

# Deep learning the invisible universe

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**GRAPPA**, University of Amsterdam

**21<sup>st</sup> May 2025**

**CEICO Cosmology Seminar**

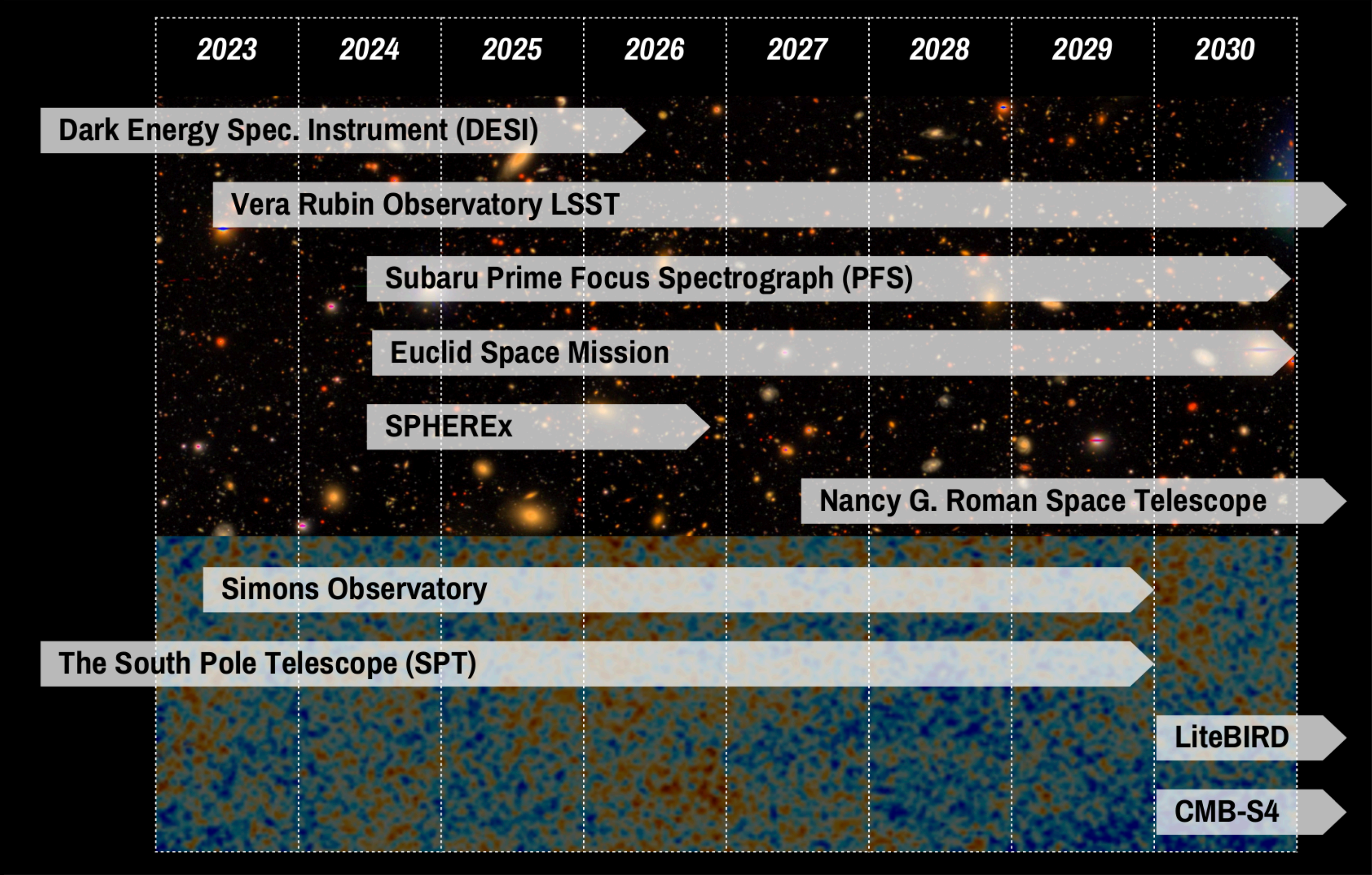
