension with Decaying Dark matter
- IV. Conclusions

# **I. Cosmic concordance and discordance**

# Cosmic recipe

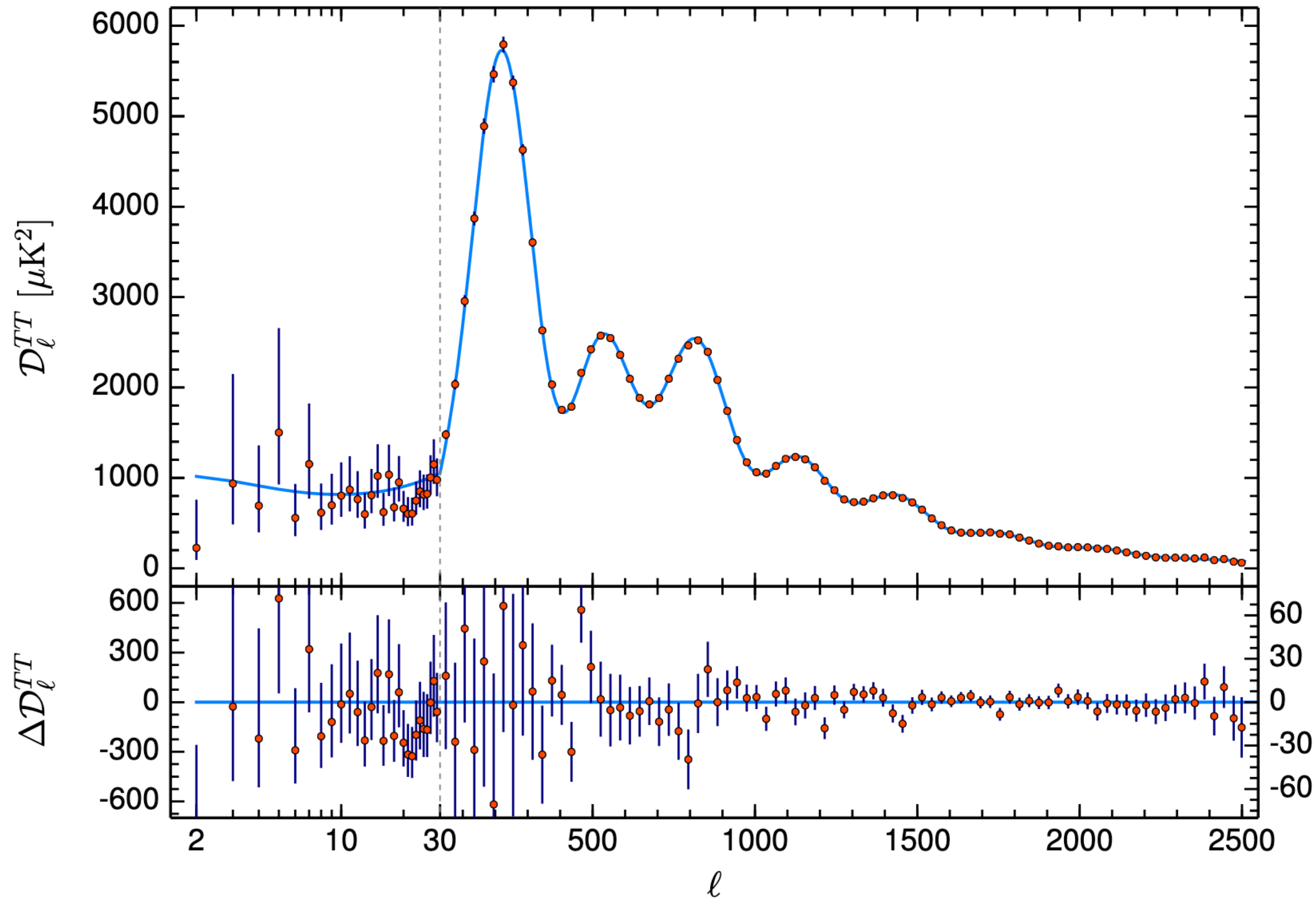


$\Lambda$ CDM model fully specified by  $\{\Omega_c, \Omega_b, H_0, A_s, n_s, \tau_{reio}\}$



# The era of precision cosmology

$\Lambda$ CDM gives excellent fit to CMB anisotropy spectra

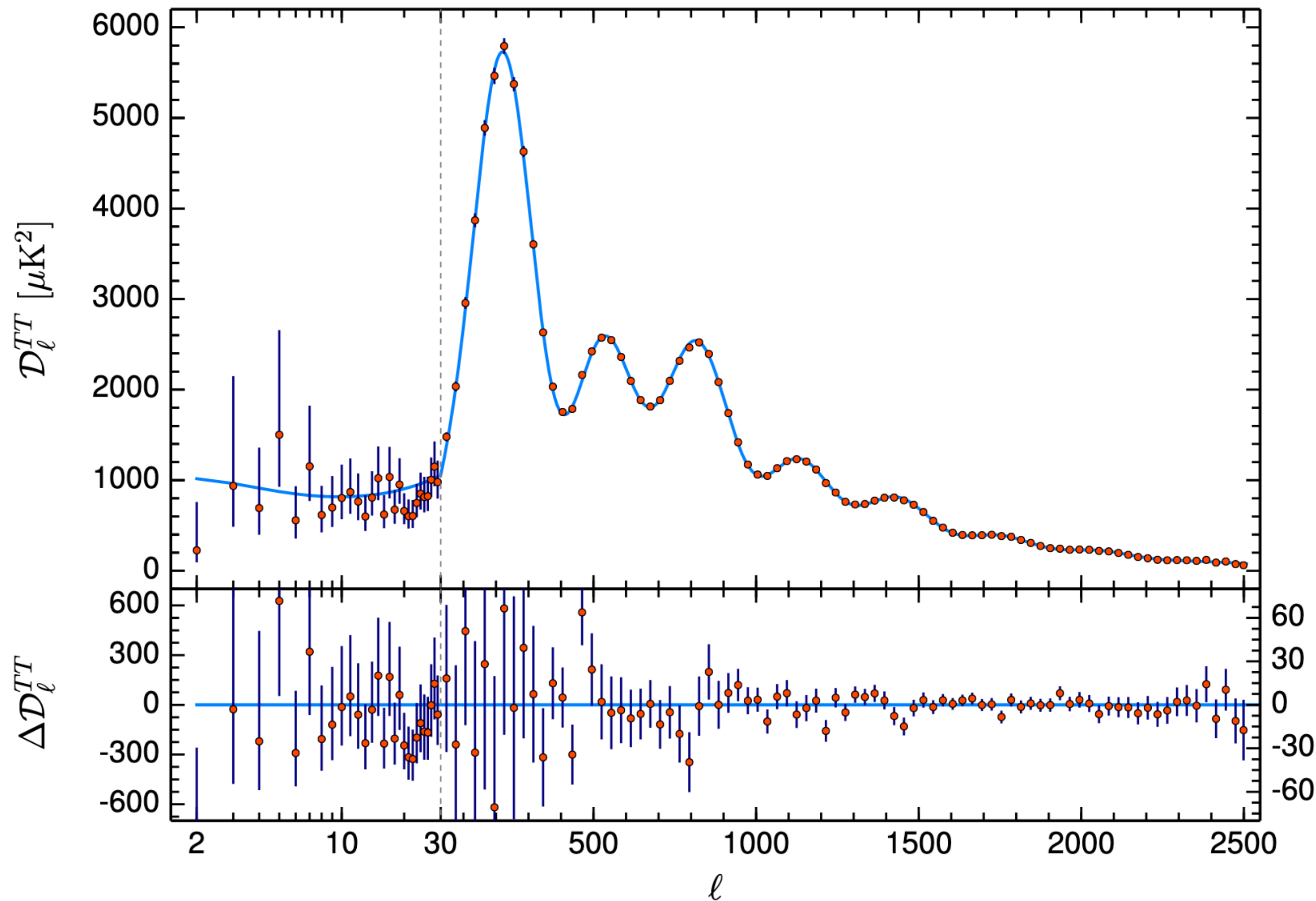


Planck 2018, 1807.06209



# The era of precision cosmology

$\Lambda$ CDM gives excellent fit to CMB anisotropy spectra



Also explains:

- Baryon acoustic oscillations,
- Supernovae Ia,
- Light element abundances,
- Large Scale Structure, etc

Planck 2018, 1807.06209



# Challenges to the $\Lambda$ CDM paradigm

## 1. What is dark matter? And dark energy?

---

- Are they made of **particles**?
- Are they made of **single species**?
- How are they **produced**?
- What is their **lifetime**?
- And their **mass**?



# Challenges to the $\Lambda$ CDM paradigm

## 2. Several discrepancies emerged in recent years

---

- $S_8$  with weak-lensing data  
[KiDS-1000 2007.15632](#)
- $H_0$  with local measurements  
[Riess++ 2012.08534](#)



# Challenges to the $\Lambda$ CDM paradigm

## 2. Several discrepancies emerged in recent years

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- $S_8$  with weak-lensing data  
KiDS-1000 2007.15632
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Riess++ 2012.08534

### *Unaccounted systematics?*

- Less exotic explanation ✓
- Difficult to account for all discrepancies ✗

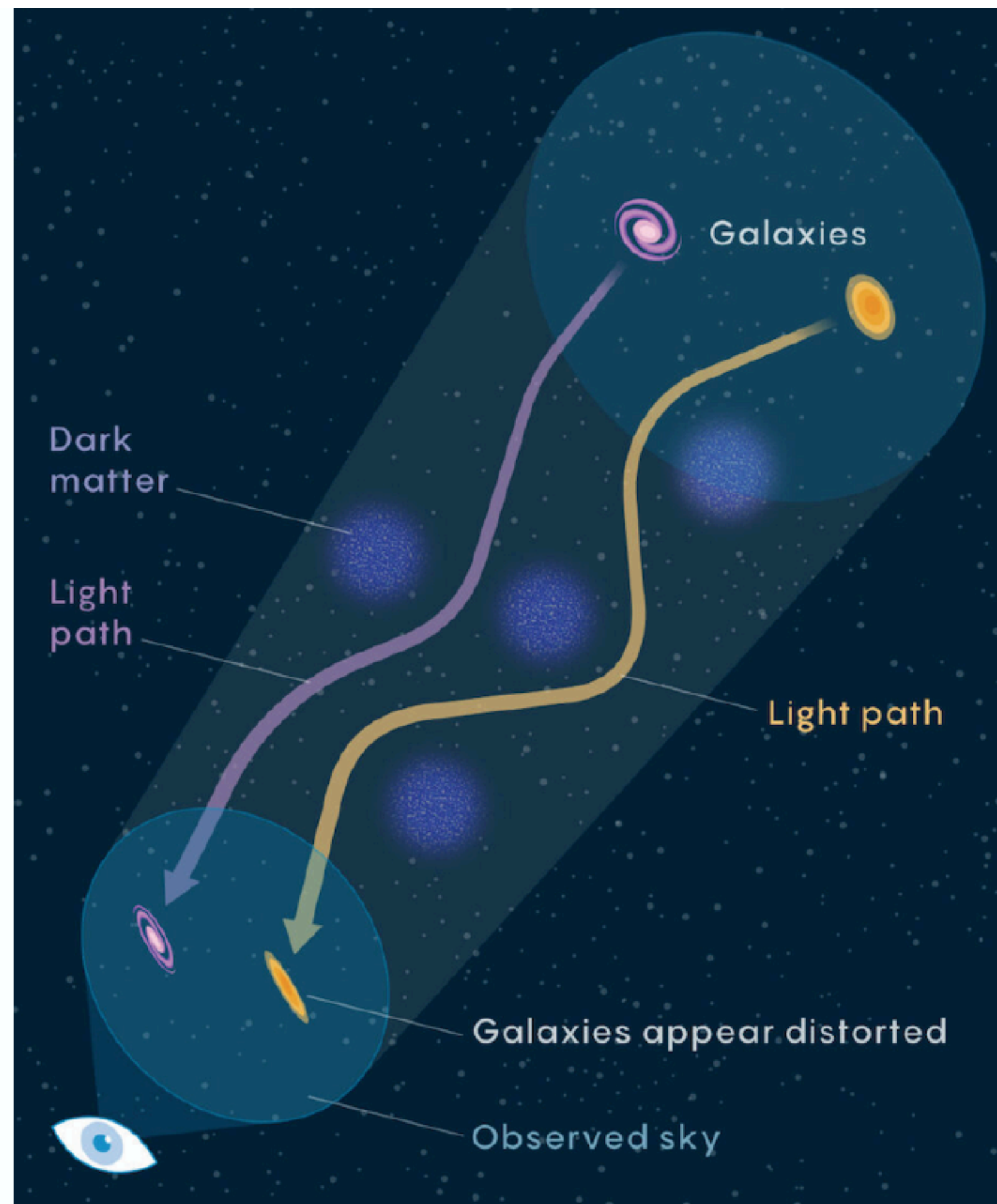
### *Physics beyond $\Lambda$ CDM?*

- Reveal properties about the dark sector ✓
- Very challenging ✗



# The $S_8$ tension

Weak-lensing surveys are mainly sensible to  $S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3}$



KiDS+BOSS+2dfLenS\*:

$$S_8 = 0.766^{+0.020}_{-0.014}$$

Planck (*under*  $\Lambda$ CDM):

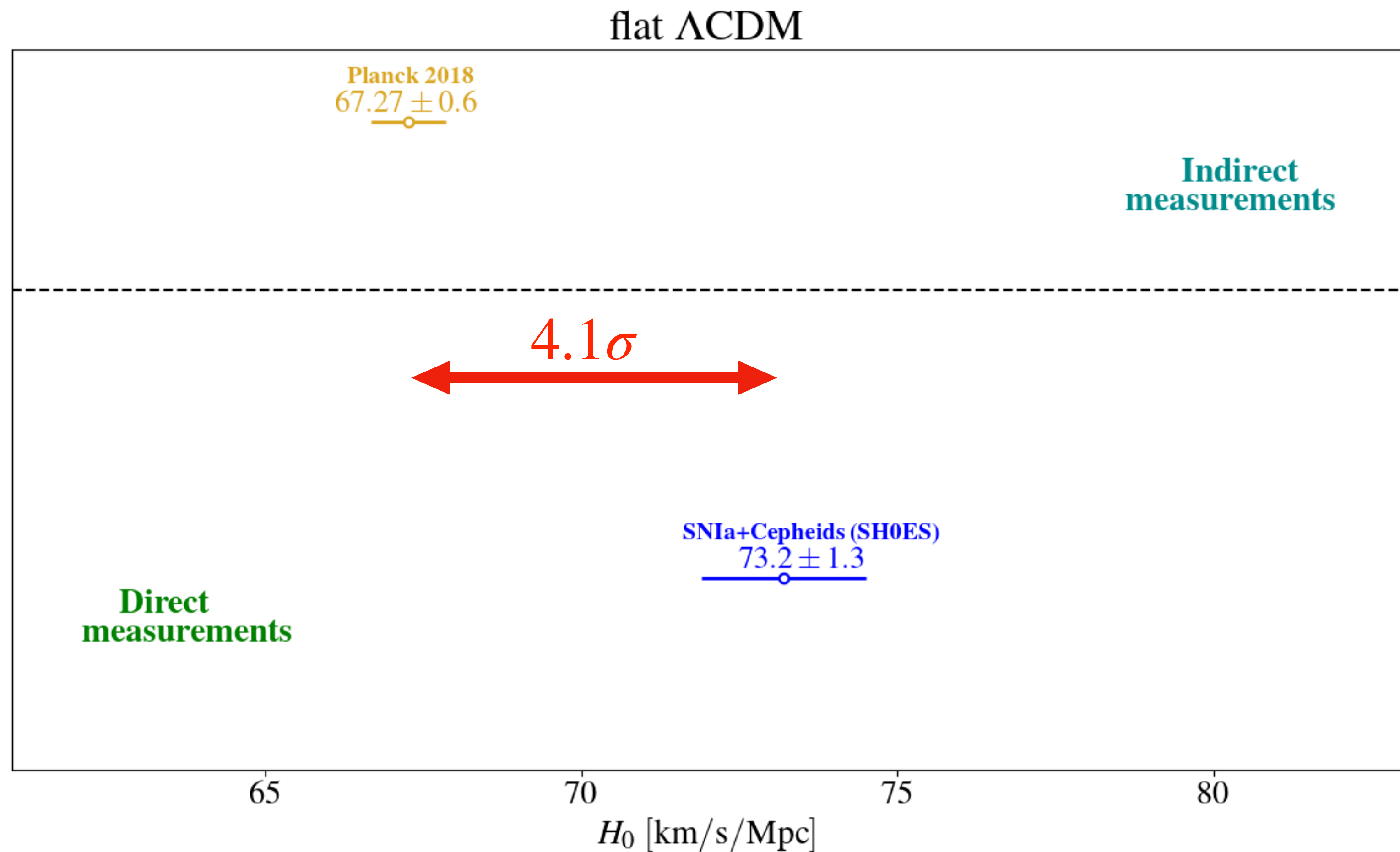
$$S_8 = 0.830 \pm 0.013$$

→  **$\sim 2 - 3\sigma$  tension**

\*Other surveys such as DES, CFHTLenS or HSC yield similar results

# The $H_0$ tension

Planck (*under  $\Lambda$ CDM*) and SHoES measurements are in **4.1 $\sigma$  tension**

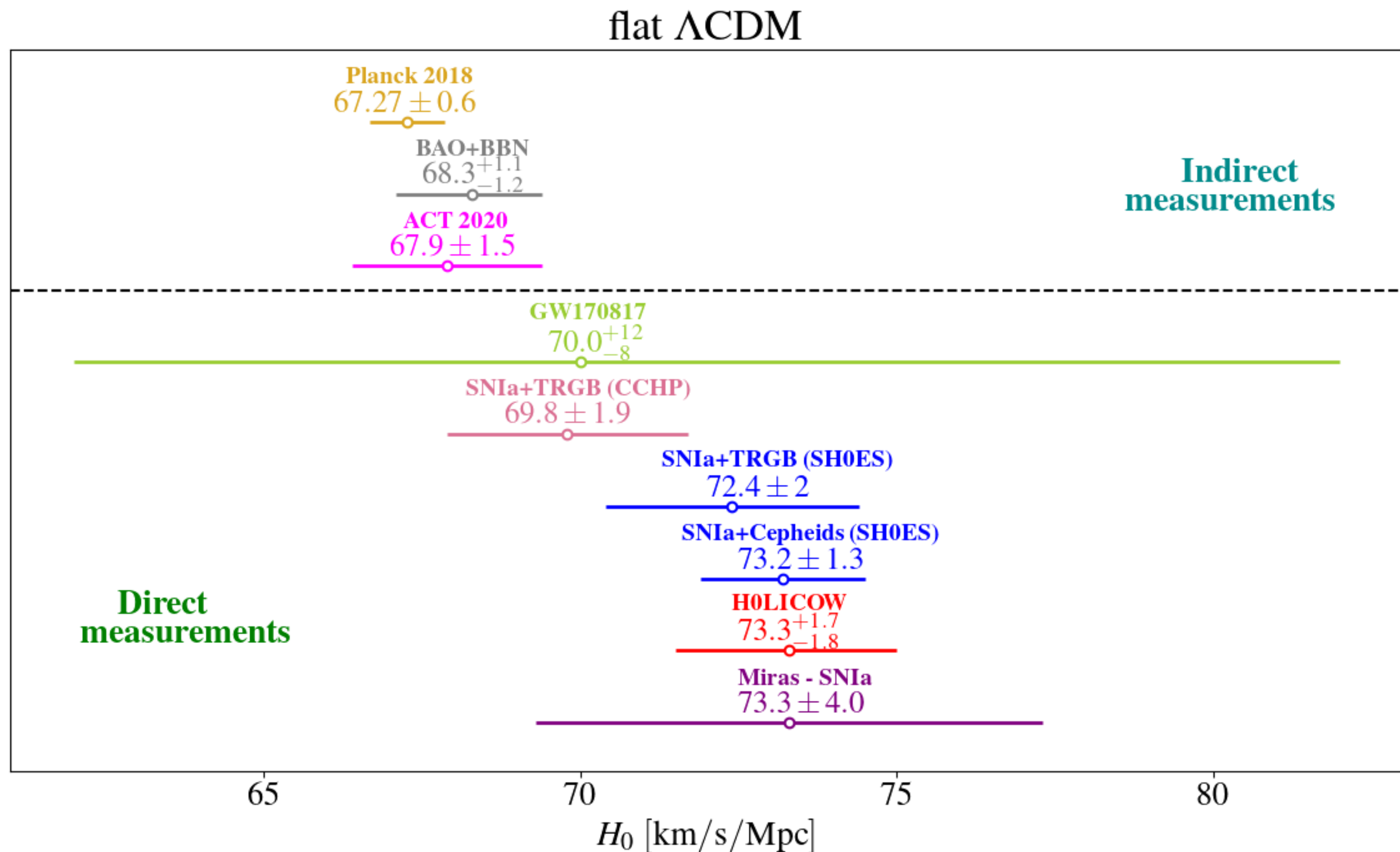




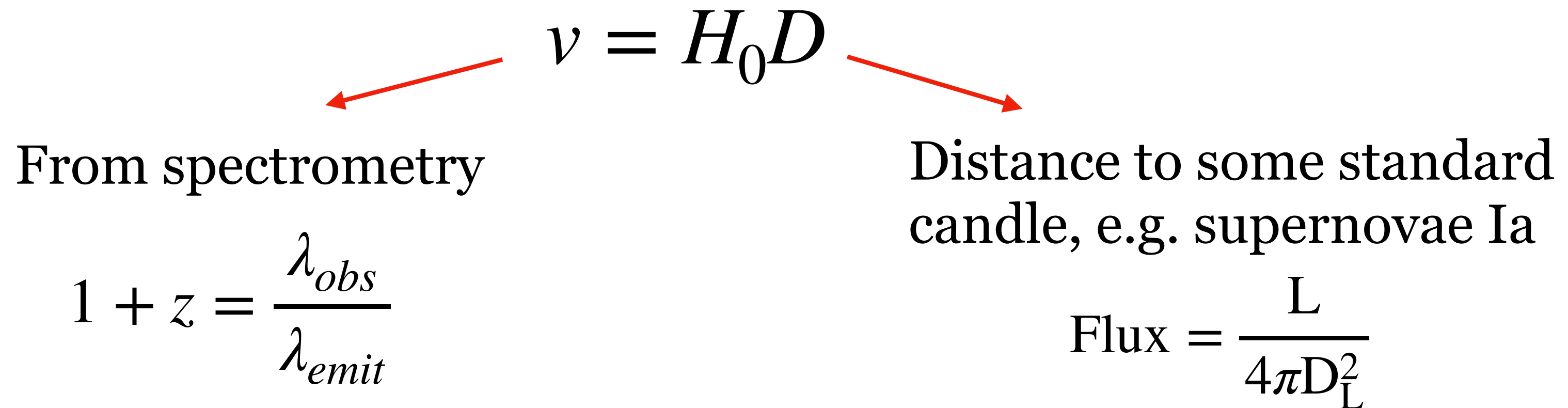
# The $H_0$ tension

Planck (*under  $\Lambda$ CDM*) and SHoES measurements are in **4.1 $\sigma$  tension**

High- and low-redshift probes are typically discrepant

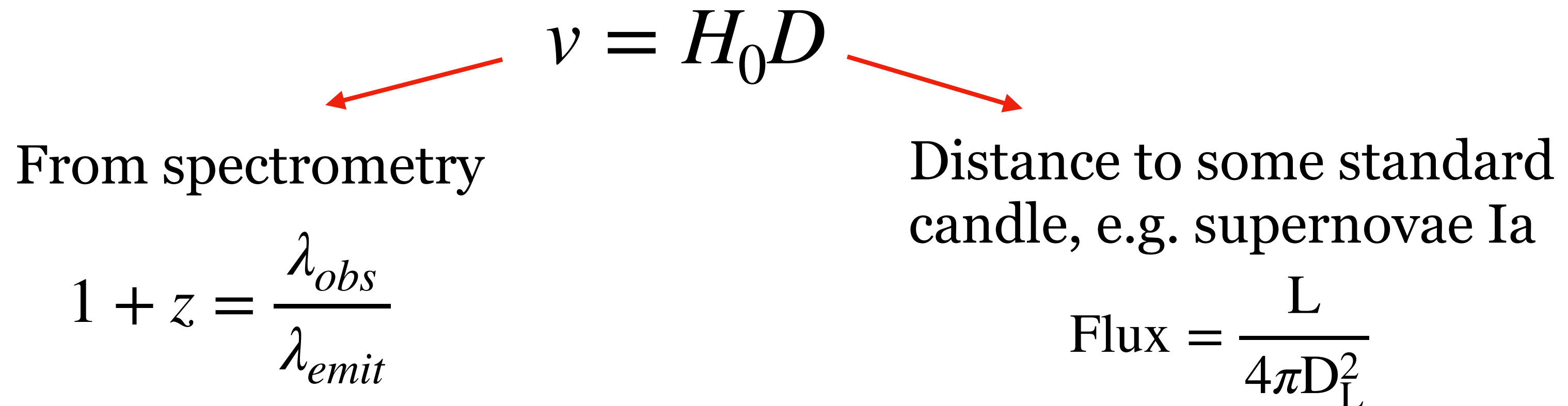


# How does SH0ES determine $H_0$ ?





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Focus on small  $z^*$ , for which distances are approx. **model-independent**

$$D_L = (1 + z) \int_0^z \frac{cdz'}{H(z')} \xrightarrow{z \ll 1} czH_0^{-1} \simeq vH_0^{-1}$$