**GRAPPA** x x x



GRavitation AstroParticle Physics Amsterdam



# We are entering in the era of **ultra-high precision** cosmology



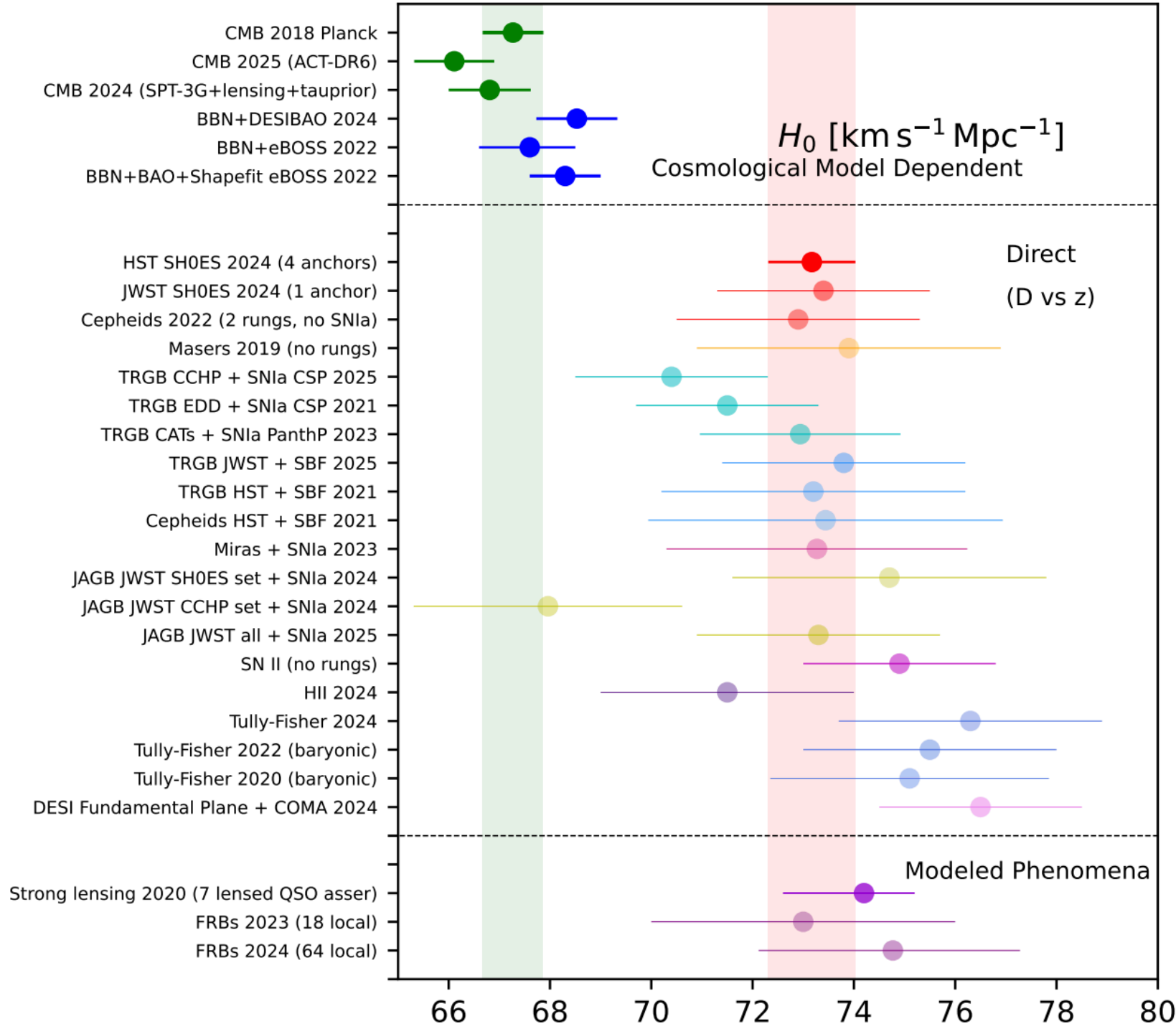
[Credit A. Bayer]



Various datasets point at **cracks in the  $\Lambda$ CDM model**

# Various datasets point at cracks in the $\Lambda$ CDM model

## $H_0$ tension

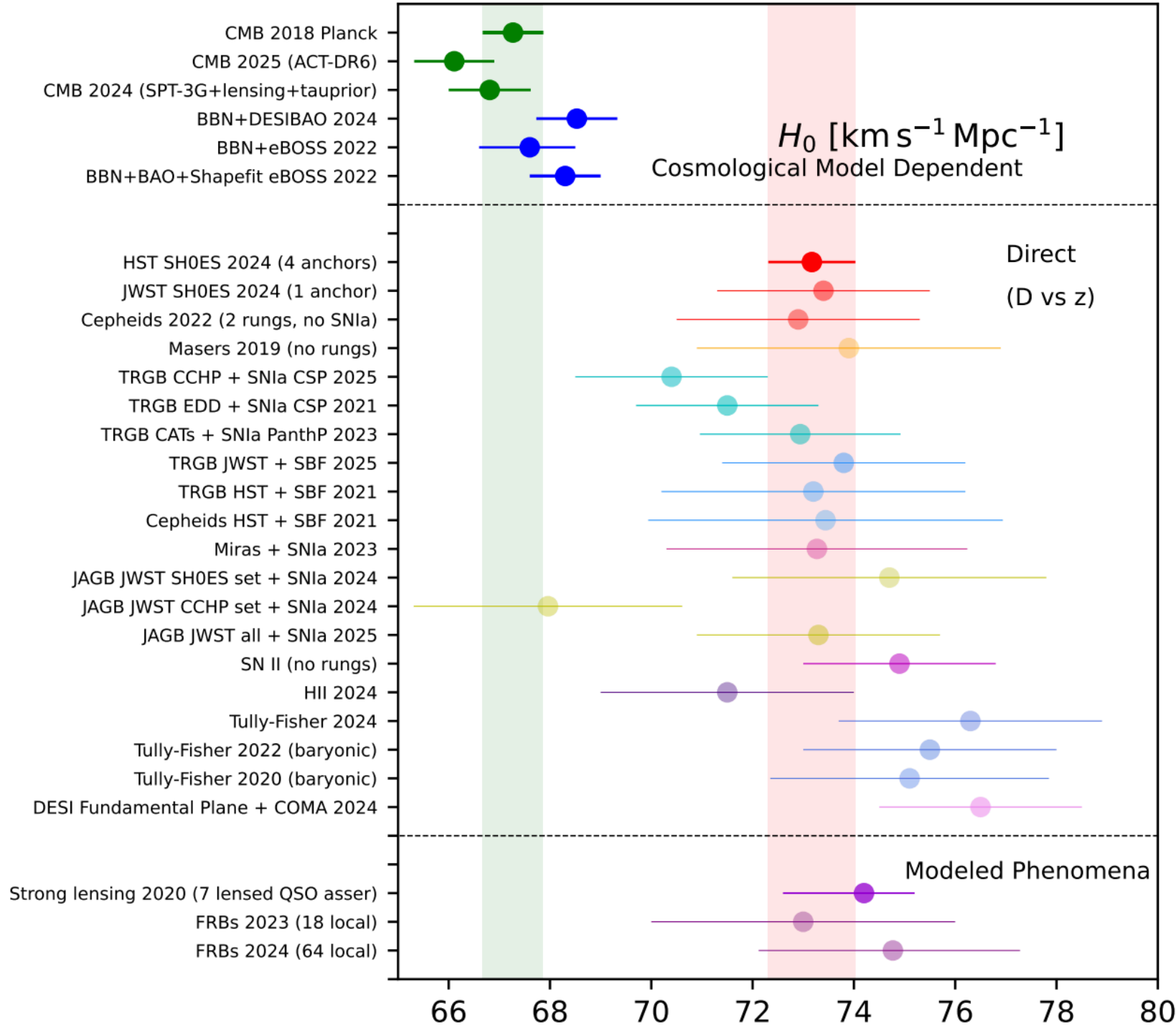


[CosmoVerse White  
Paper: 2504.01669]