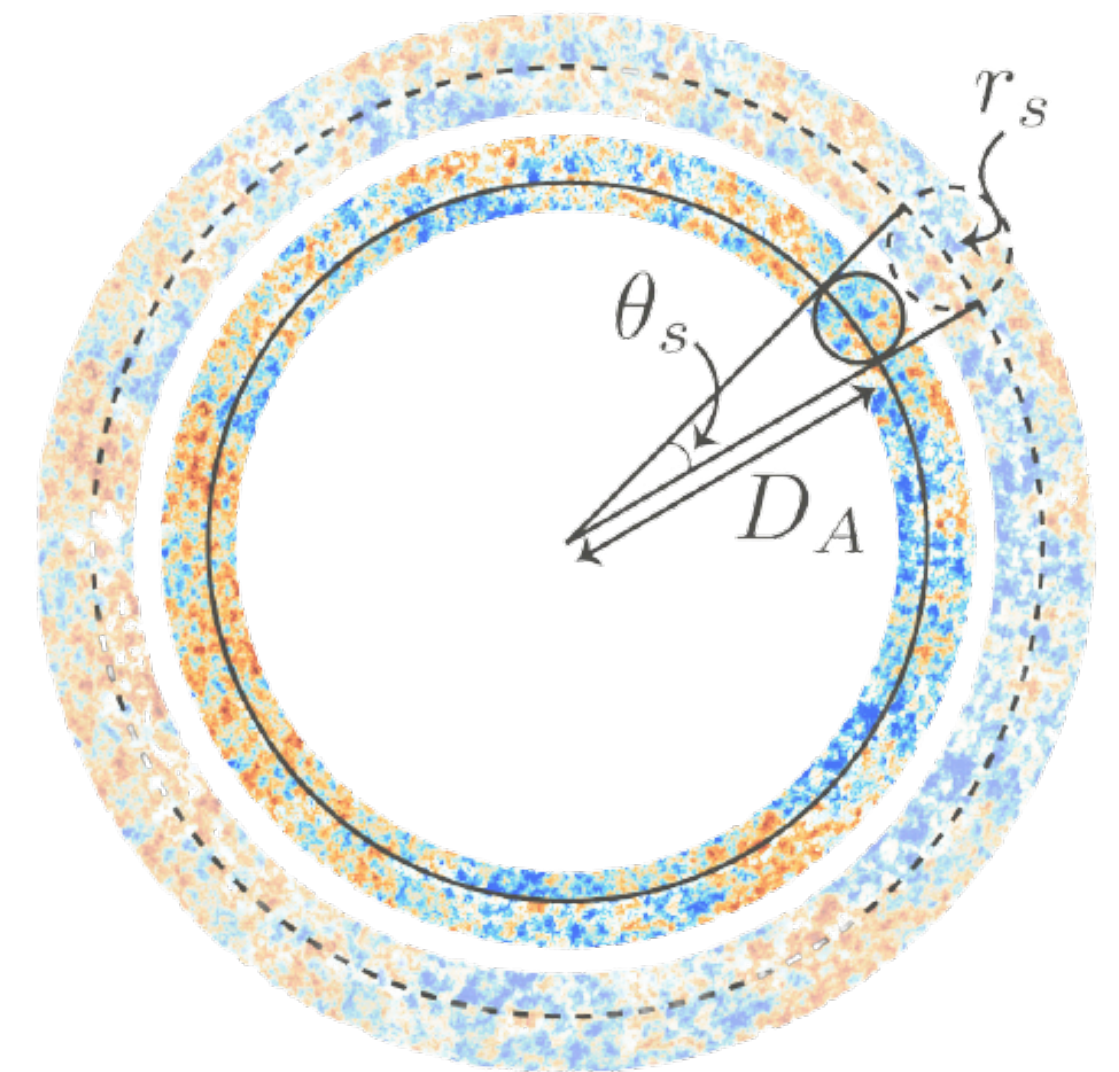
$$\text{where } H^2(z) = \frac{8\pi G}{3} \sum_i \rho_i(z)$$

\*But not too small, to make sure peculiar velocities are negligible

# How does Planck determine $H_0$ ?

Angular size of the sound horizon is measured at the 0.04 % precision

$$\theta_s = \frac{r_s(z_{\text{rec}})}{D_A(z_{\text{rec}})} = \frac{\int_0^{\tau_{\text{rec}}} c_s(\tau) d\tau}{\int_{\tau_{\text{rec}}}^{\tau_0} c d\tau}$$



T. Smith



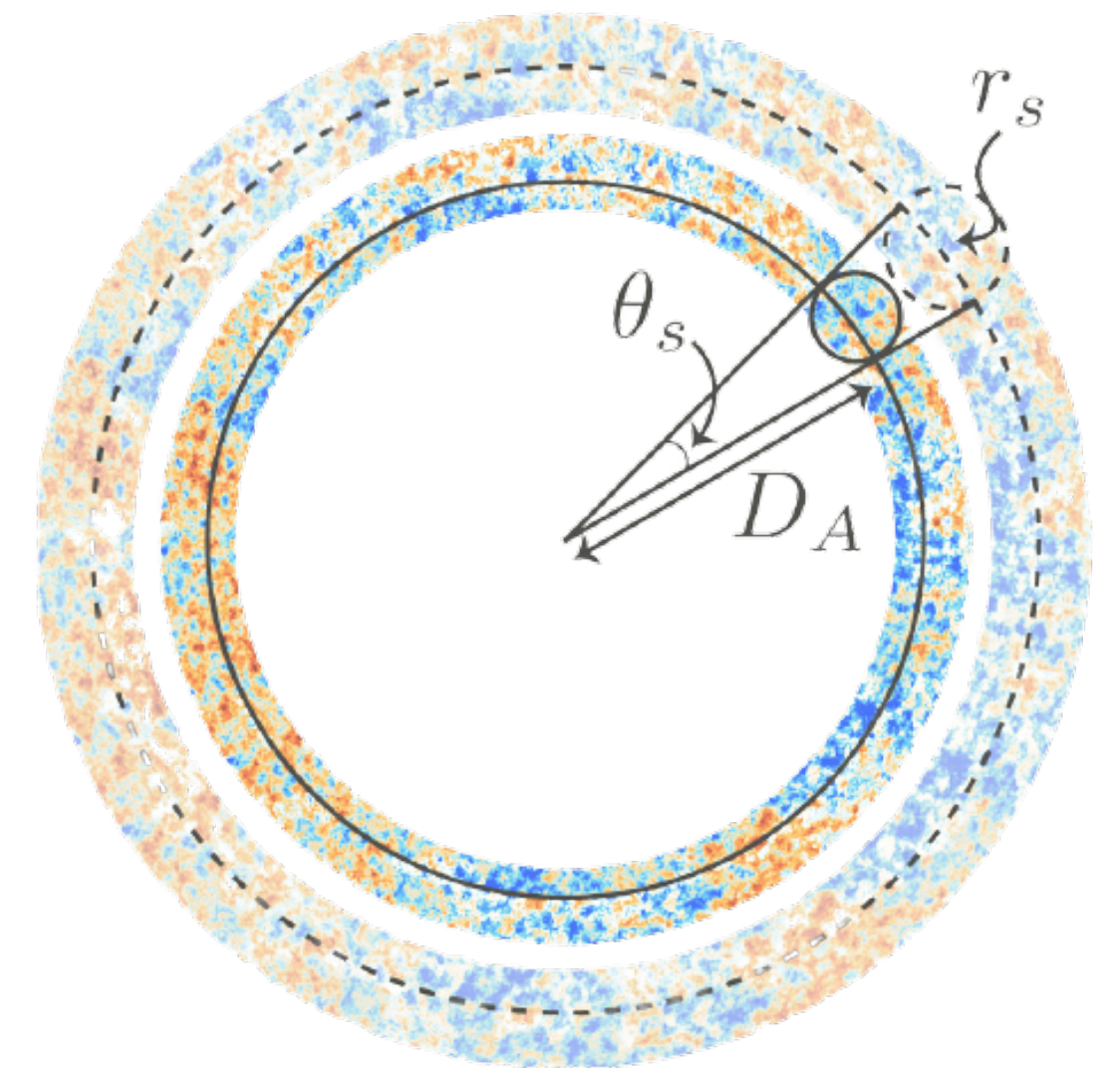
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with  $D_A \propto 1/H_0 = 1/\sqrt{\rho_{\text{tot}}(0)}$

model prediction of  $r_s$  + measurement of  $\theta_s \longrightarrow H_0$



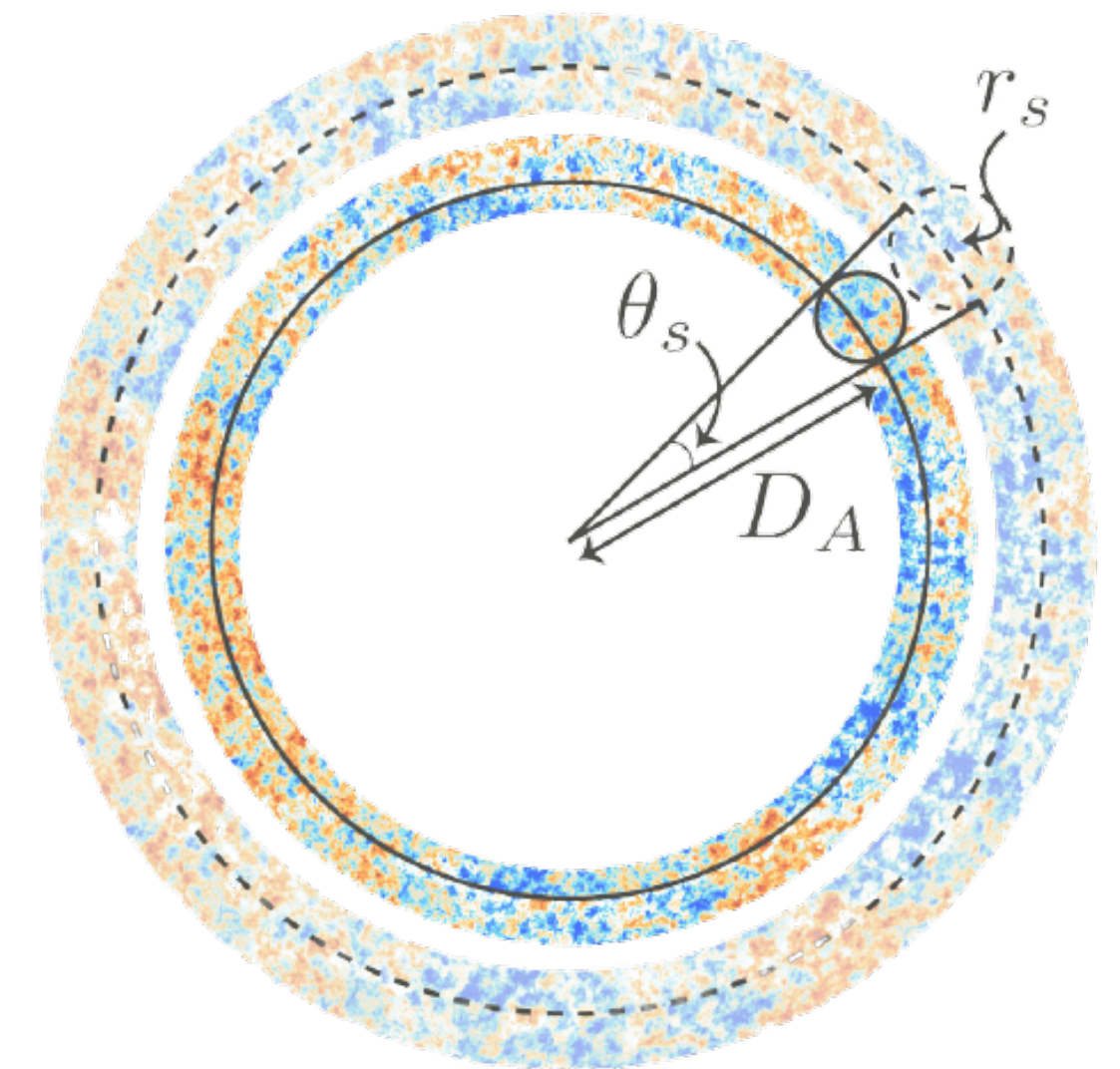
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model prediction of  $r_s$  + measurement of  $\theta_s \longrightarrow H_0$

T. Smith

## *Early-time solutions*

Decrease  $r_s(z_{\text{rec}})$  at fixed  $\theta_s$  to decrease  $D_A(z_{\text{rec}})$  and increase  $H_0$

**Ex :  $\Delta N_{\text{eff}} > 0$**

## *Late-time solutions*

$r_s(z_{\text{rec}})$  and  $D_A(z_{\text{rec}})$  are fixed, but  $D_A(z < z_{\text{rec}})$  is changed to allow higher  $H_0$

**Ex :  $w < -1$**



## **II. The $H_0$ Olympics: quantifying the success of a resolution**

*In collaboration with* Nils Schöneberg, Andrea Pérez Sánchez,  
Samuel J. Witte, Vivian Poulin and Julien Lesgourgues

# Lost in the landscape of solutions

- Cosmological tensions have become a **very hot topic** (specially the  $H_0$  tension)



# Lost in the landscape of solutions

- Cosmological tensions have become a **very hot topic** (specially the  $H_0$  tension)
- [Di Valentino, Mena++ 2103.01183](#)  $\longrightarrow$  recent review of solutions, **more than 1000 refs !**

## Early Dark Energy Can Resolve The Hubble Tension

Vivian Poulin<sup>1</sup>, Tristan L. Smith<sup>2</sup>, Tanvi Karwal<sup>1</sup>, and Marc Kamionkowski<sup>1</sup>

## Relieving the Hubble tension with primordial magnetic fields

Karsten Jedamzik<sup>1</sup> and Levon Pogosian<sup>2,3</sup>

## The Neutrino Puzzle: Anomalies, Interactions, and Cosmological Tensions

Christina D. Kreisch,<sup>1,\*</sup> Francis-Yan Cyr-Racine,<sup>2,3,†</sup> and Olivier Doré<sup>4</sup>

## Rock 'n' Roll Solutions to the Hubble Tension

Prateek Agrawal<sup>1</sup>, Francis-Yan Cyr-Racine<sup>1,2</sup>, David Pinner<sup>1,3</sup>, and Lisa Randall<sup>1</sup>

## The Hubble Tension as a Hint of Leptogenesis and Neutrino Mass Generation

Miguel Escudero<sup>1,\*</sup> and Samuel J. Witte<sup>2,†</sup>

## Can interacting dark energy solve the $H_0$ tension?

Eleonora Di Valentino,<sup>1,2,\*</sup> Alessandro Melchiorri,<sup>3,†</sup> and Olga Mena<sup>4,‡</sup>

## Dark matter decaying in the late Universe can relieve the $H_0$ tension

Kyriakos Vattis, Savvas M. Koushiappas, and Abraham Loeb

## A Simple Phenomenological Emergent Dark Energy Model can Resolve the Hubble Tension

XIAOLEI LI<sup>1,2</sup> AND ARMAN SHAFIELOO<sup>1,3</sup>

## Early recombination as a solution to the $H_0$ tension

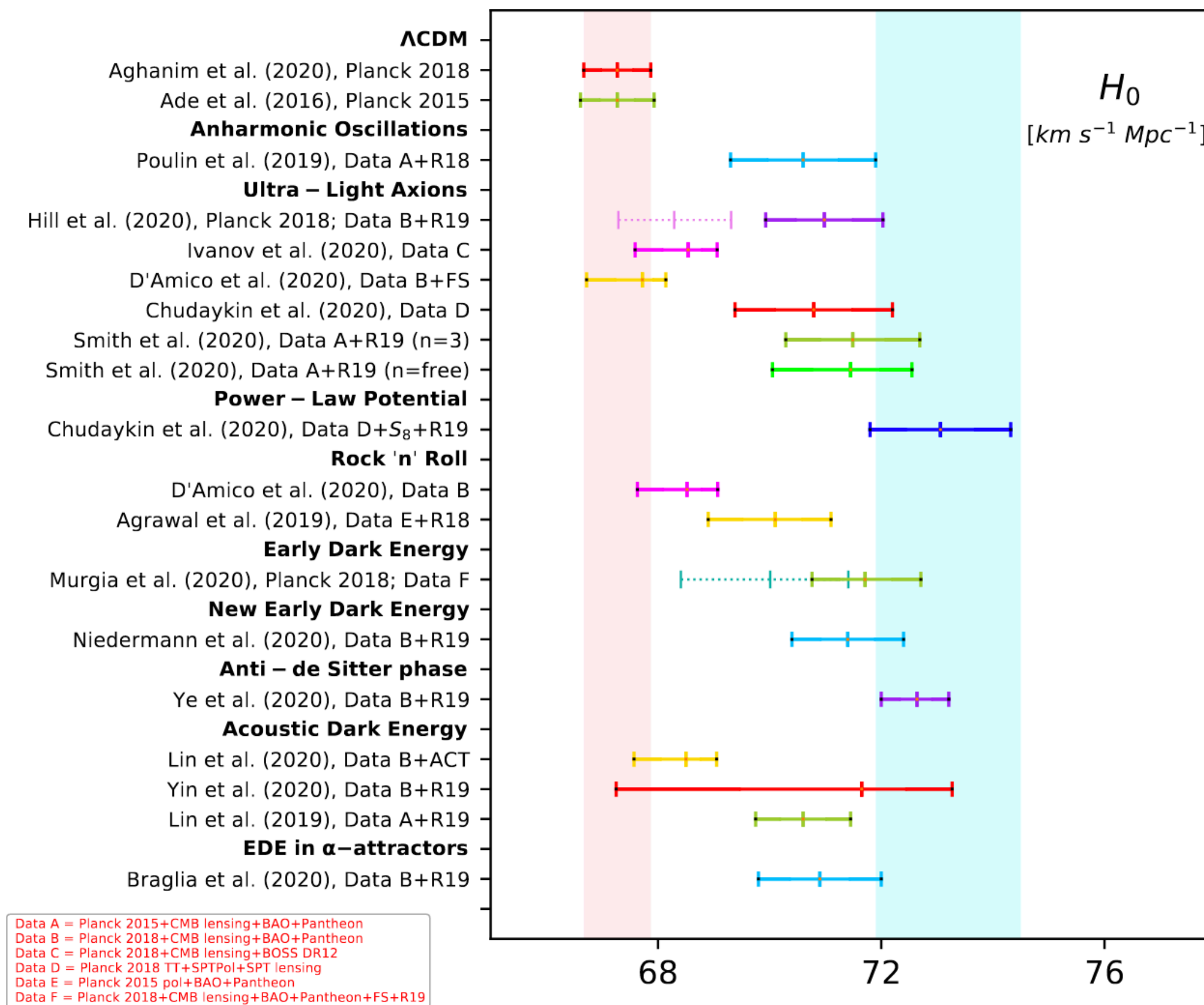
Toyokazu Sekiguchi<sup>1,\*</sup> and Tomo Takahashi<sup>2,†</sup>

## Early modified gravity in light of the $H_0$ tension and LSS data

Matteo Braglia,<sup>1,2,3,\*</sup> Mario Ballardini,<sup>1,2,3,†</sup> Fabio Finelli,<sup>2,3,‡</sup> and Kazuya Koyama<sup>4,§</sup>

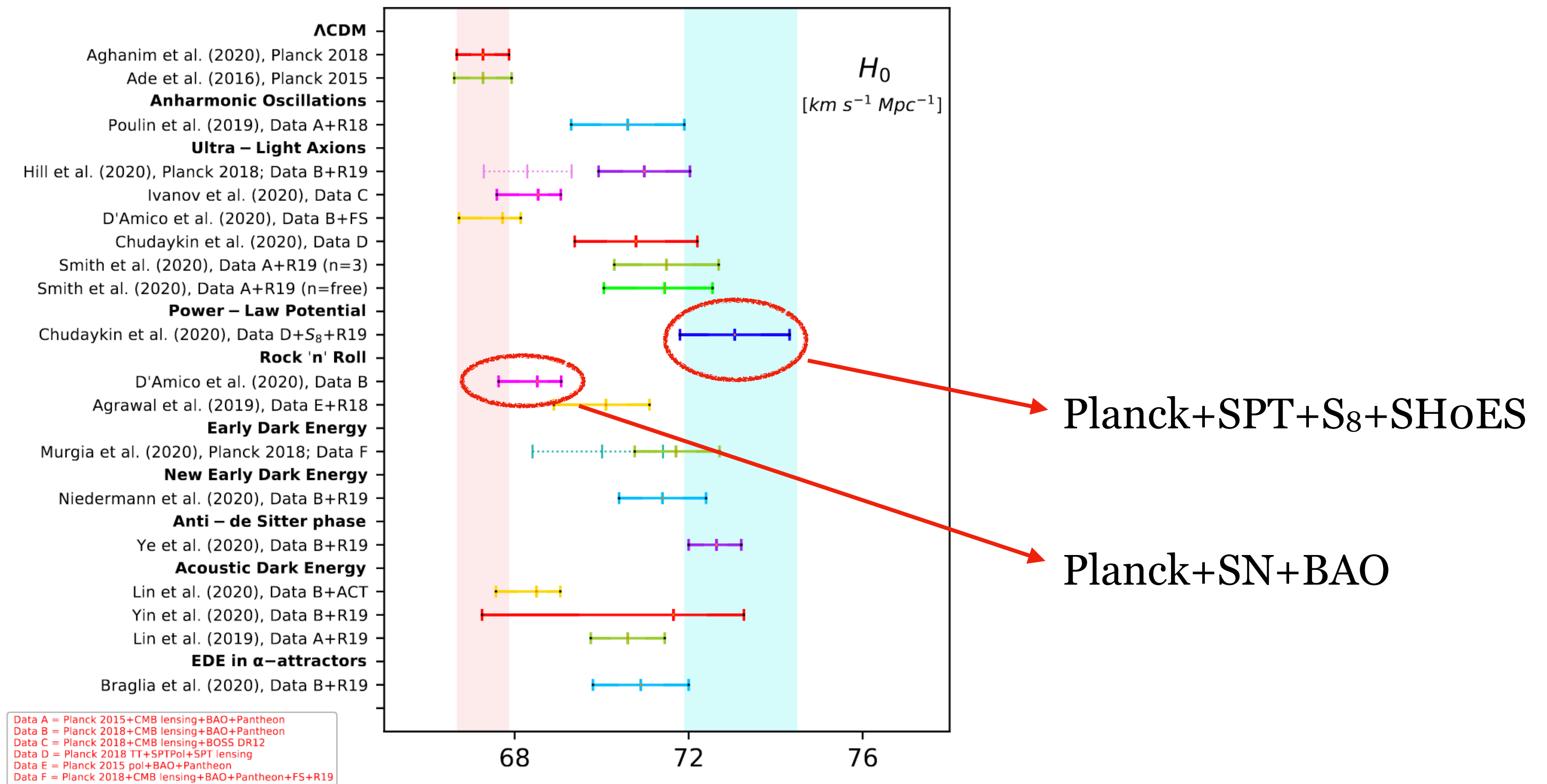
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It proves difficult to compare success of the different proposed solutions, since authors typically use **differing and incomplete combinations of data**



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# The $H_0$ Olympics

**Goal:** Take a representative **sample of proposed solutions**, and quantify the **relative success** of each using certain metrics and a wide array of data

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## Early universe

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### w Dark radiation

---

- $\Delta N_{\text{eff}}$
- Self-interacting DR
- Mixed DR
- DM-DR interactions
- Self-interacting  $\nu_s$ +DR
- Majoron- $\nu_s$  interactions

### wo Dark radiation

---

- Primordial B
- Varying  $m_e$
- Varying  $m_e + \Omega_k$
- Early Dark Energy
- New Early Dark Energy

### Late universe

---

- CPL dark energy
- PEDE
- MPEDE
- Fraction DM  $\rightarrow$  DR
- DM  $\rightarrow$  DR +WDM

# Model-independent treatment of the SH0ES data

The cosmic distance ladder method *doesn't directly measure  $H_0$* .

It directly measures the intrinsic magnitude of SNIa  $M_b$  at redshifts  $0.02 \leq z \leq 0.15$ , and then obtains  $H_0$  by comparing with the apparent SNIa magnitudes  $m$

$$m(z) = M_b + 25 - 5\text{Log}_{10}H_0 + 5\text{Log}_{10}(\hat{D}_L(z))$$

where

$$\hat{D}_L(z) \simeq z \left( 1 + (1 - q_0)\frac{z}{2} - \frac{1}{6}(1 - q_0 - 3q_0^2 + j_0)z^2 \right)$$

$$q_0 = -0.53, \quad j_0 = 1 \quad (\Lambda\text{CDM assumed!})$$



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# Quantifying model success

**Criterion 1:** Can we get high values of  $H_0$  without the inclusion of a SHoES prior?

## Gaussian tension GT

$$\frac{\bar{x}_D - \bar{x}_{SHoES}}{\sqrt{\sigma_D^2 + \sigma_{SHoES}^2}} \text{ for } x = H_0 \text{ or } M_b$$

We demand  $GT < 3\sigma$

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We demand  $GT < 3\sigma$

## Caveats:

- Only valid for gaussian posteriors ✗
- Doesn't quantify quality of the fit ✗

Example:  $\Lambda$ CDM with fixed  $\Omega_{\text{cdm}} h^2 = 0.11$  yields  $H_0 = 71.84 \pm 0.16$  km/s/Mpc but has  $\Delta\chi^2 \simeq 106$



# Quantifying model success

**Criterion 2:** Can we get a good fit to all the data in a given model?

**$Q_{\text{DMAP}}$  tension**

$$\sqrt{\chi^2_{\text{min}, \text{D+SH0ES}} - \chi^2_{\text{min}, \text{D}}}$$

Raveri&Hu 1806.04649

We demand  $Q_{\text{DMAP}} < 3\sigma$

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Raveri&Hu 1806.04649

We demand  $Q_{\text{DMAP}} < 3\sigma$

## Caveats:

- Accounts for non-gaussianity of posteriors 
- Doesn't account for effects of over-fitting 

# Quantifying model success

**Criterion 3:** Is a model M favoured over  $\Lambda$ CDM?

**Akaike Information Criterion  $\Delta$ AIC**

$$\chi^2_{\min,M} - \chi^2_{\min,\Lambda\text{CDM}} + 2(N_M - N_{\Lambda\text{CDM}})$$

We demand  $\Delta\text{AIC} < -6.91$  \*

\*Corresponds to weak preference according to Jeffrey's scale



# Quantifying model success

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**Caveats:**

- Simple to use and prior-independent 

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# Steps of the contest

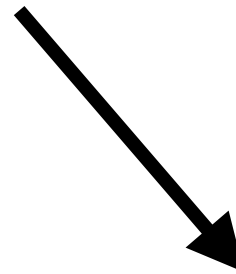
Compare all models against

- Planck 18 TTTEEE+lensing
- BAO (BOSS DR12+MGS+6dFGS)
- Pantheon SNIa catalog
- SHoES

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As long as  $\Delta AIC < 0$ , models go into finalist if criterium 2 or 3 are satisfied



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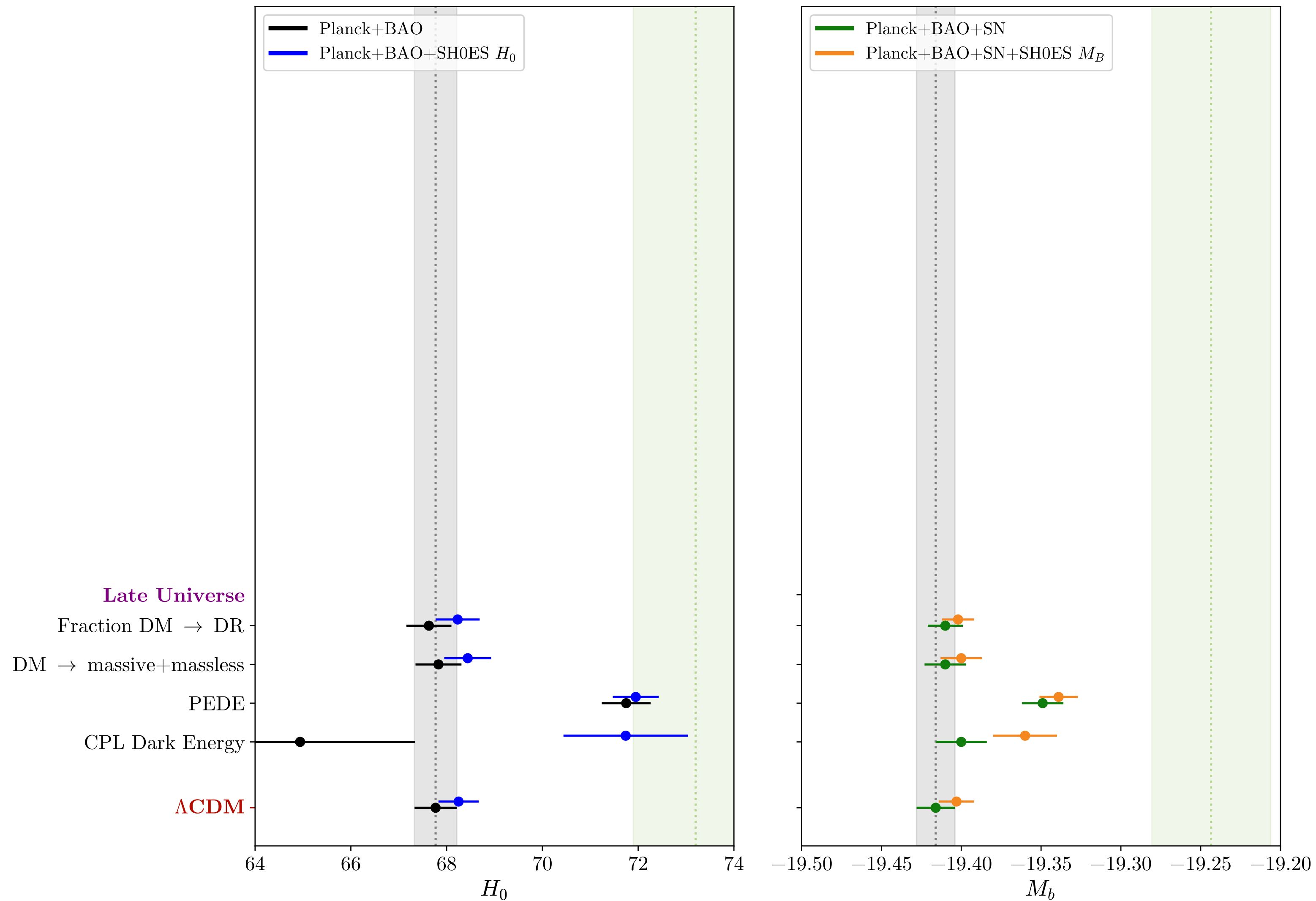
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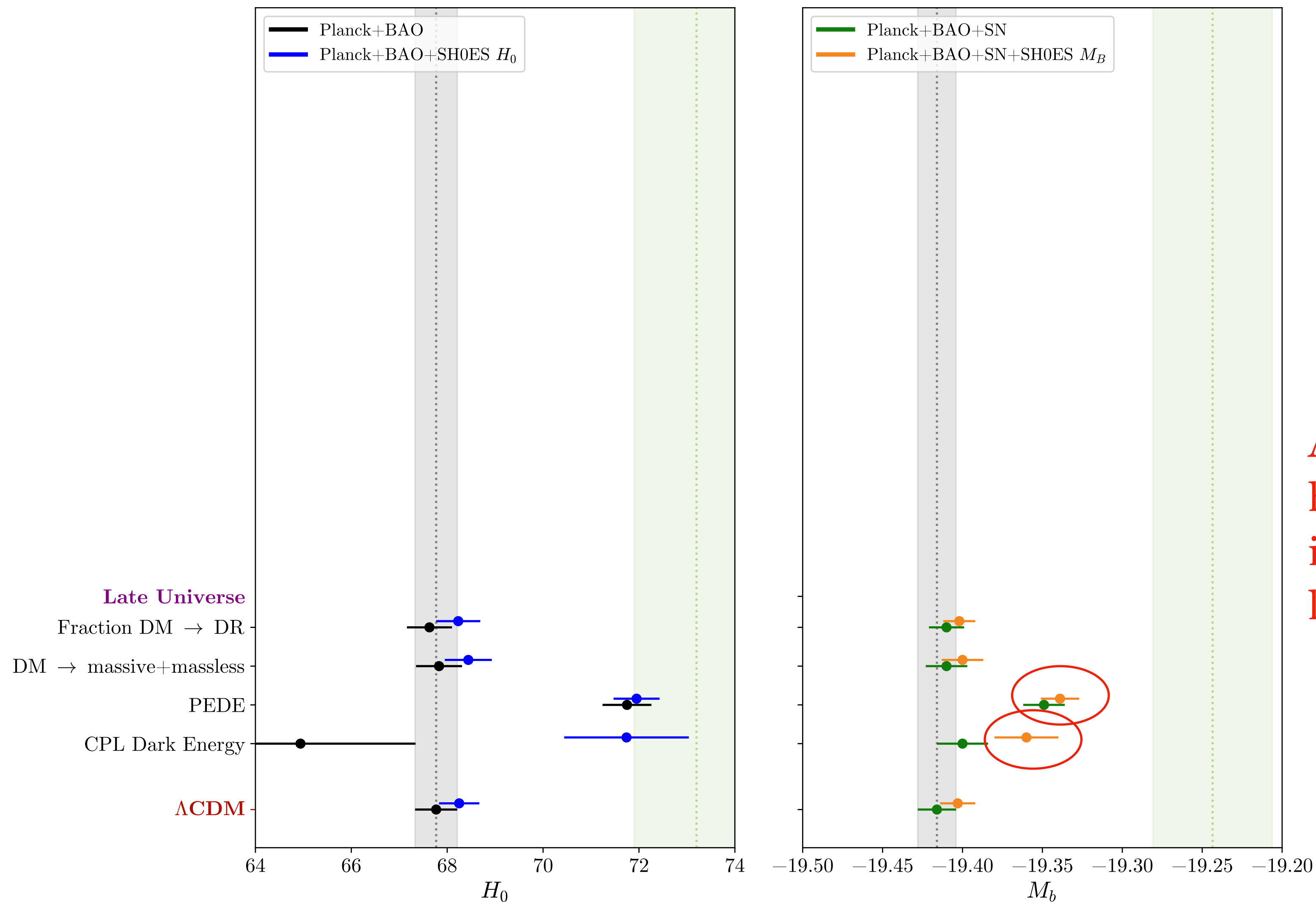
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Finalists receive bronze, silver or golden medals if they satisfy one, two or three criteria, respectively

# Results of the contest



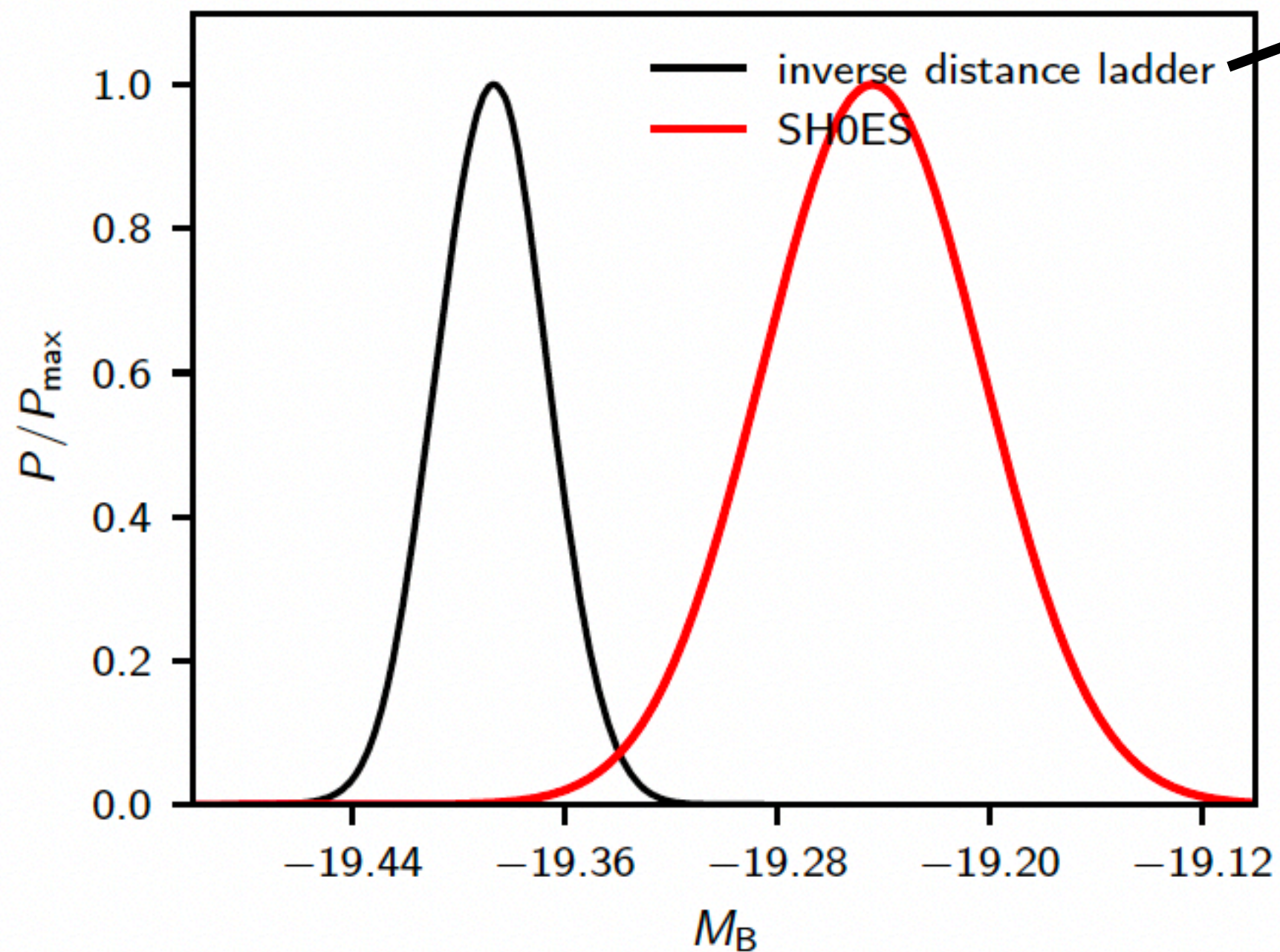
# Results of the contest



Adding  $M_b$  prior  
has a strong  
impact on  
late solutions!



# Late-time solutions are disfavoured by BAO+SNIa



Efstathiou 2103.08723

Given  $r_s$ , obtain  $D_A$  using BAO data

$$\theta_d(z)^\perp = \frac{r_s(z_{\text{drag}})}{D_A(z)}, \quad \theta_d(z)^\parallel = r_s(z_{\text{drag}})H(z)$$

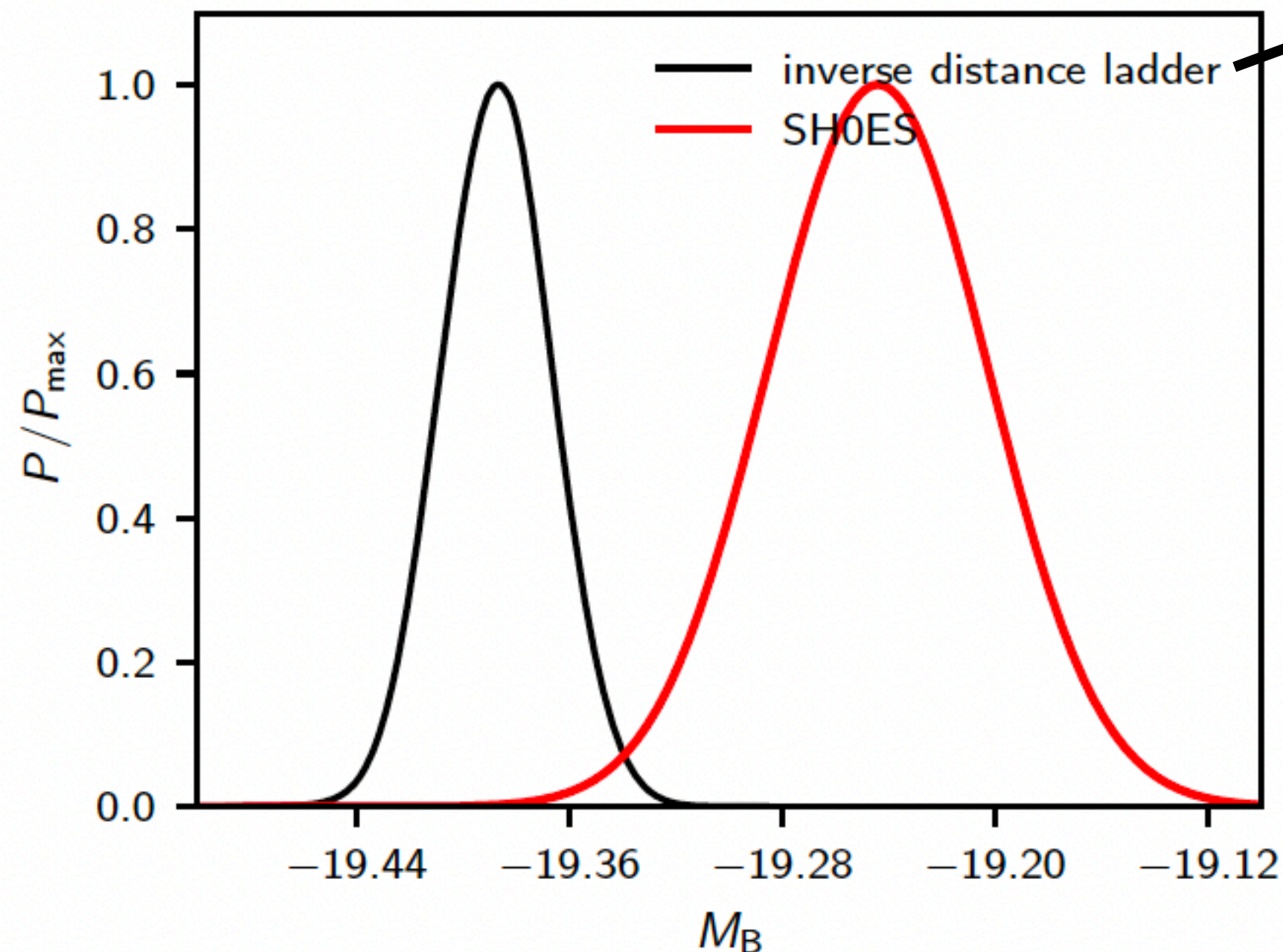
$$D_L(z) = D_A(z)(1+z)^2$$

Obtain  $M_b$  from calibration const. of SNIa

$$m(z) = 5\text{Log}_{10}D_L(z) + \text{const}$$



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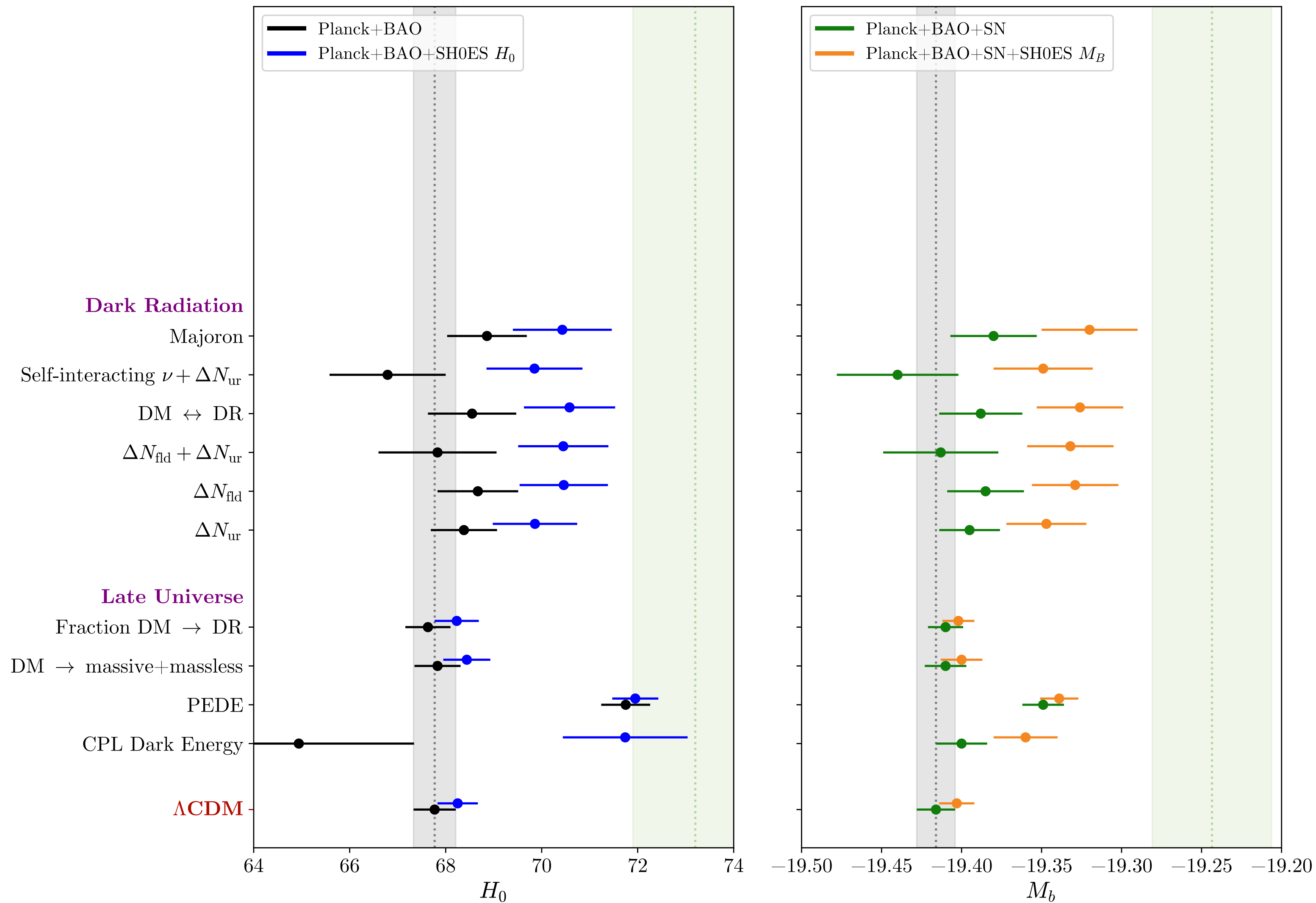
$$m(z) = 5\text{Log}_{10}D_L(z) + \text{const}$$

For  $r_s^{\Lambda\text{CDM}} = 147$  Mpc, **inverse distance ladder** disagrees with SH0ES

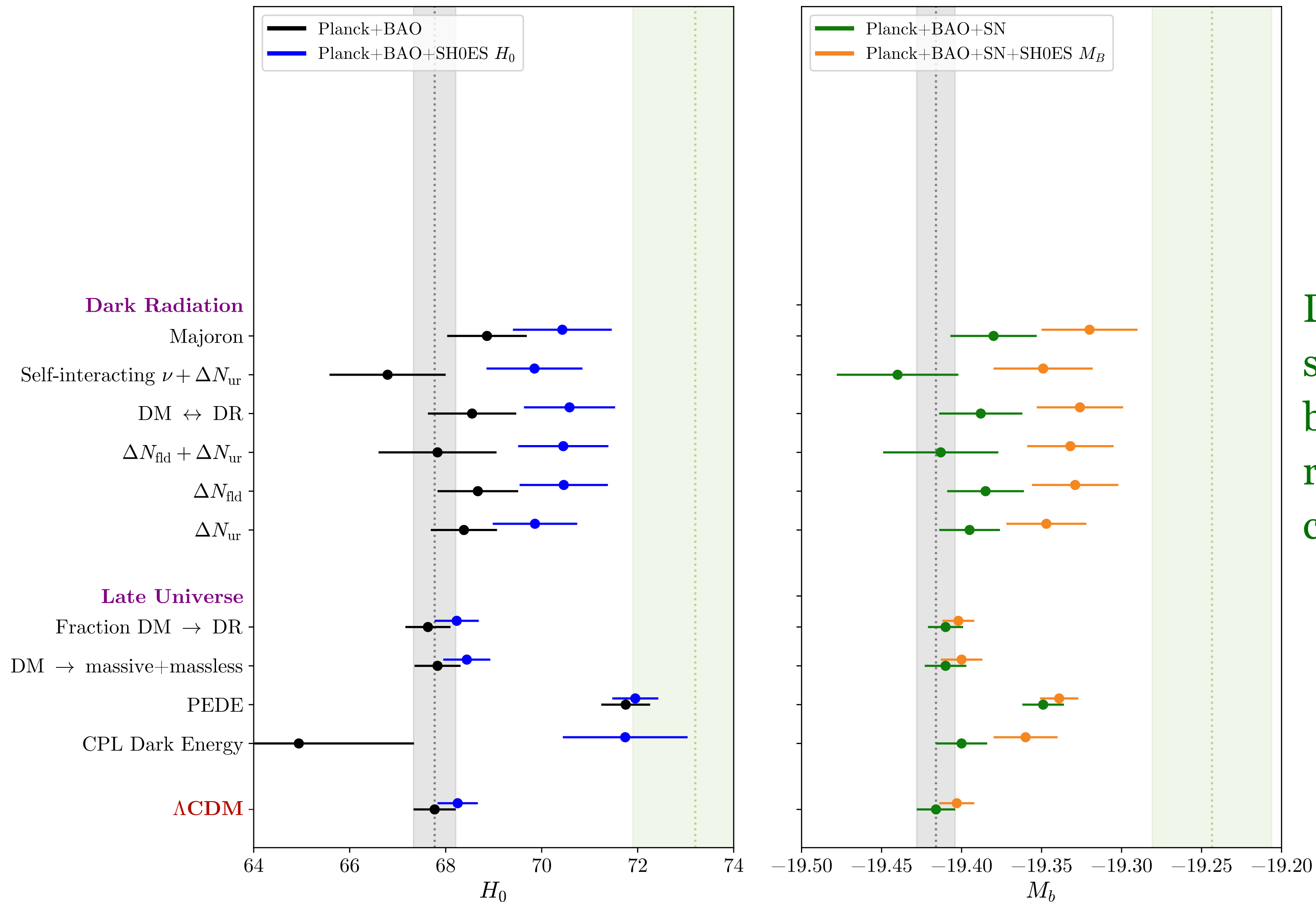
To make the two determinations agree, one is forced to **reduce  $r_s$**