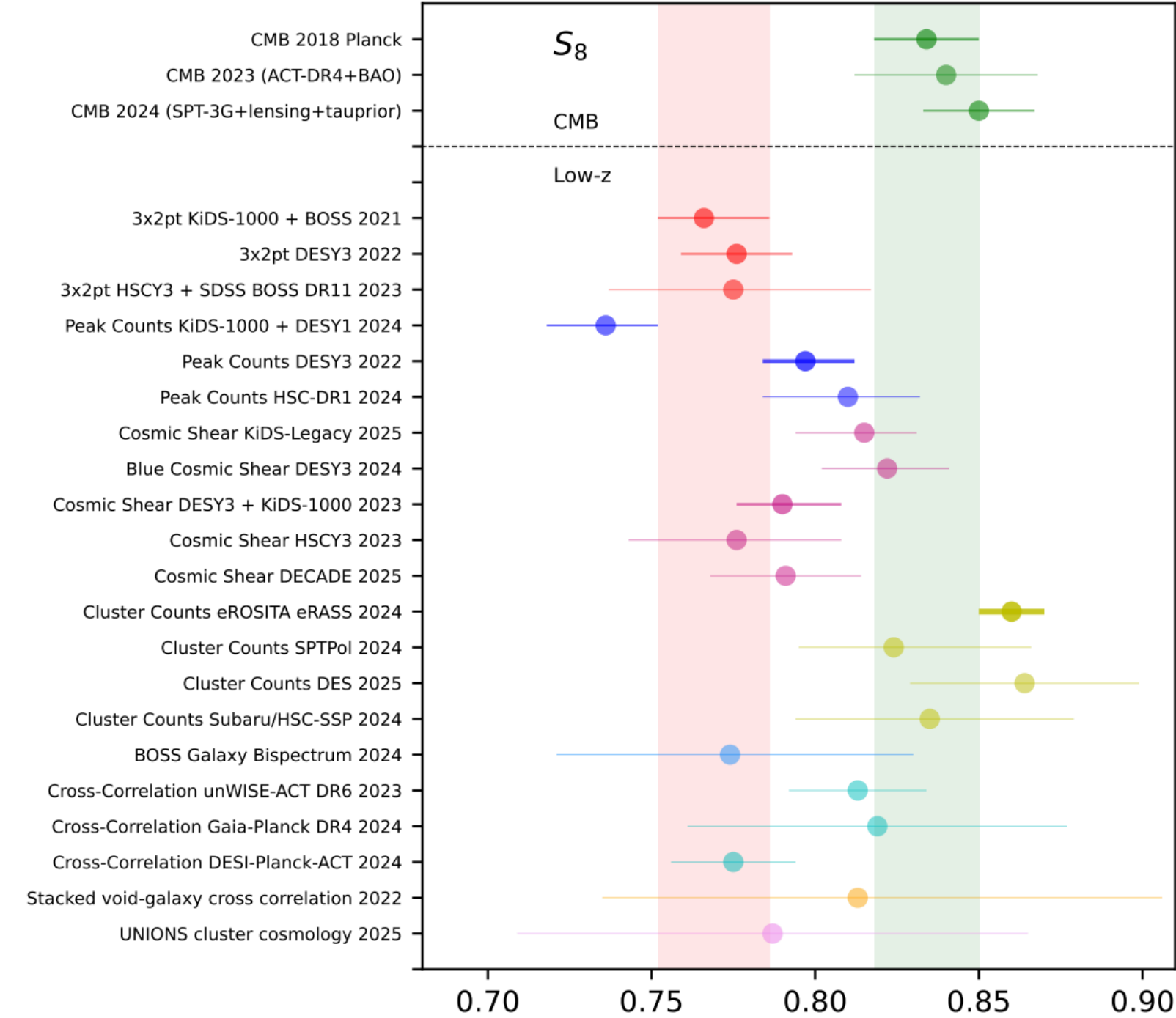


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## $S_8$ tension?