**Ex:** *Early Dark Energy or exotic neutrino interactions*

# Results of the contest

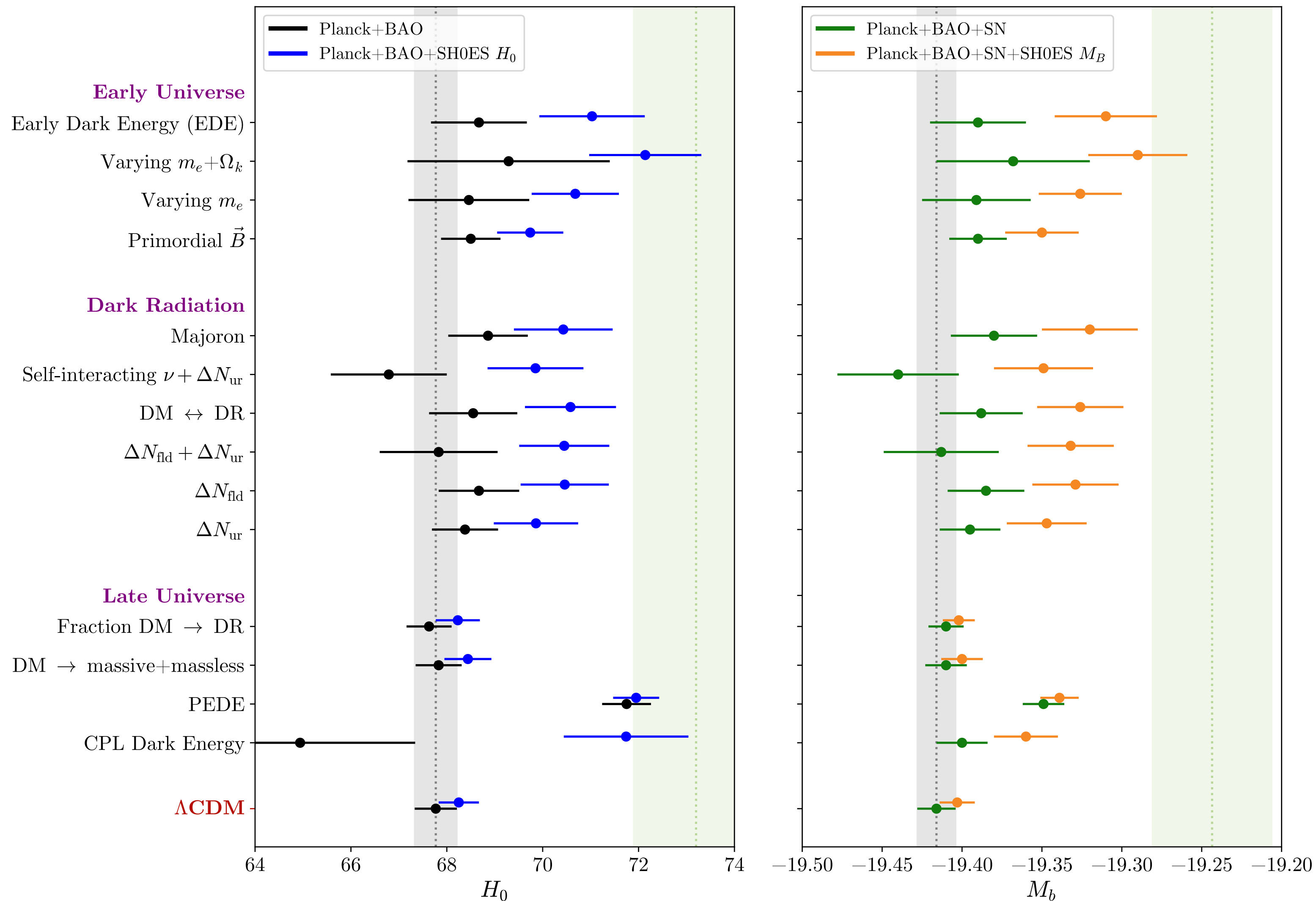


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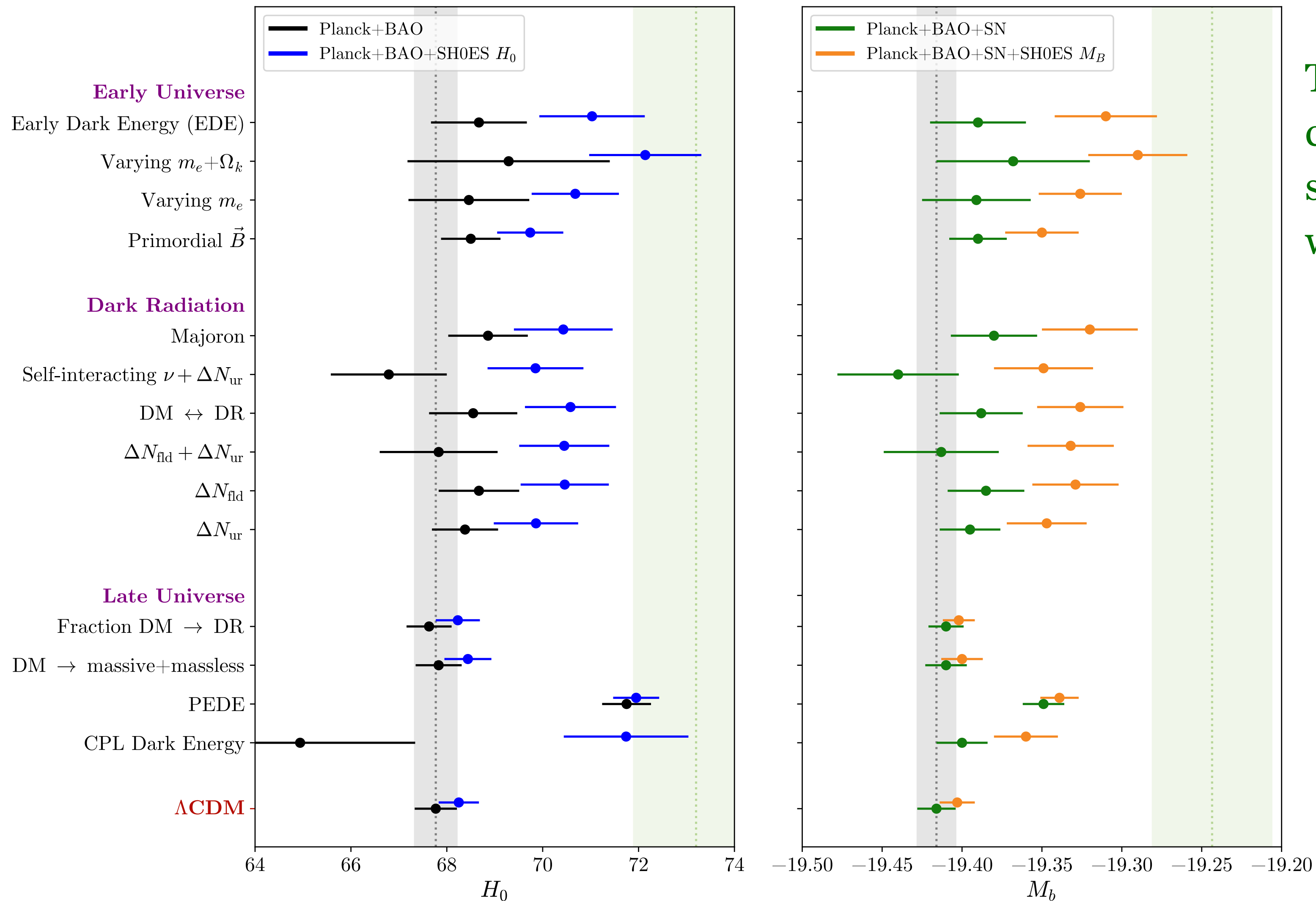
Dark radiation solutions work better, but remain very constrained

# Results of the contest



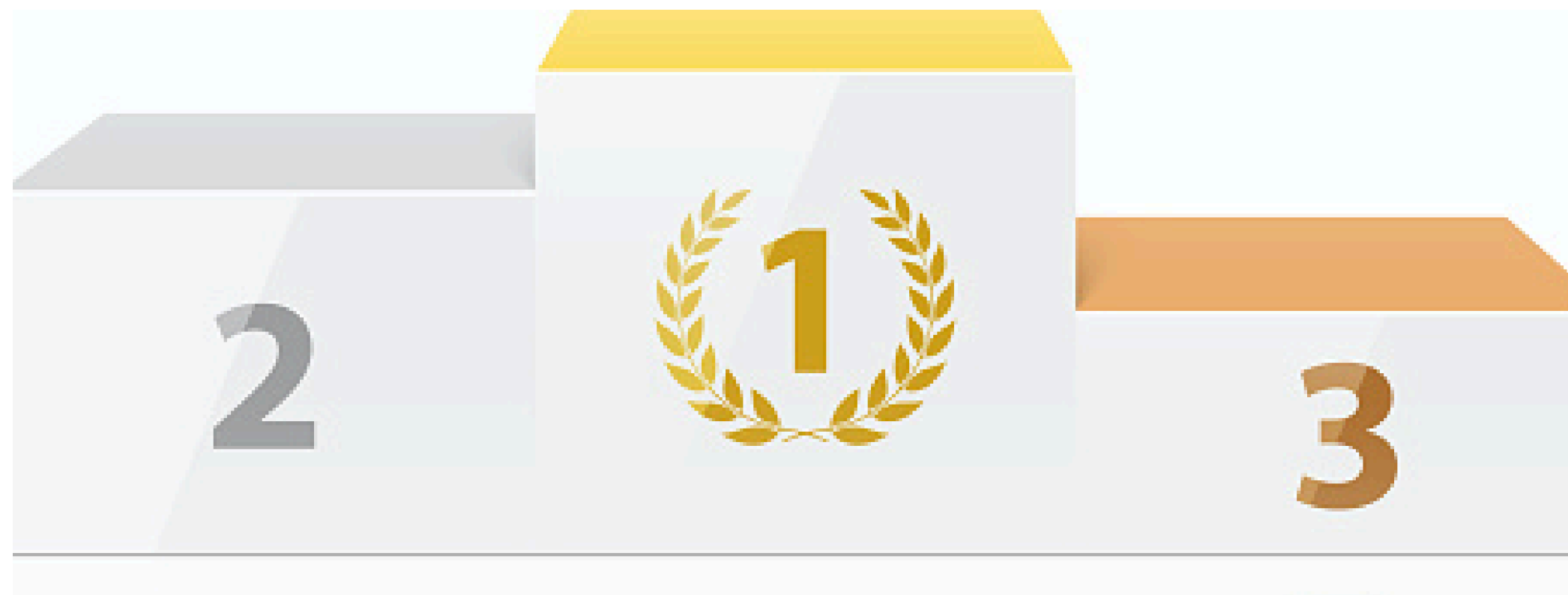


# Results of the contest



This is the category of solutions that work the best

# Results of the contest



# Results of the contest



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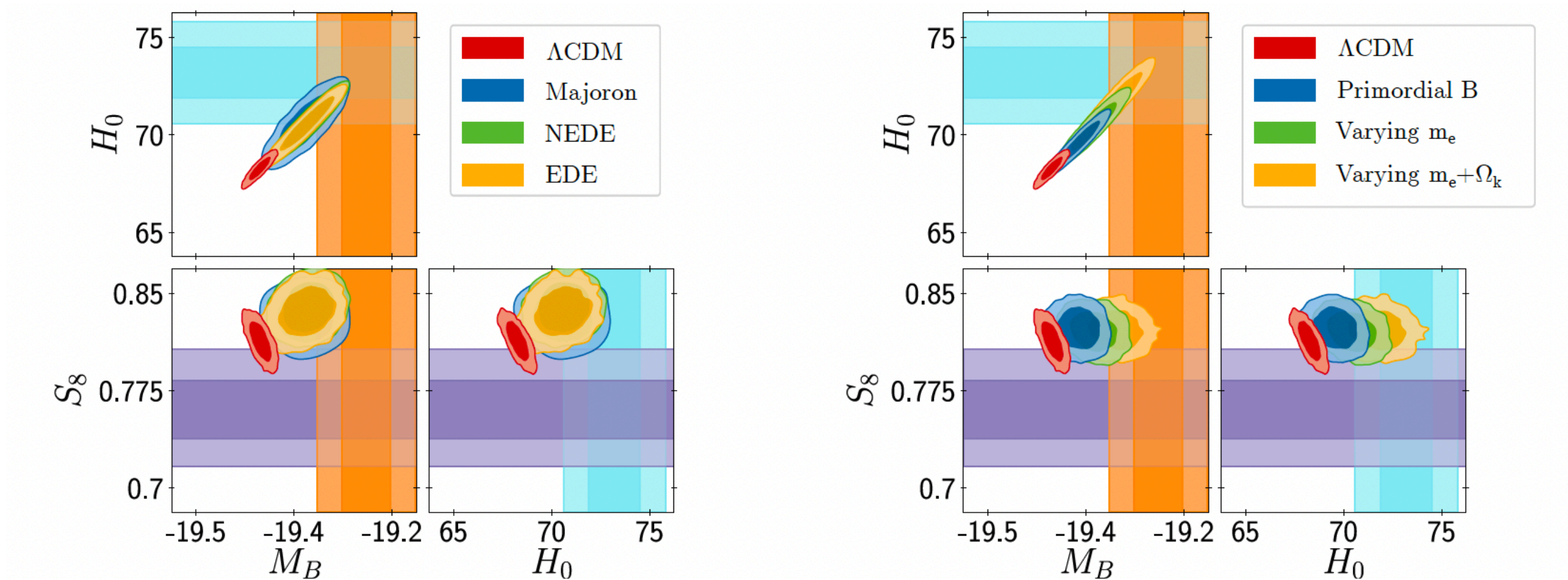


# Results of the contest



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Unfortunately, the most successful models are unable to explain the  $S_8$  tension

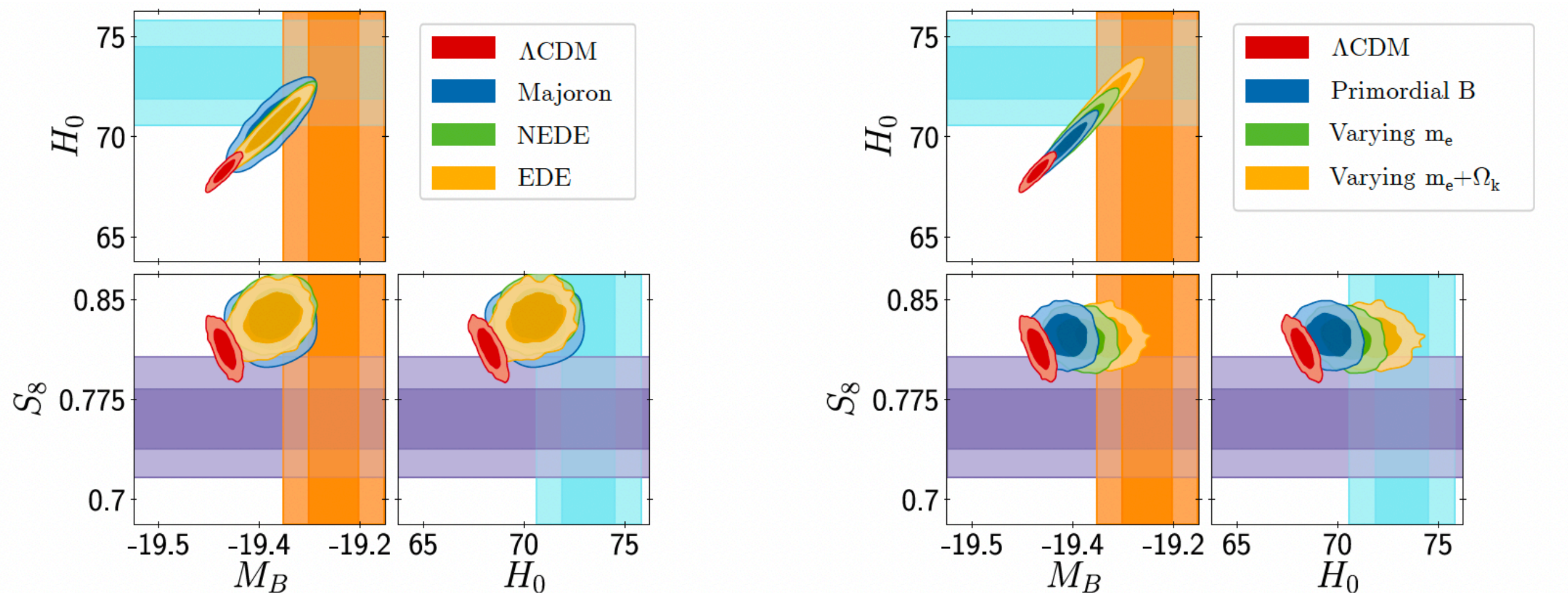


Schöneberg, GFA, Pérez, Witte, Poulin, Lesgourgues 2107.10291

Does this mean that adding **Large Scale Structure** data rules out the resolution of some of the winners (e.g. **Early Dark Energy**)?

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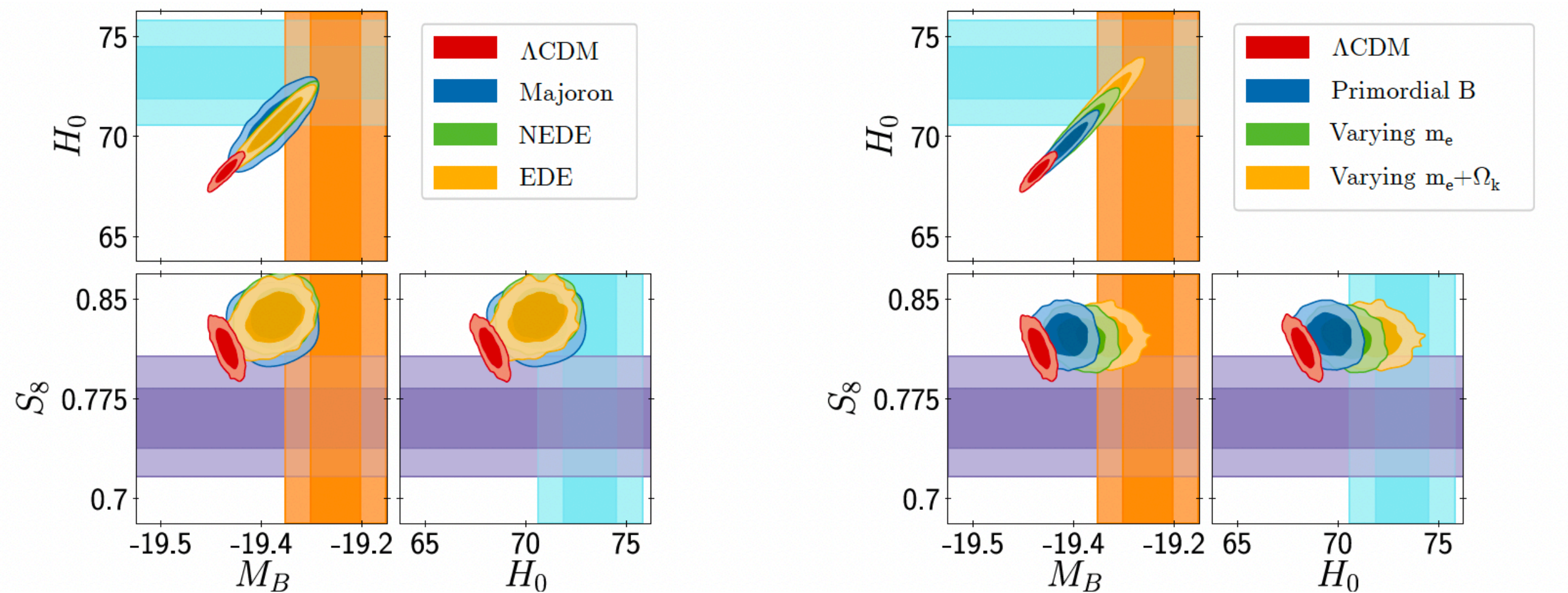
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Does this mean that adding **Large Scale Structure** data rules out the resolution of some of the winners (e.g. **Early Dark Energy**)?

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Is there any model that could explain the  $S_8$  anomaly?



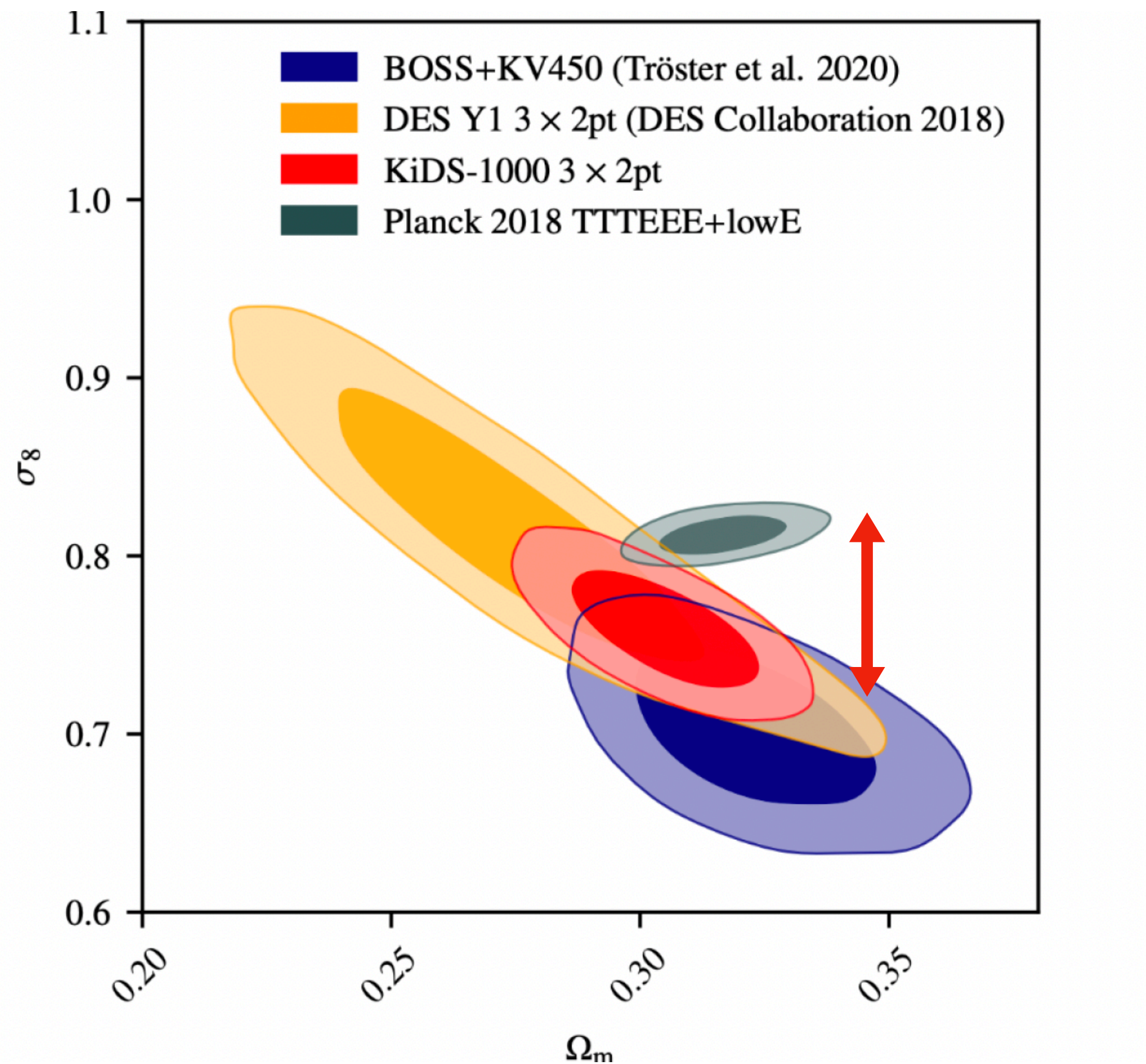
# **III. Explaining the $S_8$ tension with Decaying Dark Matter**

*In collaboration with* Riccardo Murgia, Vivian Poulin and Julien Laval

# What is needed to resolve the $S_8$ tension?

Di Valentino++ 2008.11285

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3}$$



$\Omega_m$  should be left unchanged

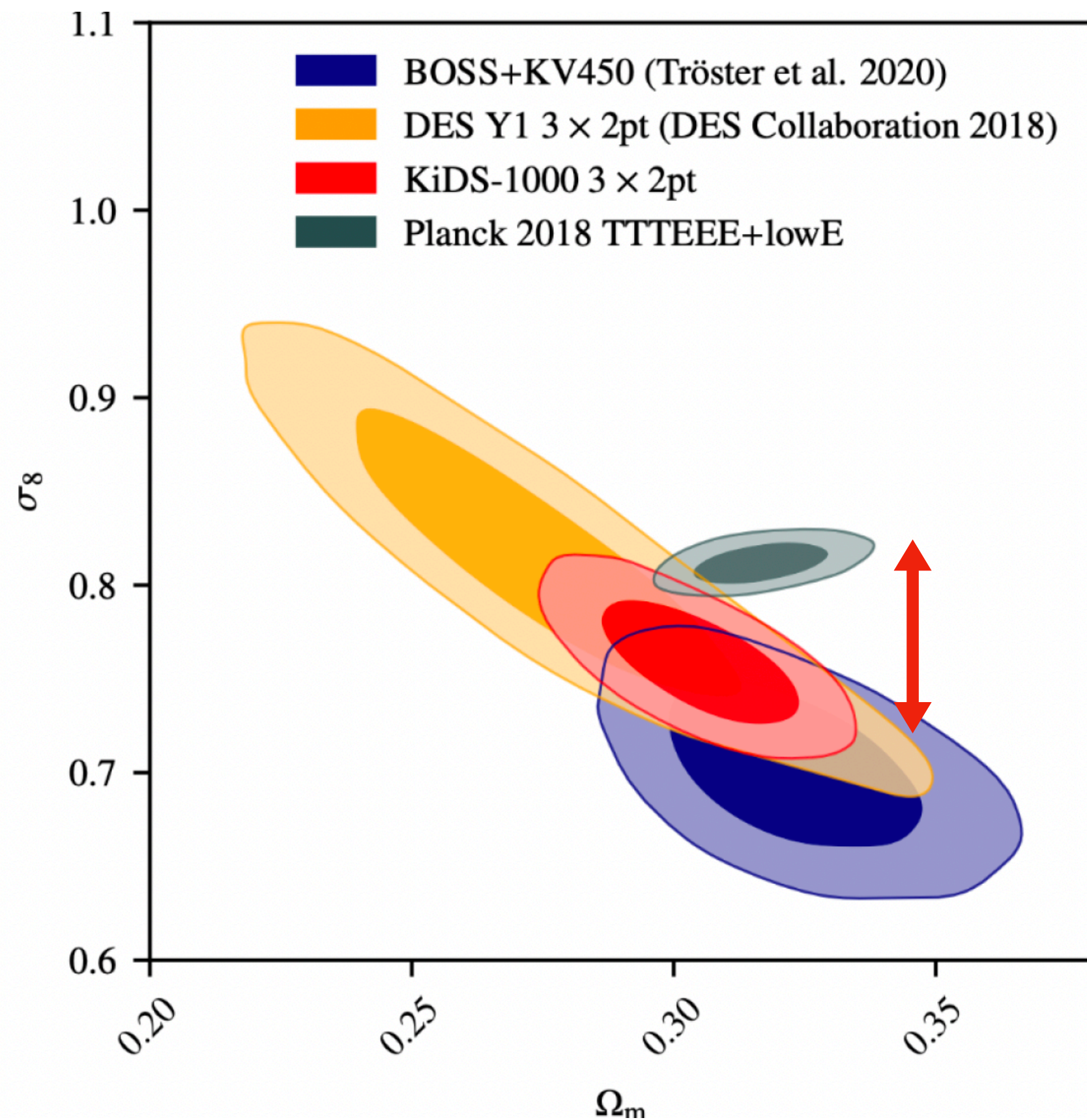
$$\sigma_8 = \int P_m(k, z=0) W_R^2(k) d \ln k$$



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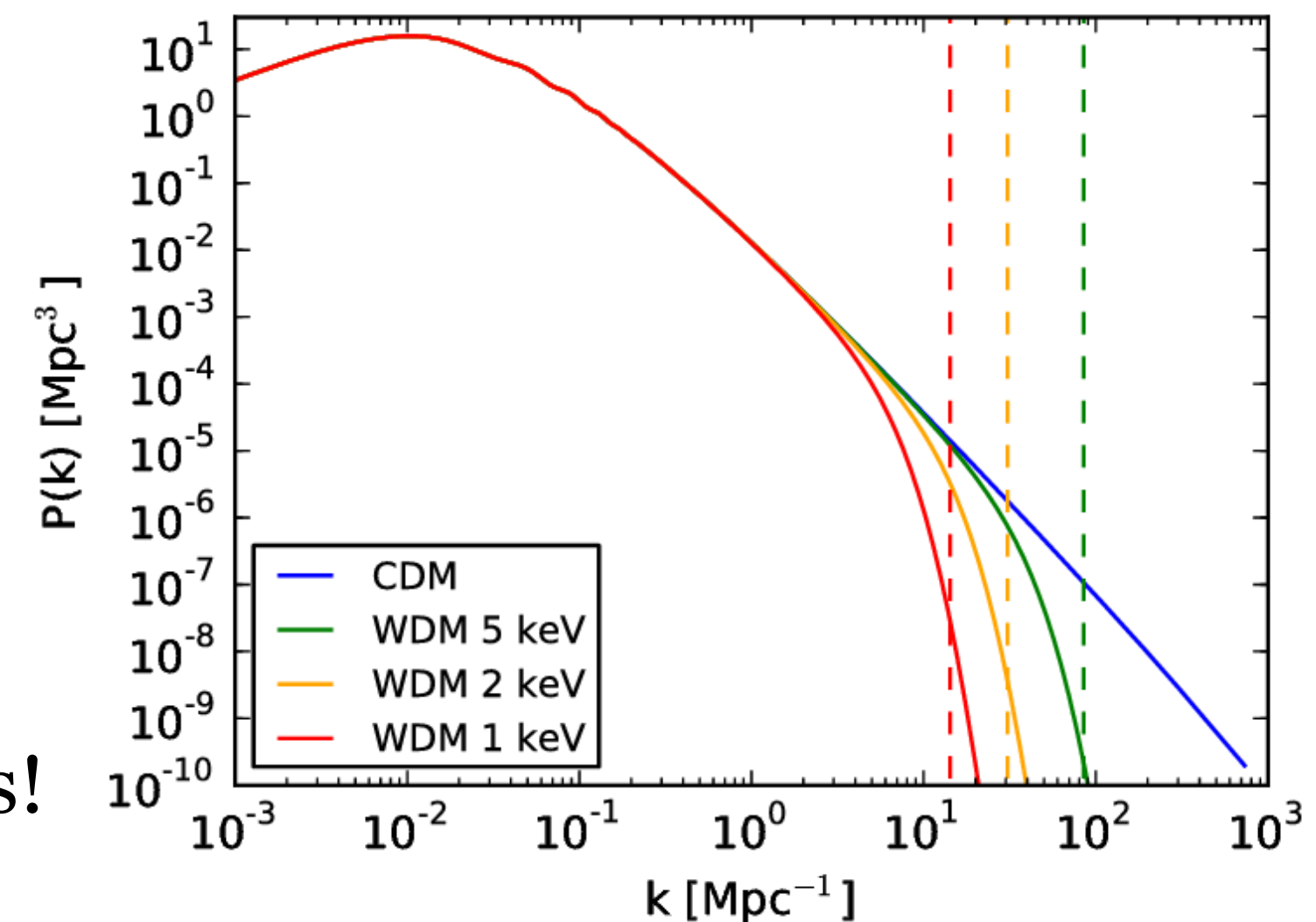
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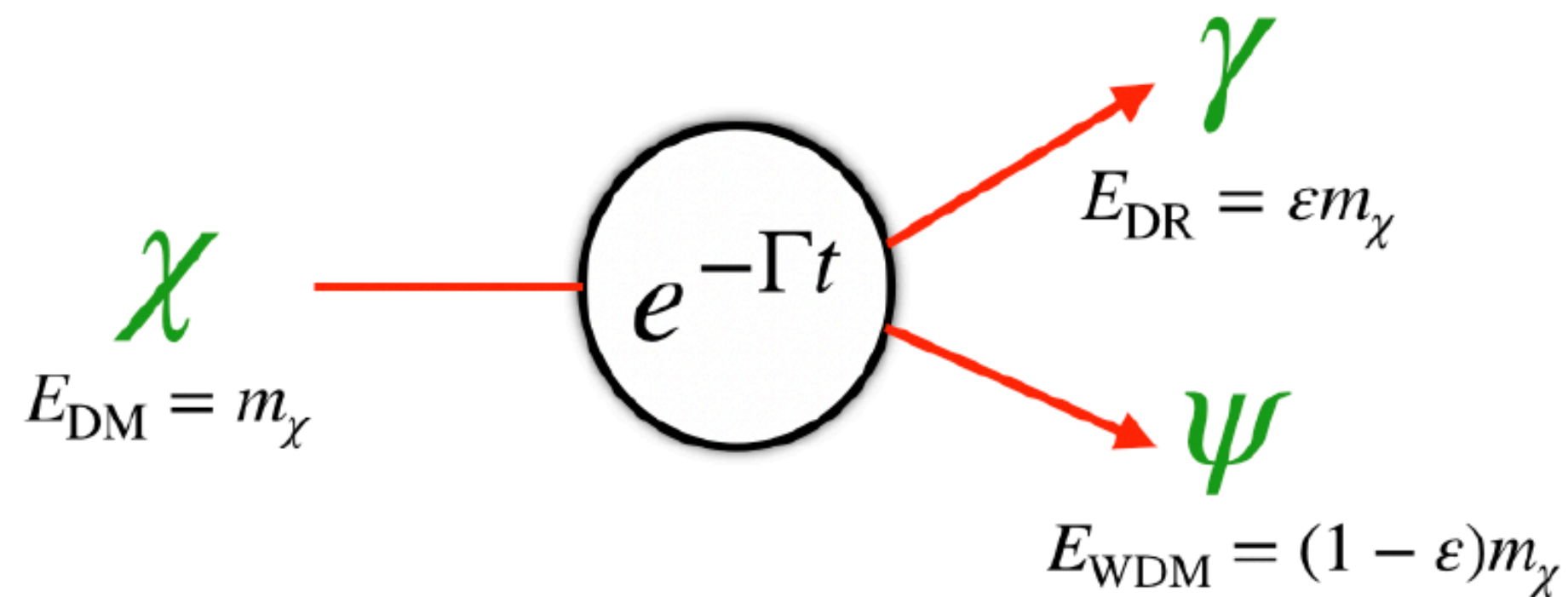
Need to **suppress power** at scales  $k \sim 0.1 - 1 \ h/\text{Mpc}$

**Ex:** Warm Dark Matter  
Very constrained by many probes!



# 2-body Dark Matter decay

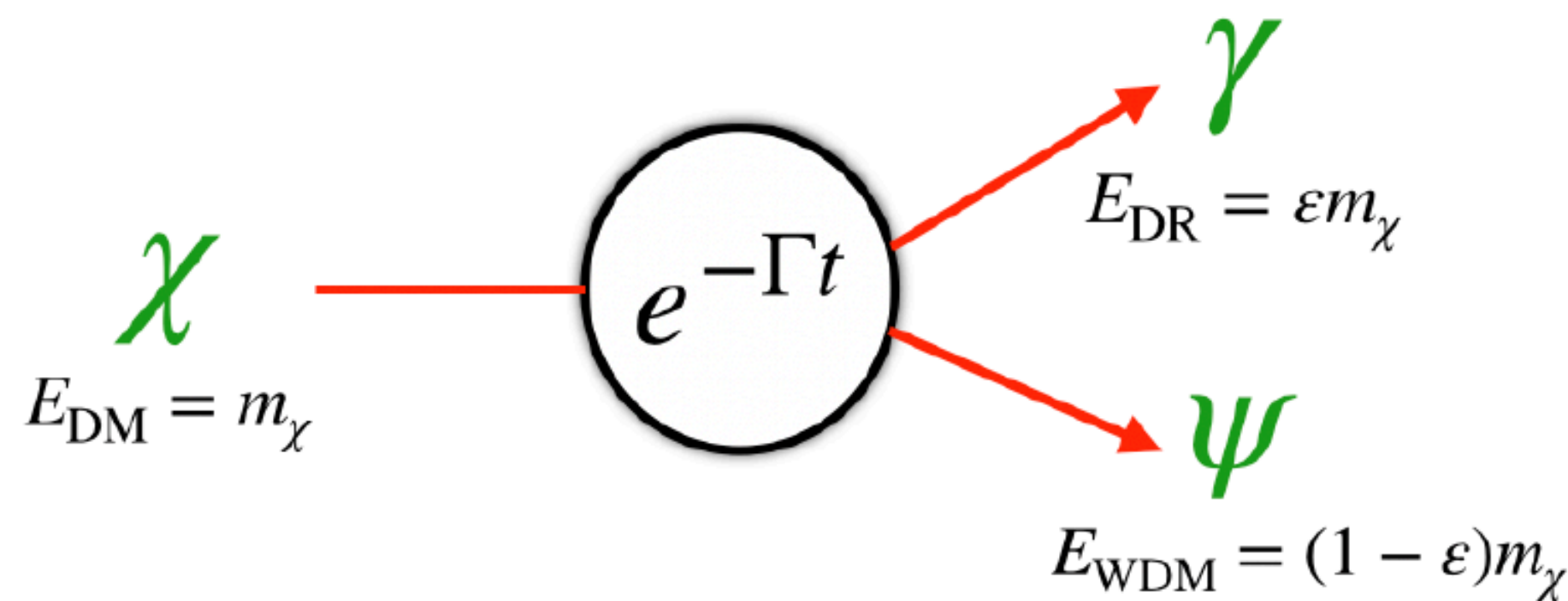
We explore DM decays to massless (**Dark Radiation**) and massive (**Warm Dark Matter**) particles,  $\chi(\text{DM}) \rightarrow \gamma(\text{DR}) + \psi(\text{WDM})$





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We explore DM decays to massless (**Dark Radiation**) and massive (**Warm Dark Matter**) particles,  $\chi(\text{DM}) \rightarrow \gamma(\text{DR}) + \psi(\text{WDM})$



The model is fully specified by:

$$\{\Gamma, \varepsilon\} \quad \text{where} \quad \varepsilon = \frac{1}{2} \left( 1 - \frac{\mathbf{m}_\psi^2}{\mathbf{m}_\chi^2} \right) \begin{cases} = \mathbf{0} & \text{for } \Lambda\text{CDM} \\ = \mathbf{1/2} & \text{for } \text{DM} \rightarrow \text{DR} \end{cases}$$

# 2-body Dark Matter decay

Aoyama++ 1402.2972	→	Full treatment of perts.	No parameter scan
Vattis++ 1903.06220	→	Resolution to $H_0$ tension ?	No perturbations
Haridasu&Viel 2004.07709	→	SNIa+BAO rule out solution	
Clark++ 2006.03678	→	CMB rule out solution	

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**Our goal:** Perform parameter scan by including full treatment of linear perts, in order to assess the impact on the  $S_8$  tension

→ Track  $\delta_i$ ,  $\theta_i$  and  $\sigma_i$  for  $i = \text{dm, dr, wdm}$

# Evolution of perturbations: fluid equations

New fluid eqs.\*, based on previous approximation for massive neutrinos

Lesgourgues & Tram, 1104.2935

$$\dot{\delta}_{\text{wdm}} = -3aH(c_{\text{syn}}^2 - w)\delta_{\text{wdm}} - (1 + w)\left(\theta_{\text{wdm}} + \frac{\dot{h}}{2}\right) + a\Gamma(1 - \varepsilon)\frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}}(\delta_{\text{dm}} - \delta_{\text{wdm}})$$

$$\dot{\theta}_{\text{wdm}} = -aH(1 - 3c_a^2)\theta_{\text{wdm}} + \frac{c_{\text{syn}}^2}{1 + w}k^2\delta_{\text{wdm}} - k^2\sigma_{\text{wdm}} - a\Gamma(1 - \varepsilon)\frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}}\frac{1 + c_a^2}{1 + w}\theta_{\text{wdm}}$$

\*Implemented in modified version of public Boltzmann solver CLASS



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where

$$c_a^2(\tau) = w\left(5 - \frac{\mathfrak{p}_{\text{wdm}}}{\bar{P}_{\text{wdm}}} - \frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}}\frac{\Gamma}{3wH}\frac{\varepsilon^2}{1 - \varepsilon}\right)\left[3(1 + w) - \frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}}\frac{\Gamma}{H}(1 - \varepsilon)\right]^{-1}$$

and

$$c_{\text{syn}}^2(k, \tau) = c_a^2(\tau)\left[1 + (1 - 2\varepsilon)T(k/k_{\text{fs}})\right]$$

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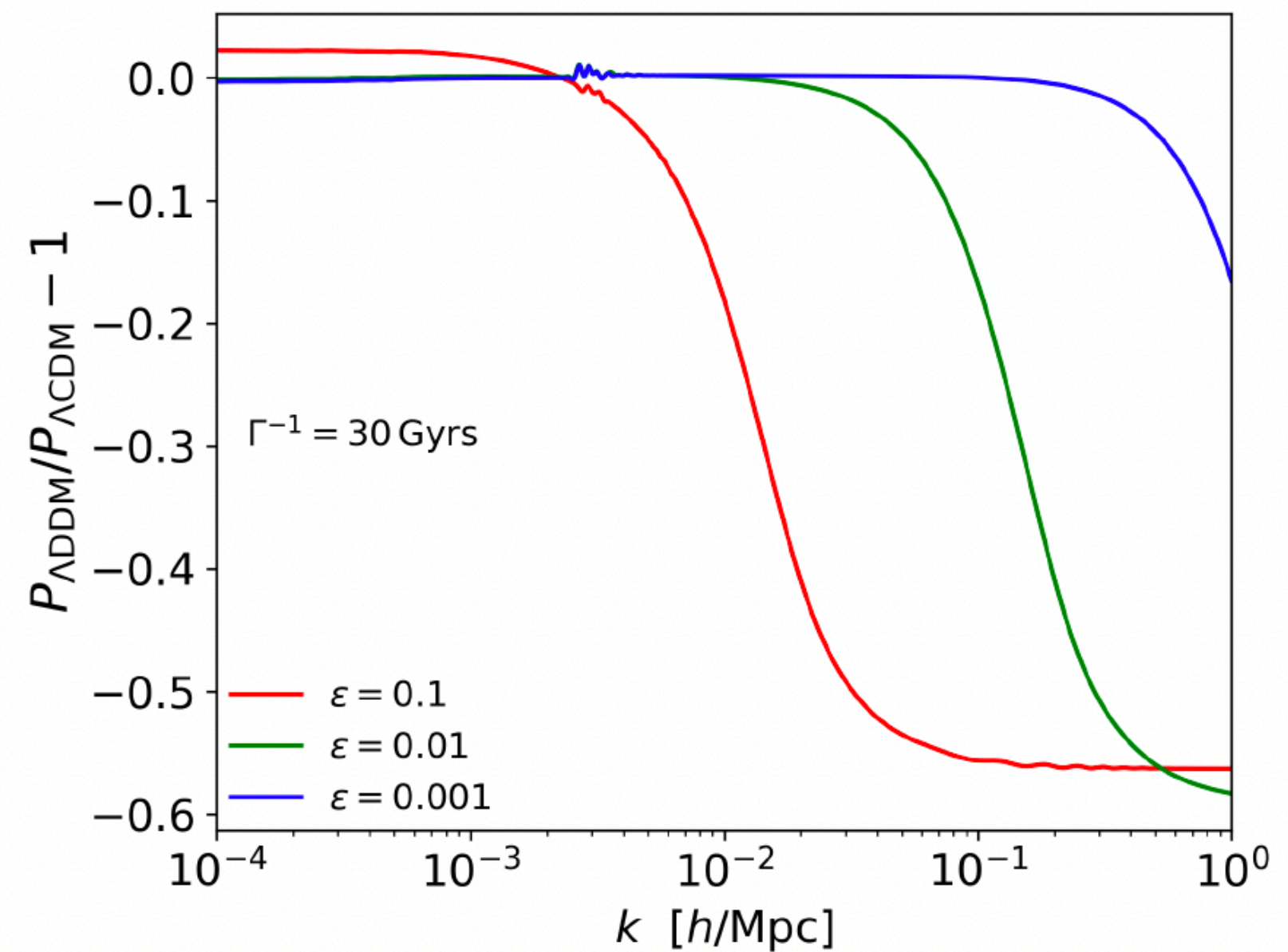
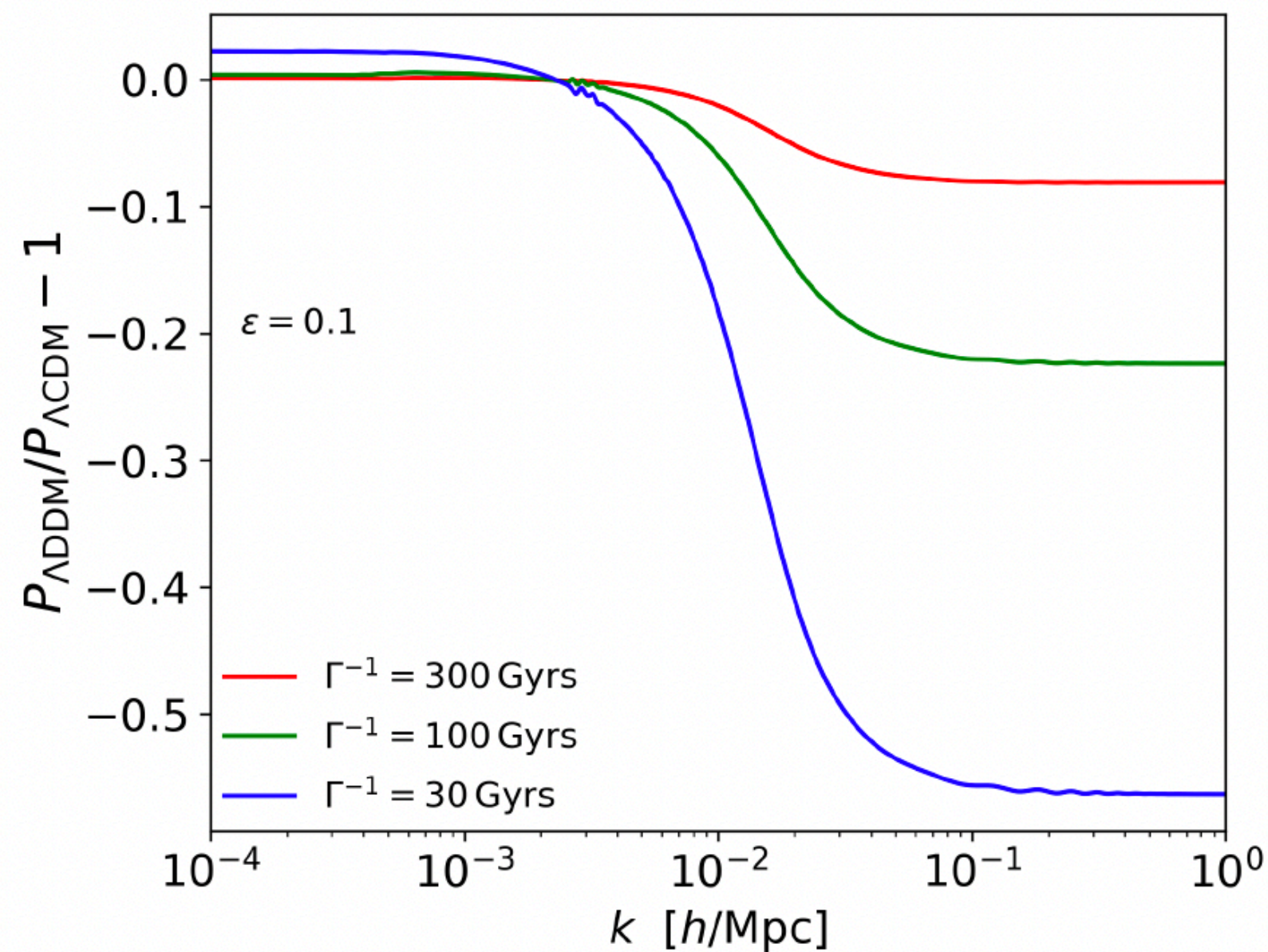
$$c_{\text{syn}}^2(k, \tau) = c_a^2(\tau)\left[1 + (1 - 2\varepsilon)T(k/k_{\text{fs}})\right]$$

***CPU time reduced from  $\sim 1$  day to  $\sim 1$  minute!***

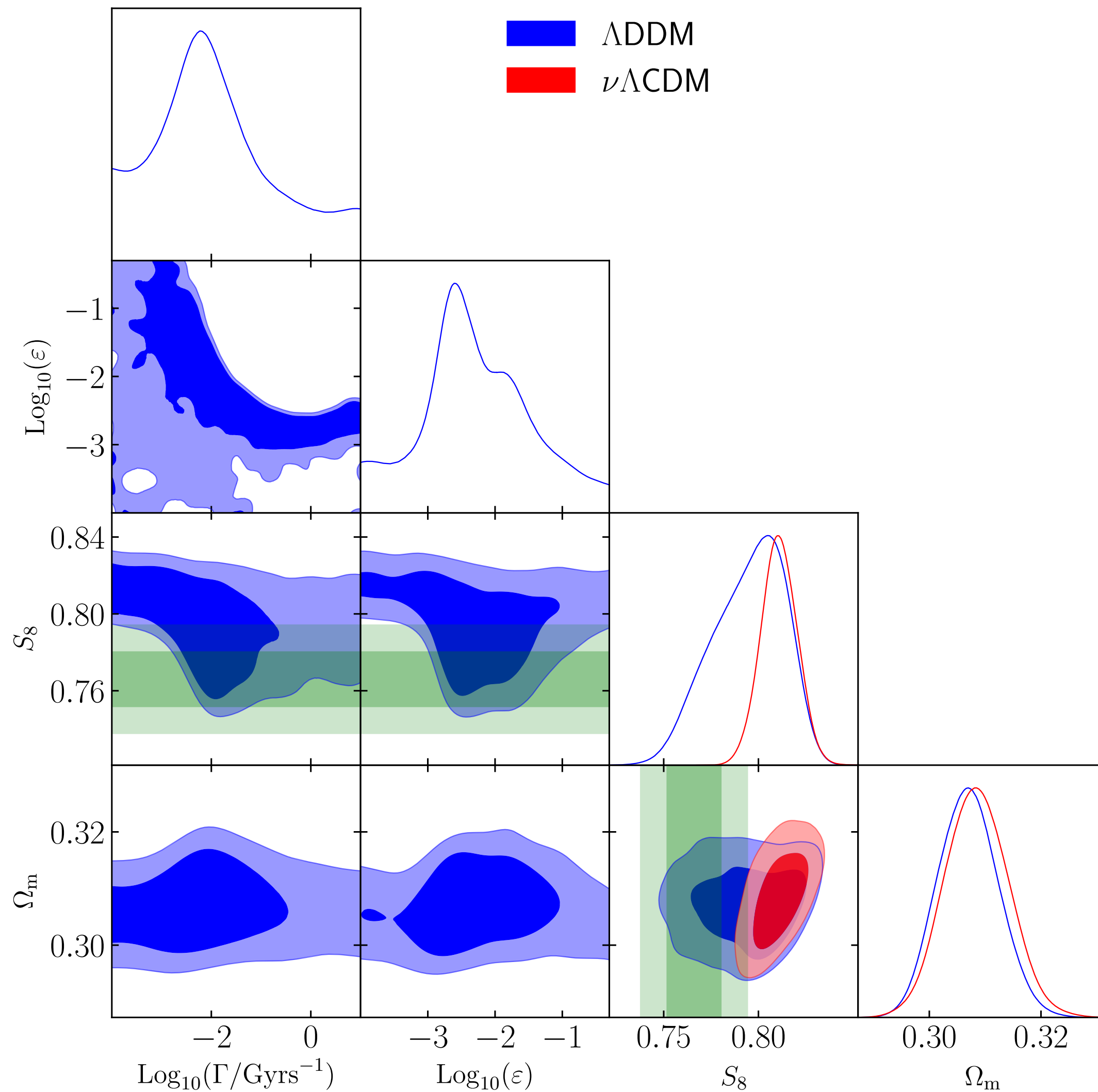
\*Implemented in modified version of public Boltzmann solver CLASS

# Impact of decaying DM on the matter spectrum

The WDM daughter leads to a power suppression in  $P_m(k)$  at small scales  $k > k_{\text{fs}}$ , where  $k_{\text{fs}} \sim aH/c_a$



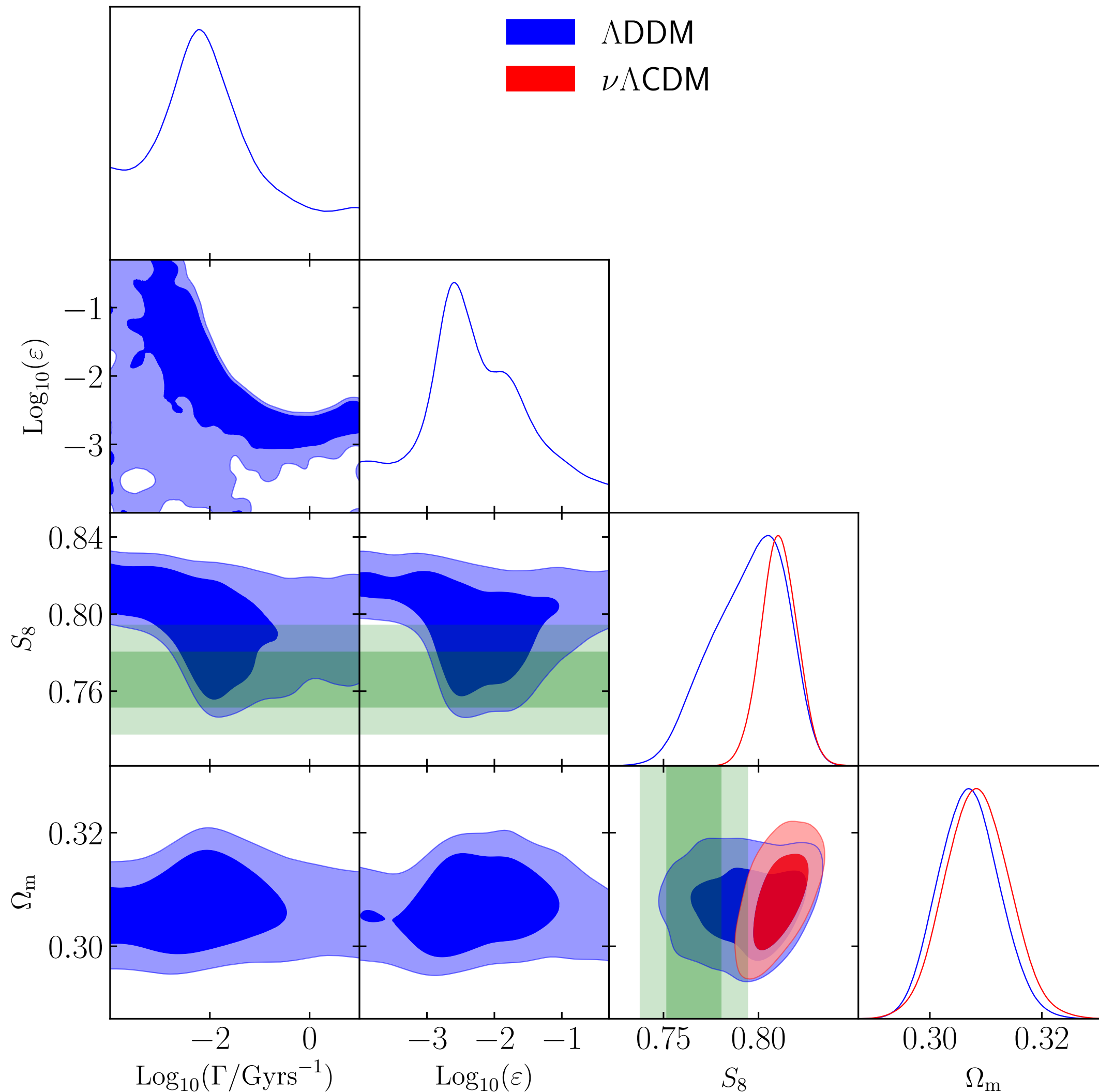
# Resolution to the $S_8$ tension



- MCMC analysis using Planck+BAO+SNIa+prior on  $S_8$  from KIDS+BOSS+2dfLenS



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- MCMC analysis using Planck+BAO+SNIa+prior on  $S_8$  from KIDS+BOSS+2dfLenS
- Reconstructed  $S_8$  values are in excellent agreement with WL data!