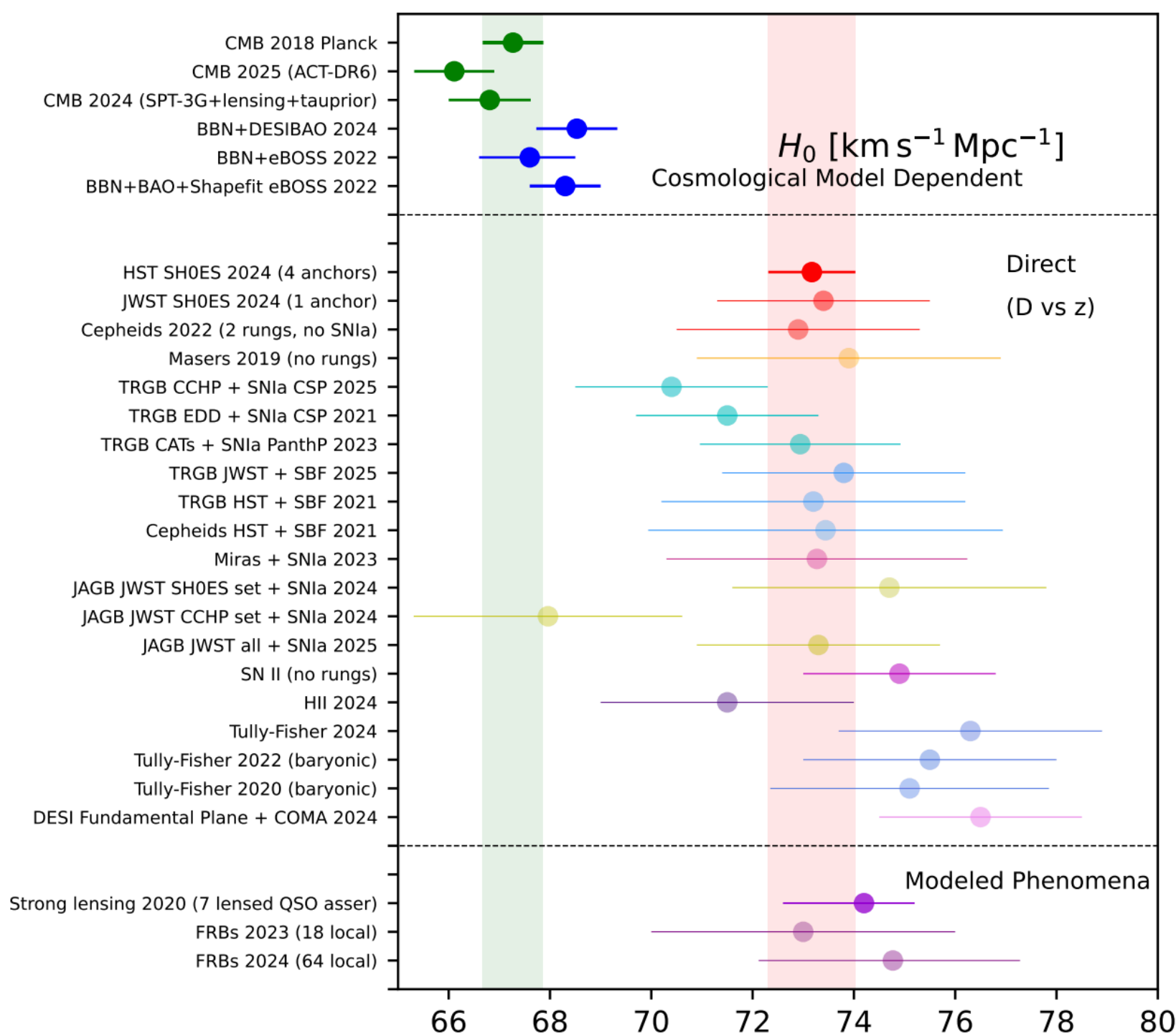


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