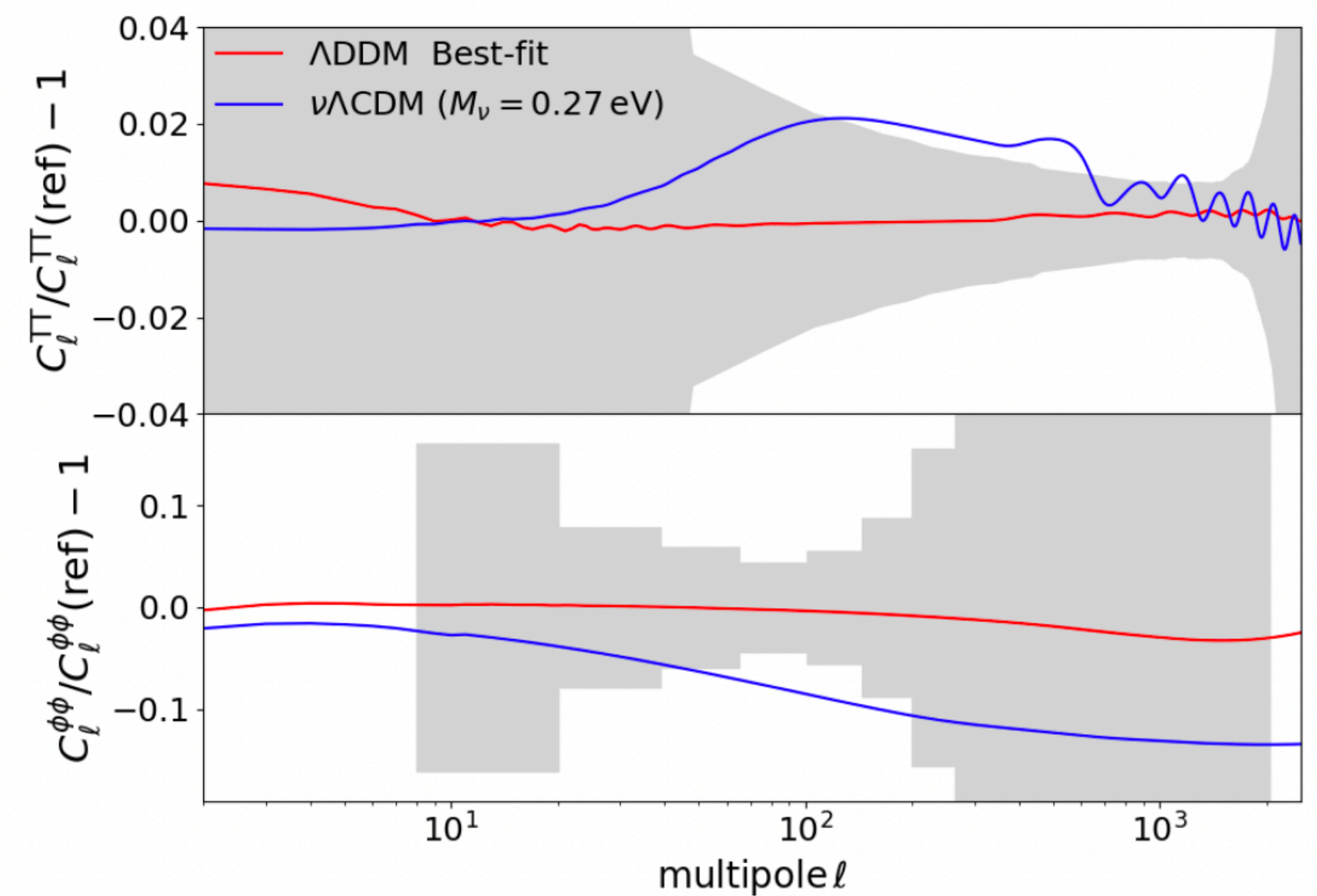
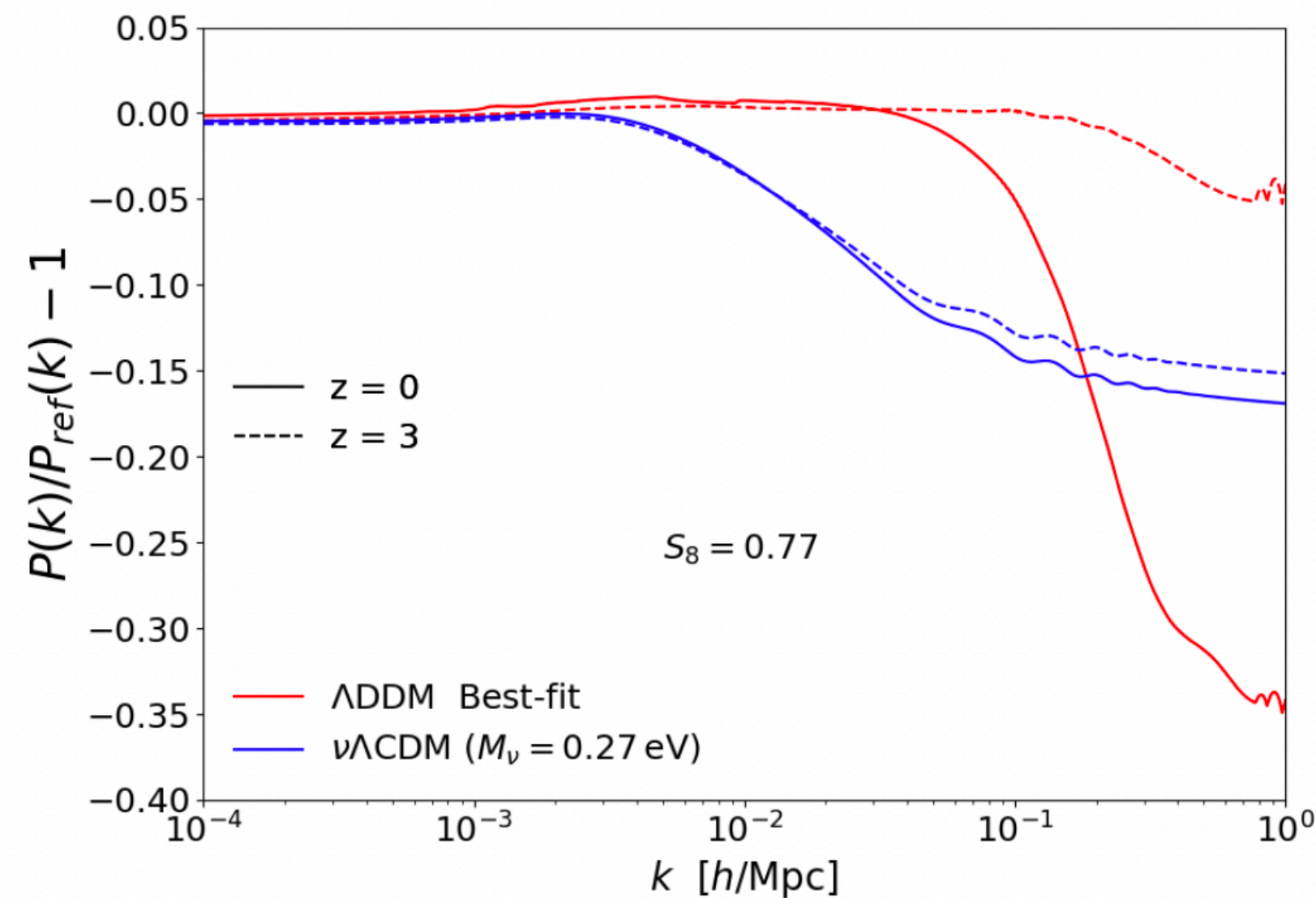
	$\nu\Lambda$ CDM	$\Lambda$ CDM
$\chi^2_{\text{CMB}}$	1015.9	1015.2
$\chi^2_{S_8}$	5.64	0.002

$$\longrightarrow \Delta\chi^2_{\min} \simeq -5.5$$

$$\Gamma^{-1} \simeq 55 (\epsilon/0.007)^{1.4} \text{ Gyr}$$

# Why does the 2-body DM decay work better than massive neutrinos?

The 2-body decay gives a better fit thanks to the **time-dependence of the power suppression** and the cut-off scale



# Interesting implications

- **Model building:** Why  $\varepsilon \ll 1/2$ , i.e.  $m_{\text{wdm}} \sim m_{\text{dm}}$  ?  
Ex : Supergravity [Choi&Yanagida 2104.02958](#)

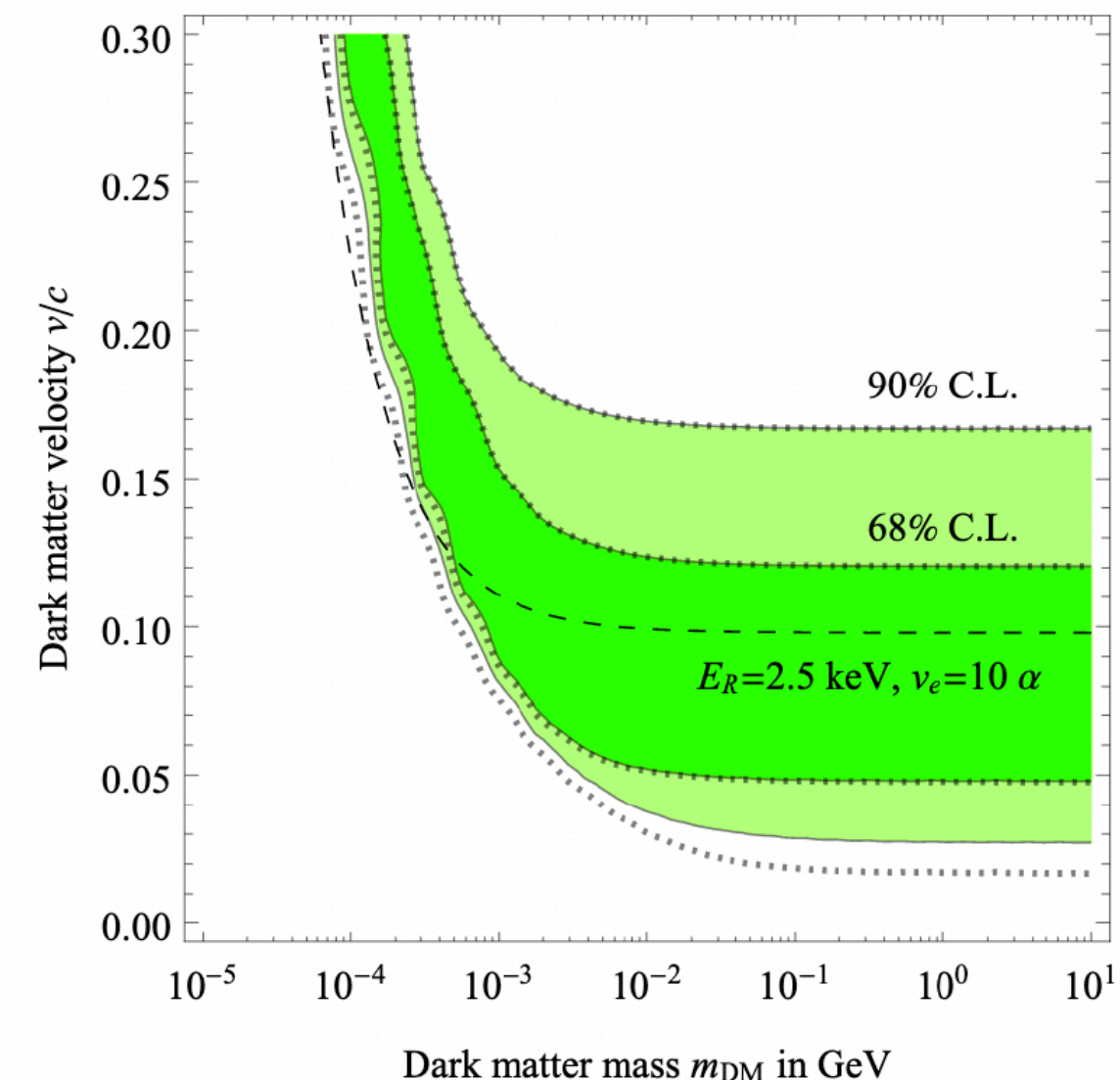
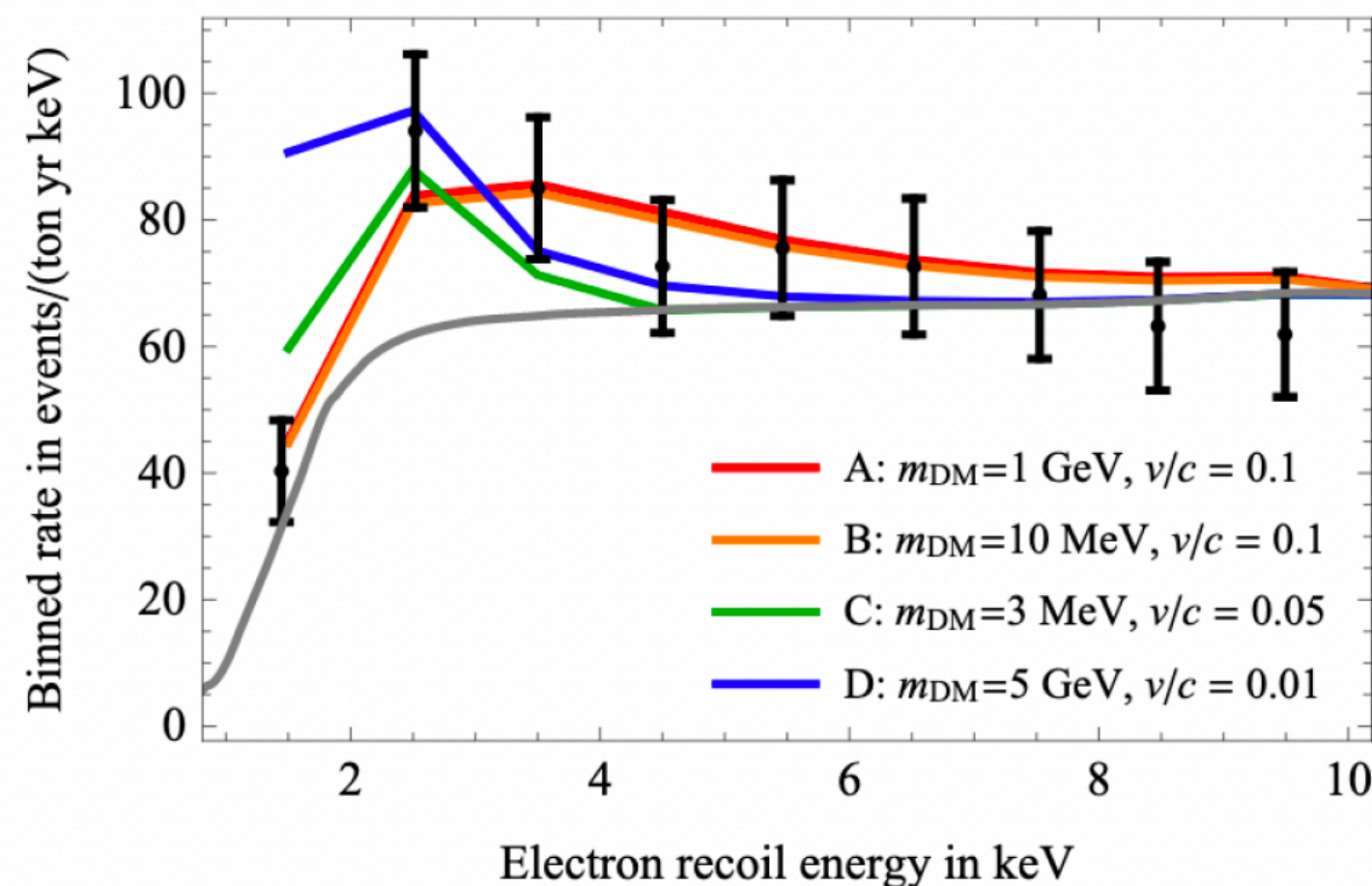
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- **Small-scale crisis of  $\Lambda$ CDM:** Reduction in the abundance of subhalos and their concentrations [Wang++ 1406.0527](#)
- **Xenon-1T excess:** It could be explained by a fast DM component, such as the WDM, with  $v/c \simeq \varepsilon$  [Kannike++ 2006.10735](#)



# Conclusions

- $\Lambda$ CDM provides a remarkable fit to many observations, but there exists a  $4\text{-}5\sigma$   $H_0$  tension and a  $2\text{-}3\sigma$   $S_8$  tension. These tensions offer an interesting window to the yet unknown dark sector.

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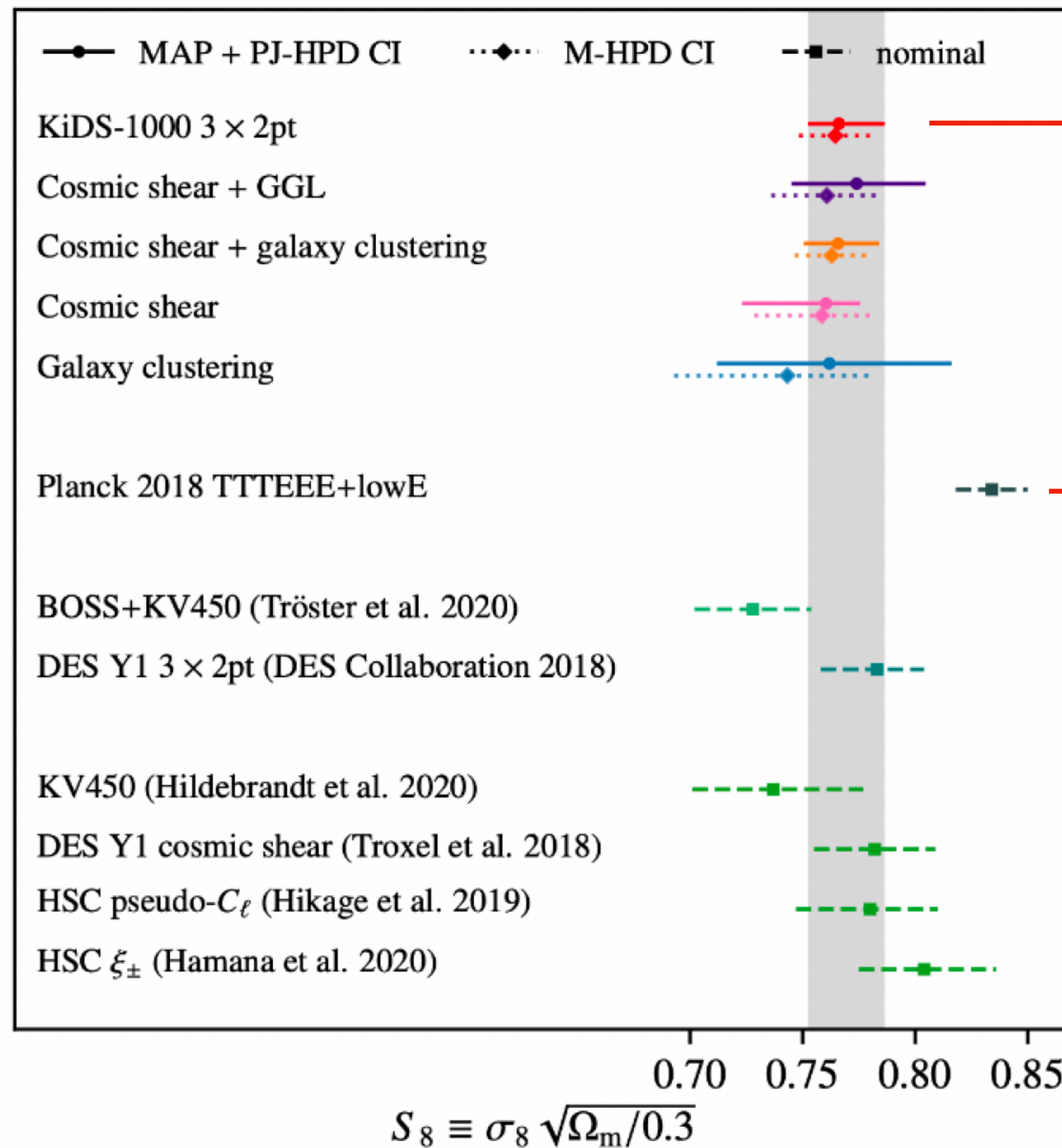
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- The  $S_8$  anomaly can be explained by a 2-body Decaying Dark Matter (DDM), which has many interesting implications for model building, the Xenon-1T excess, etc.

**We might be on the verge of the discovery of a rich dark sector!**

# **BACK-UP SLIDES**

# The $S_8$ tension



$$S_8 = 0.766^{+0.020}_{-0.014}$$

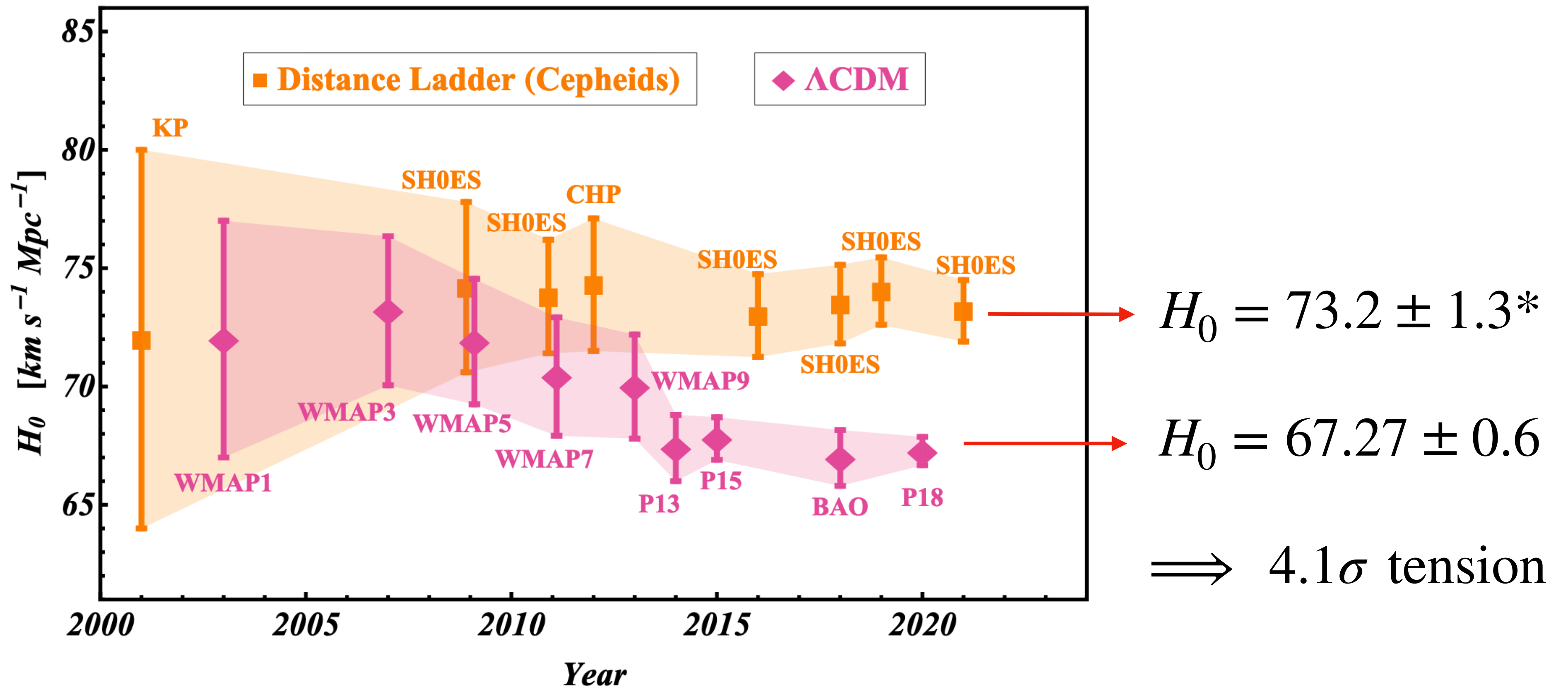
$$S_8 = 0.830 \pm 0.013$$

$\Rightarrow \sim 3\sigma$  tension



# The $H_0$ tension

Predominantly driven by the Planck and SHoES collaborations



[Perivolaropoulos&Skara 2105.05208](#)

\*Units of km/s/Mpc are always assumed

# $H_0$ Olympics: testing against other datasets

**Role of Planck data:** We replaced Planck by WMAP+ACT and BBN+BAO

————→ No significant changes (*notable exceptions are EDE and NEDE*)

**Adding extra datasets:** We included data from Cosmic Chronometers, Redshift-Space-Distortions and BAO Ly- $\alpha$ .

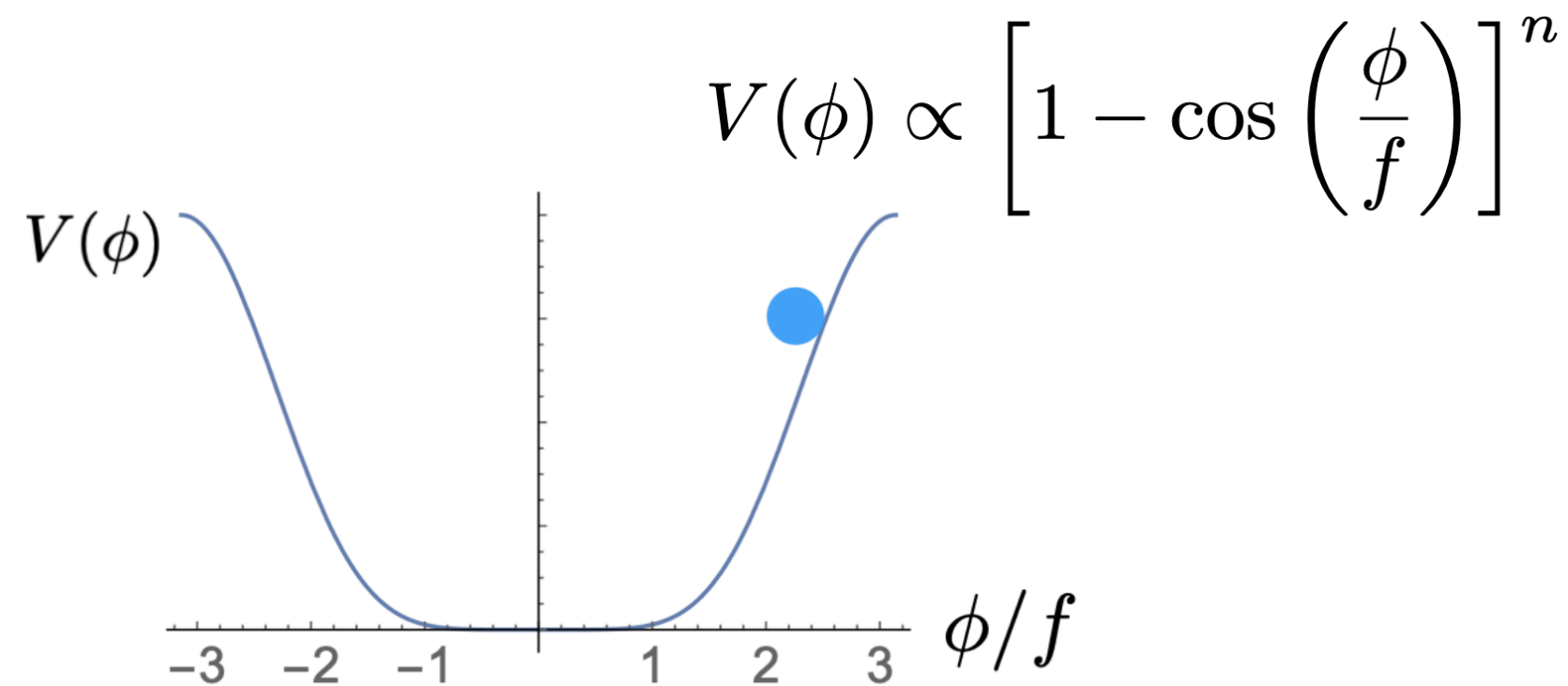
————→ No huge impact, but decreases performance of finalist models