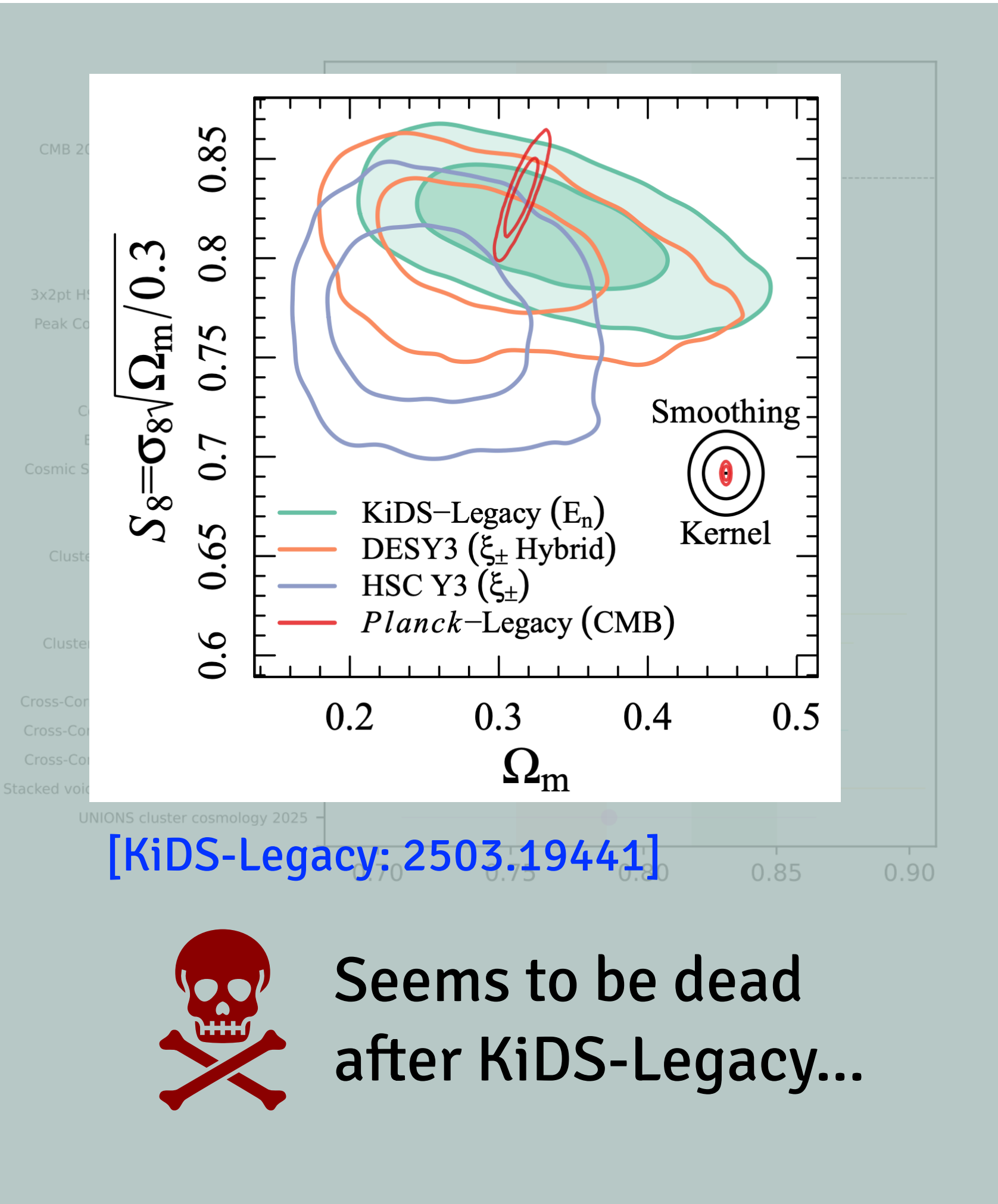
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