# Early Dark Energy

Scalar field initially frozen, then dilutes away equal or faster than radiation

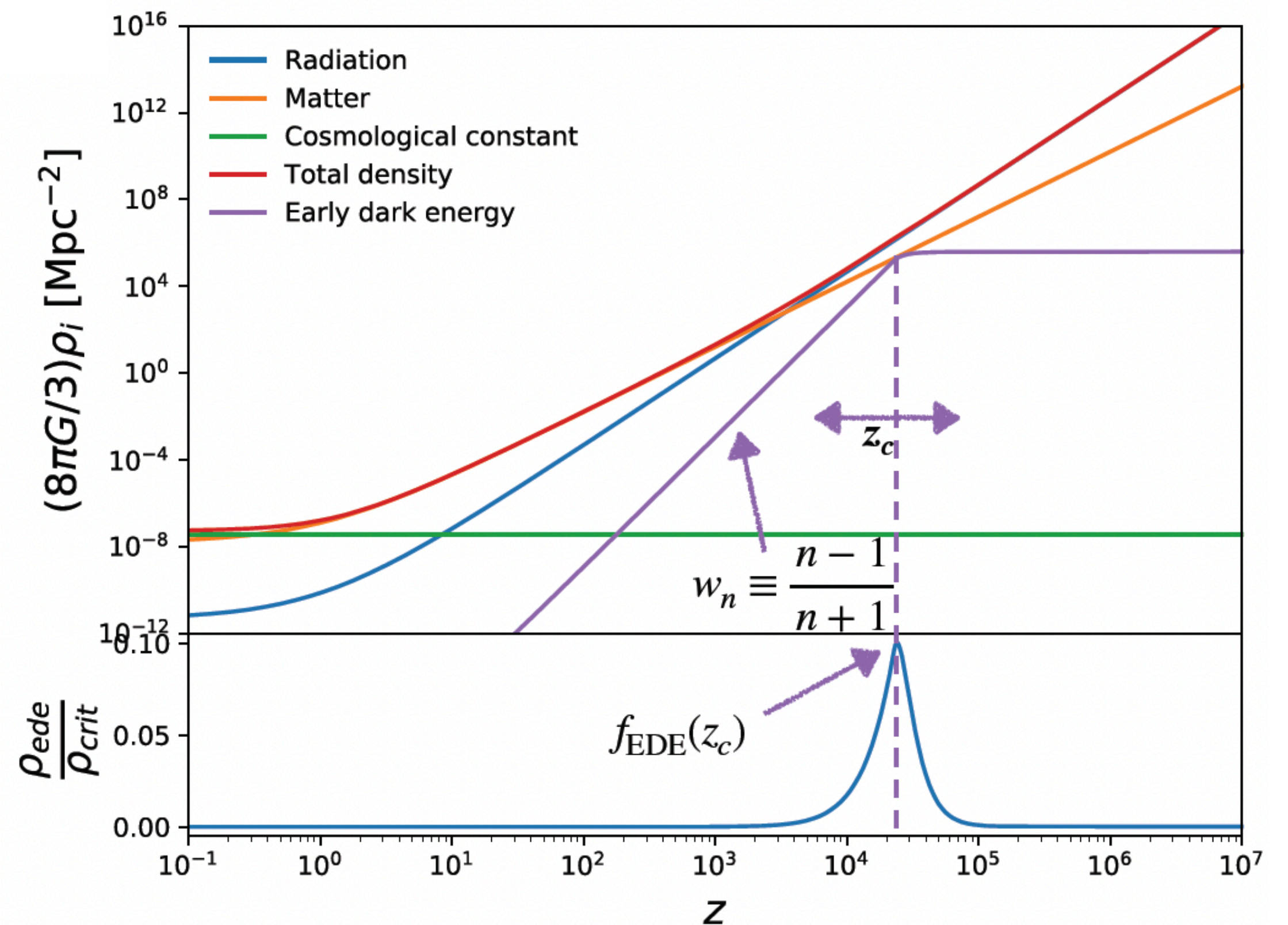
$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

+ perturbed linear eqs.



The model is fully specified by

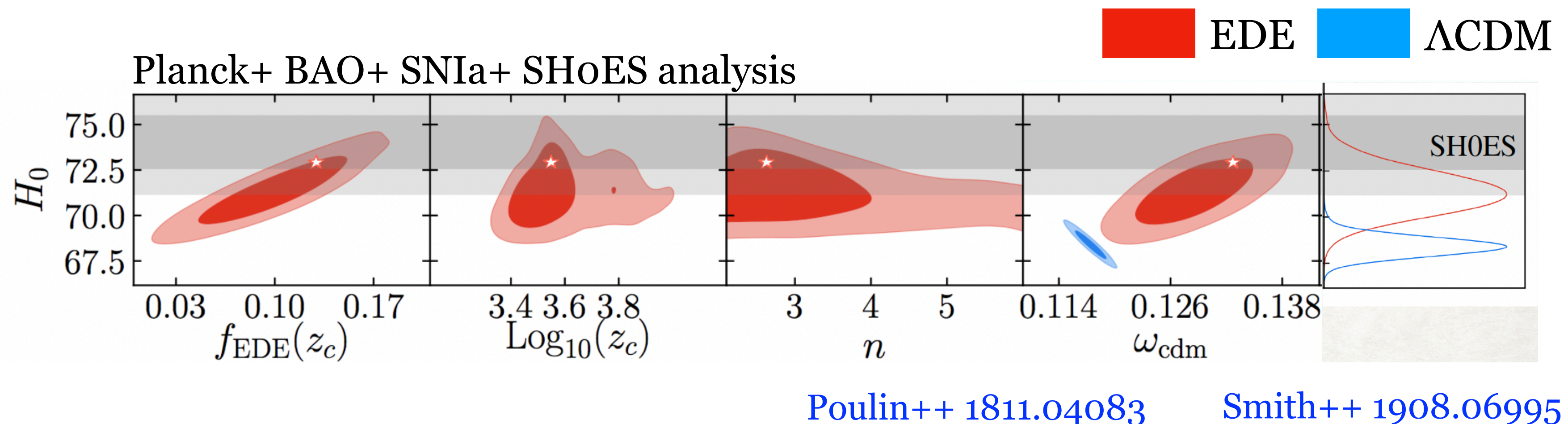
$$\{f_{\text{EDE}}(z_c), z_c, n, \phi_i\}$$





# Early Dark Energy

Early Dark Energy **can resolve the  $H_0$  tension** if  $f_{\text{EDE}}(z_c) \sim 10\%$  for  $z_c \sim z_{\text{eq}}$



Some caveats

## 1. *Very fine tuned?*

→ Proposed connexions of EDE with neutrino sector and present DE

Sakstein++ 1911.11760

Freese++ 2102.13655

## 2. Increased value of $\omega_{\text{cdm}} = \Omega_{\text{cdm}} h^2$ , **exacerbates $S_8$ tension**

Jedamzik++ 2010.04158.



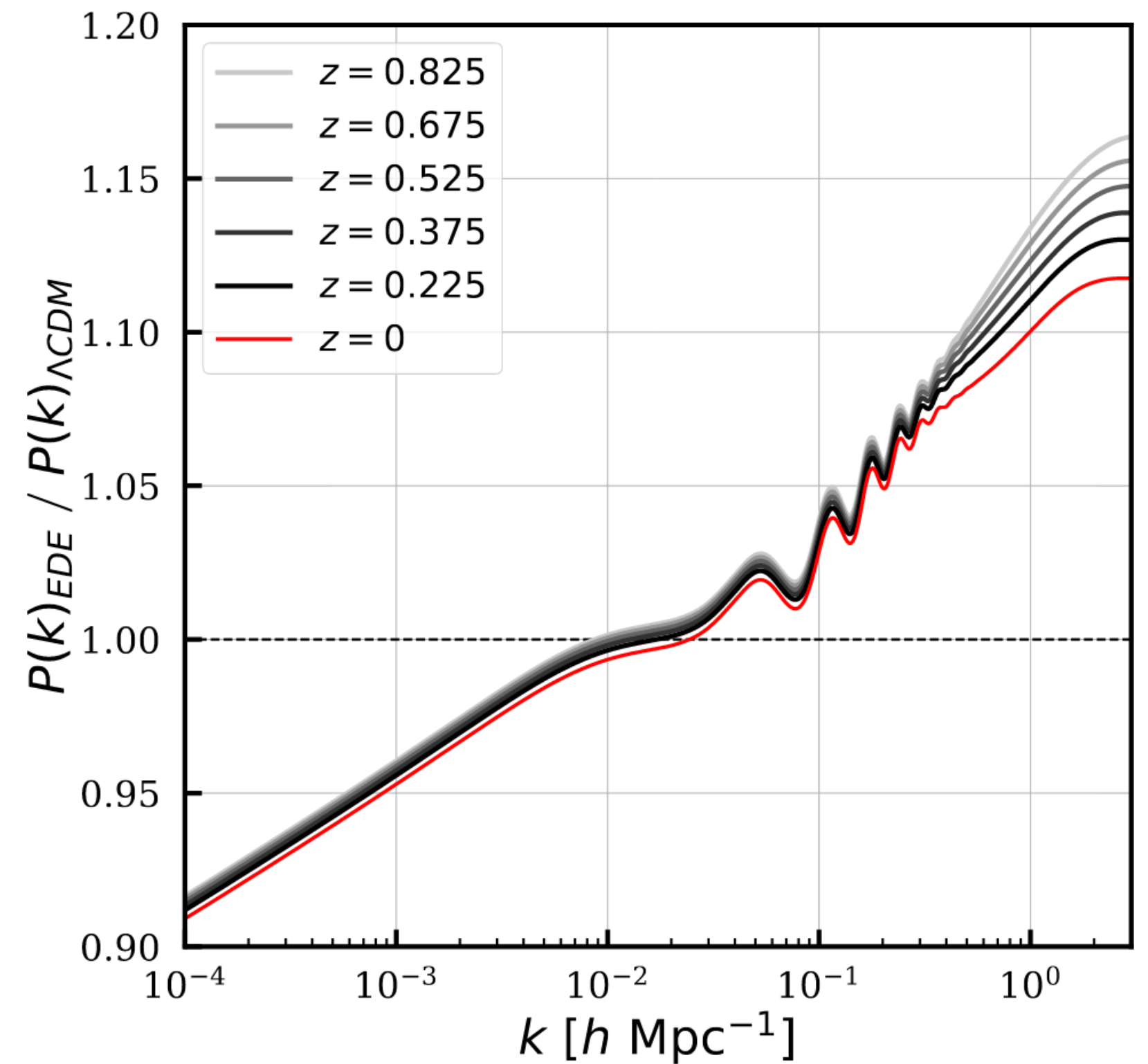
# Is EDE solution ruled out?

EDE solution **increases power at small  $k$**  (*with a corresponding increase in  $S_8$* ), rising mild tension with Large Scale Structure (LSS) data

When **LSS data** is added to analysis, EDE **detection is reduced** from  $3\sigma$  to  $2\sigma$

In addition, EDE is **not detected from Planck data alone**

D'amico++ 2006.12420  
Ivanov++ 2006.11235



Hill++ 2003.07355

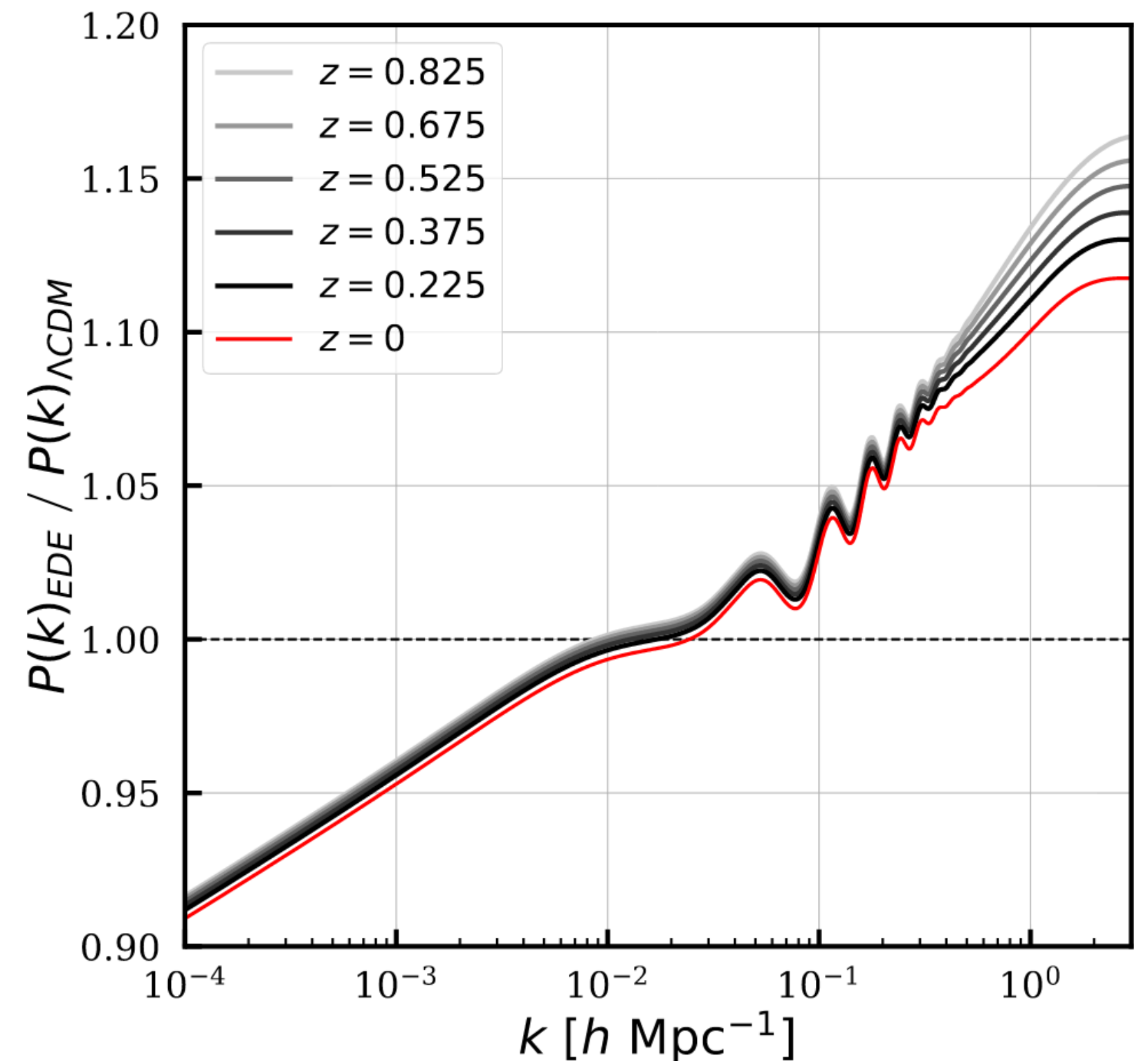
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# Answer: no, EDE solution is still robust

## 1. Why EDE is not detected from Planck alone?

---

Strong  $\chi^2$  degeneracy in Planck between  $\Lambda$ CDM and EDE :

Once  $f_{\text{EDE}} \rightarrow 0$ , parameters  $z_c$  and  $\phi_i$  become irrelevant, so posteriors are naturally weighted towards  $\Lambda$ CDM

To avoid this Bayesian volume effect, consider a

**1 parameter model (1pEDE)** : Fix  $z_c$  and  $\phi_i$  and let  $f_{\text{EDE}}$  free to vary

Within 1pEDE, we get a  $2\sigma$  detection of EDE from *Planck data alone*

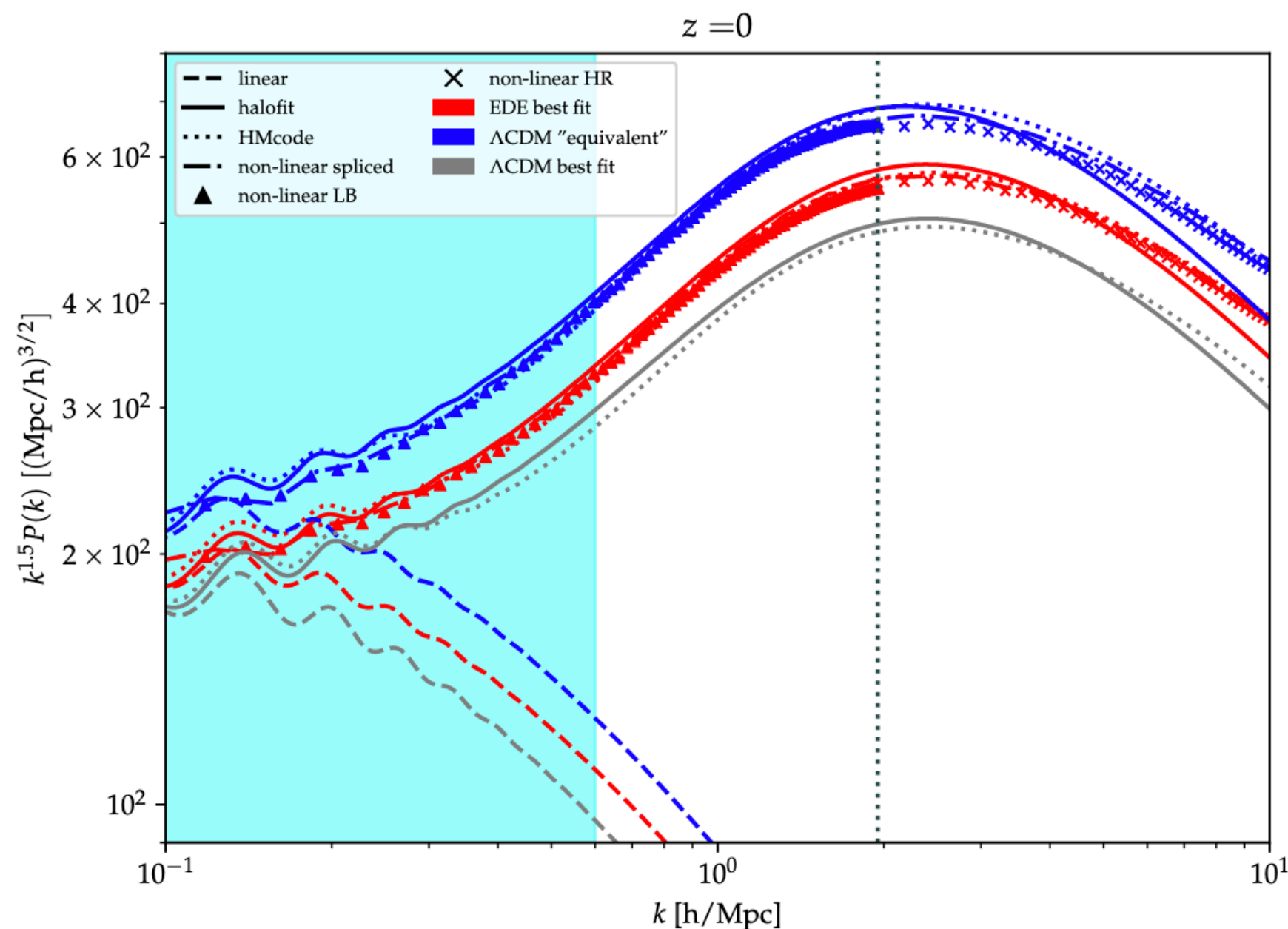
$$f_{\text{EDE}} = 0.08 \pm 0.04$$

$$H_0 = 70 \pm 1.5 \text{ km/s/Mpc}$$

Murgia, GFA, Poulin 2107.10291

# Answer: no, EDE solution is still robust

## 2. Is LSS data constraining enough to rule out EDE?



Important cross-check:

EDE **non-linear**  $P(k)$  from standard semi-analytical algorithms agrees well with results from N-body simulations

1pEDE tested against **Planck+BAO+SNIa+SHoEs** and WL data from **KiDS/Viking+DES**:  $S_8$  tension persists, but **fit is not significantly degraded wrt  $\Lambda$ CDM**, and solution to the  $H_0$  tension survives

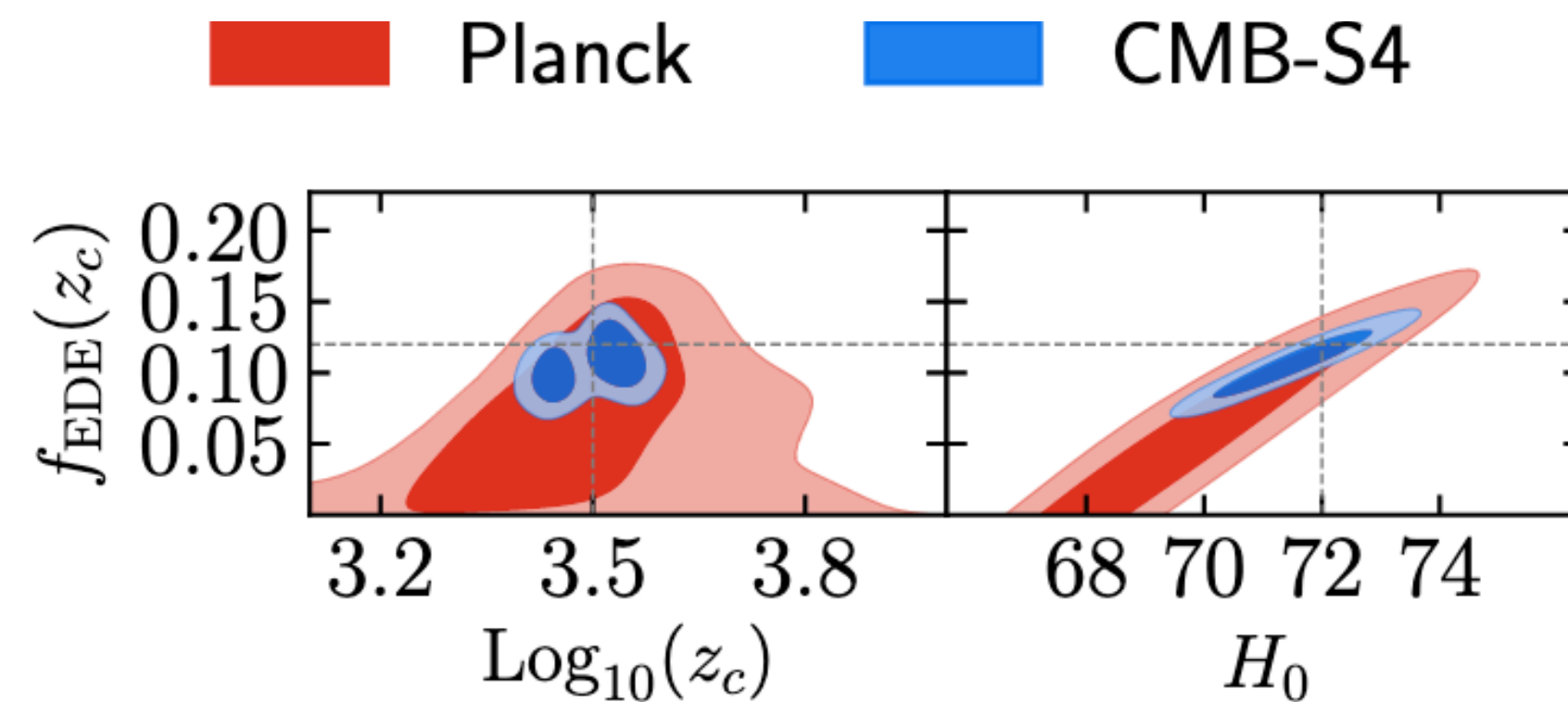
$$f_{\text{EDE}} = 0.09^{+0.03}_{-0.02}$$

$$H_0 = 71.3 \pm 0.9 \text{ km/s/Mpc}$$



# Prospects for Early Dark Energy

Future CMB experiments (i.e. CMB-S4) will be able to unambiguously detect EDE



Smith++ 1908.06995

Other current CMB experiments like ACT are already showing a  $3\sigma$  detection of EDE!

Hill++ 2109.04451

Poulin++ 2109.06229

# Decaying dark matter

- Dark matter (DM) is assumed to be perfectly **stable** in  $\Lambda$ CDM

*Can we test this hypothesis?*

- DM Decays to SM particles  $\longrightarrow$  **very constrained**

From **e . m . impact** on CMB :  $\Gamma^{-1} \gtrsim 10^8$  Gyr [Poulin++ 1610.10051](#)

- DM decays to **massless** Dark Radiation  $\longrightarrow$  **less constrained,**  
**but more model-independent**

From **grav . impact** on CMB :  $\Gamma^{-1} \gtrsim 10^2$  Gyr [Audren++ 1407.2418](#)  
[Poulin++ 1606.02073](#)

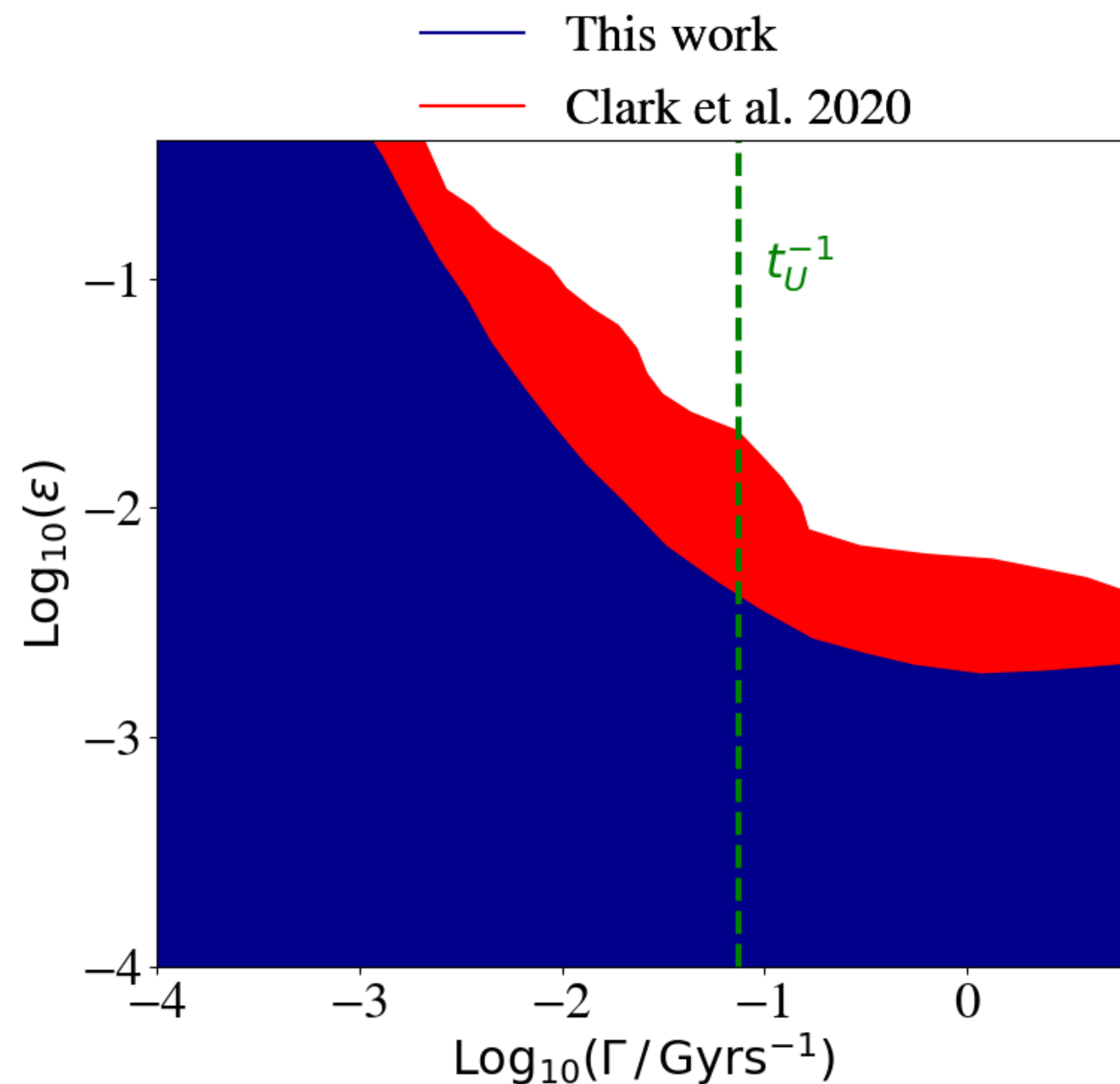
- What about massive products?

# Evolution of perturbations: full treatment

- Effects on  $P_m(k)$  and  $C_\ell$  ? Track **linear perts.** for the particles species involved in the decay:  $\delta_i$ ,  $\theta_i$  and  $\sigma_i$  for  $i = \text{dm, dr, wdm}$
- Boltzmann hierarchy of eqs. Dictate the evolution of the **p.s.d. multipoles**  $\Delta f_\ell(q, k, \tau)$ 
  - ◆ **DM and DR treatments are easy**, momentum d.o.f. are integrated out
  - ◆ **For WDM**, one needs to follow the evolution of the full p.s.d.  
Computationally expensive  $\longrightarrow \mathcal{O}(10^8)$  ODEs to solve!

# General constraints on the 2-body DM decay

Planck+BAO+SNIa analysis



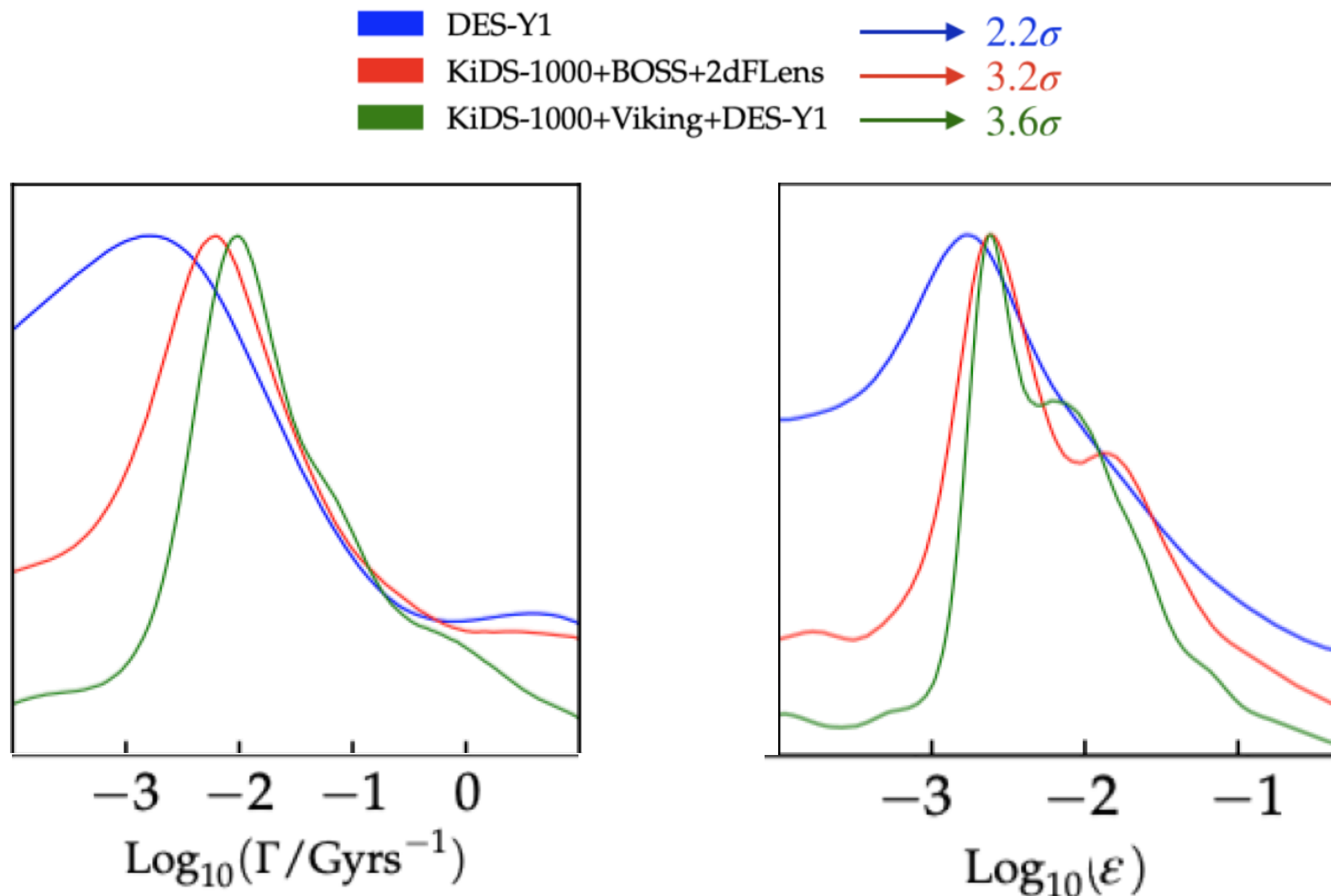
Strong **negative correlation** between  $\epsilon$  and  $\Gamma$

Constraints up to **1 order of magnitude stronger** than previous literature



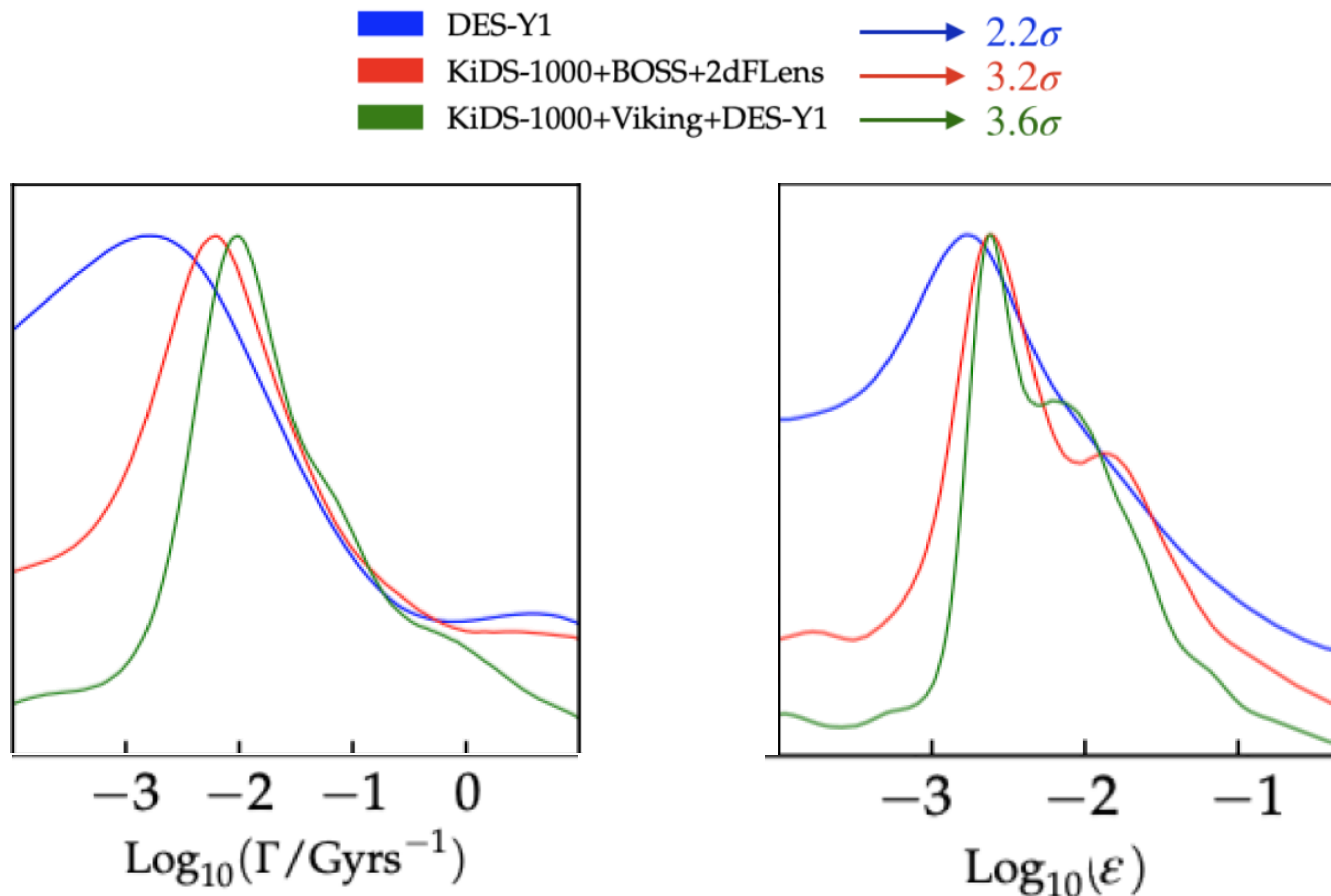
# Resolution to the $S_8$ tension

The level of detection depends on the level of tension with  $\Lambda$ CDM



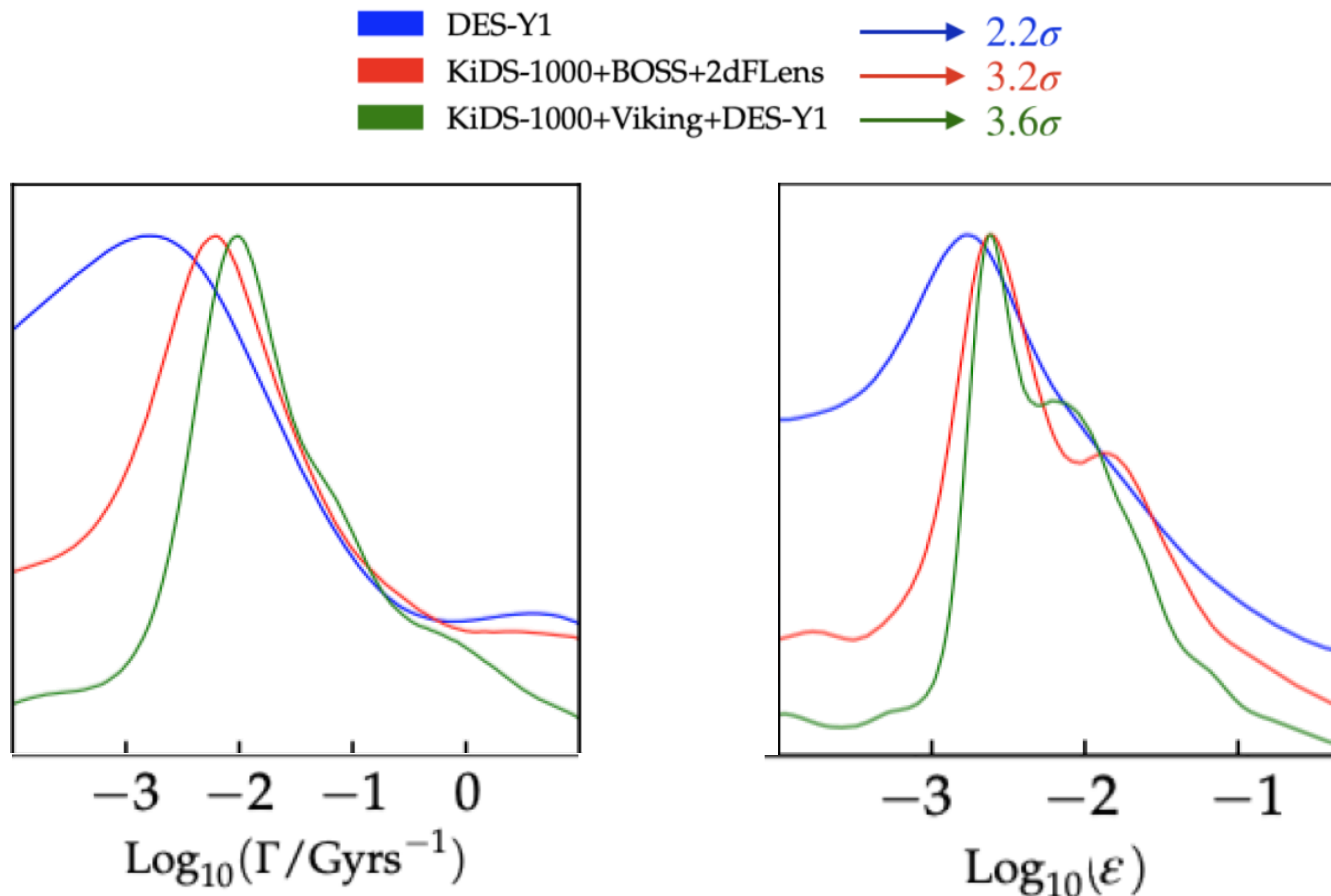
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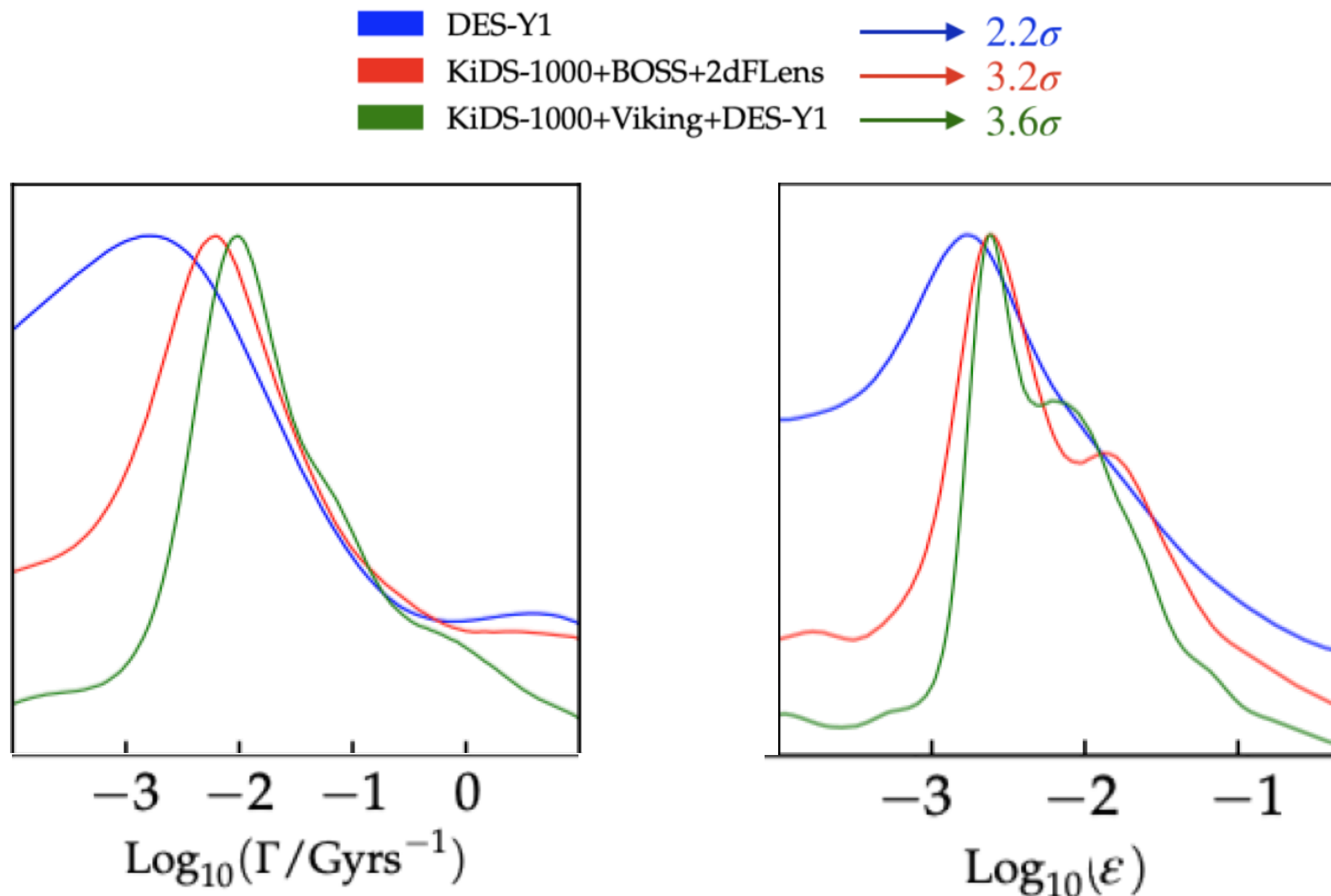
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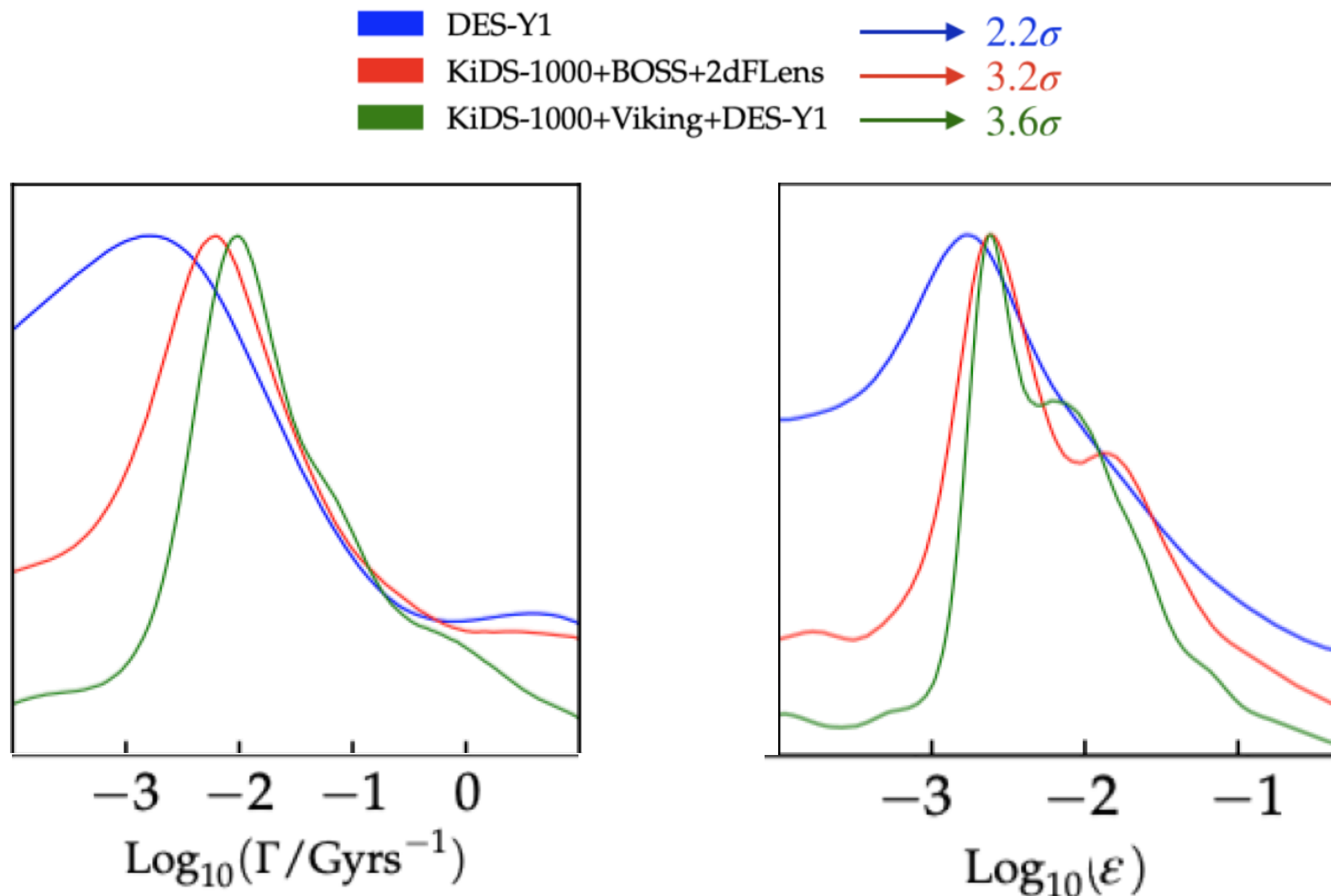
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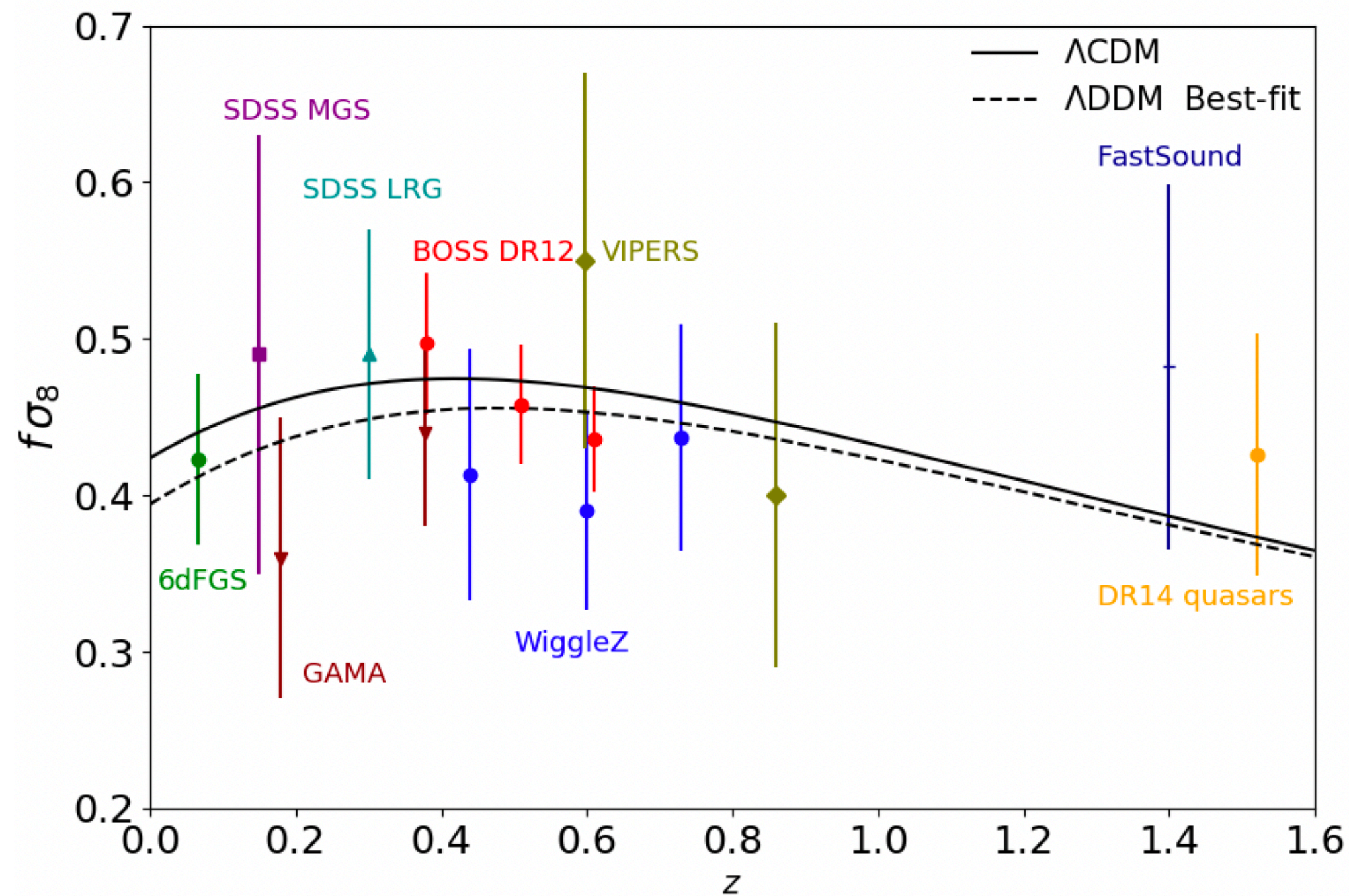


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# Prospects for the 2-body DM decay



Accurate measurements of  $f\sigma_8$  at  $0 \lesssim z \lesssim 1$  will further test the 2-body decay

**Next goal:** Predict non-linear matter power spectrum (using either N-body simulations or EFT of LSS)