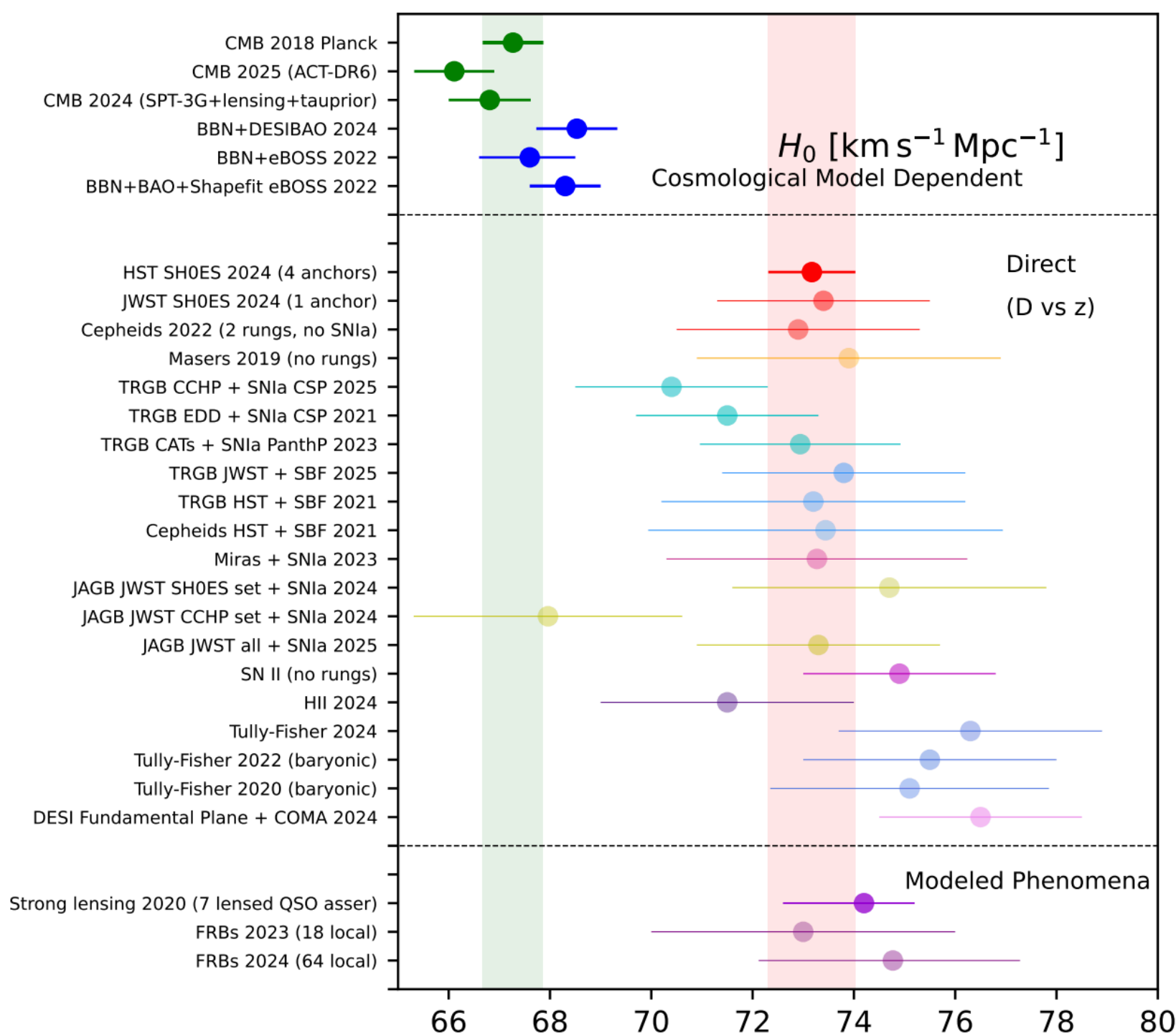


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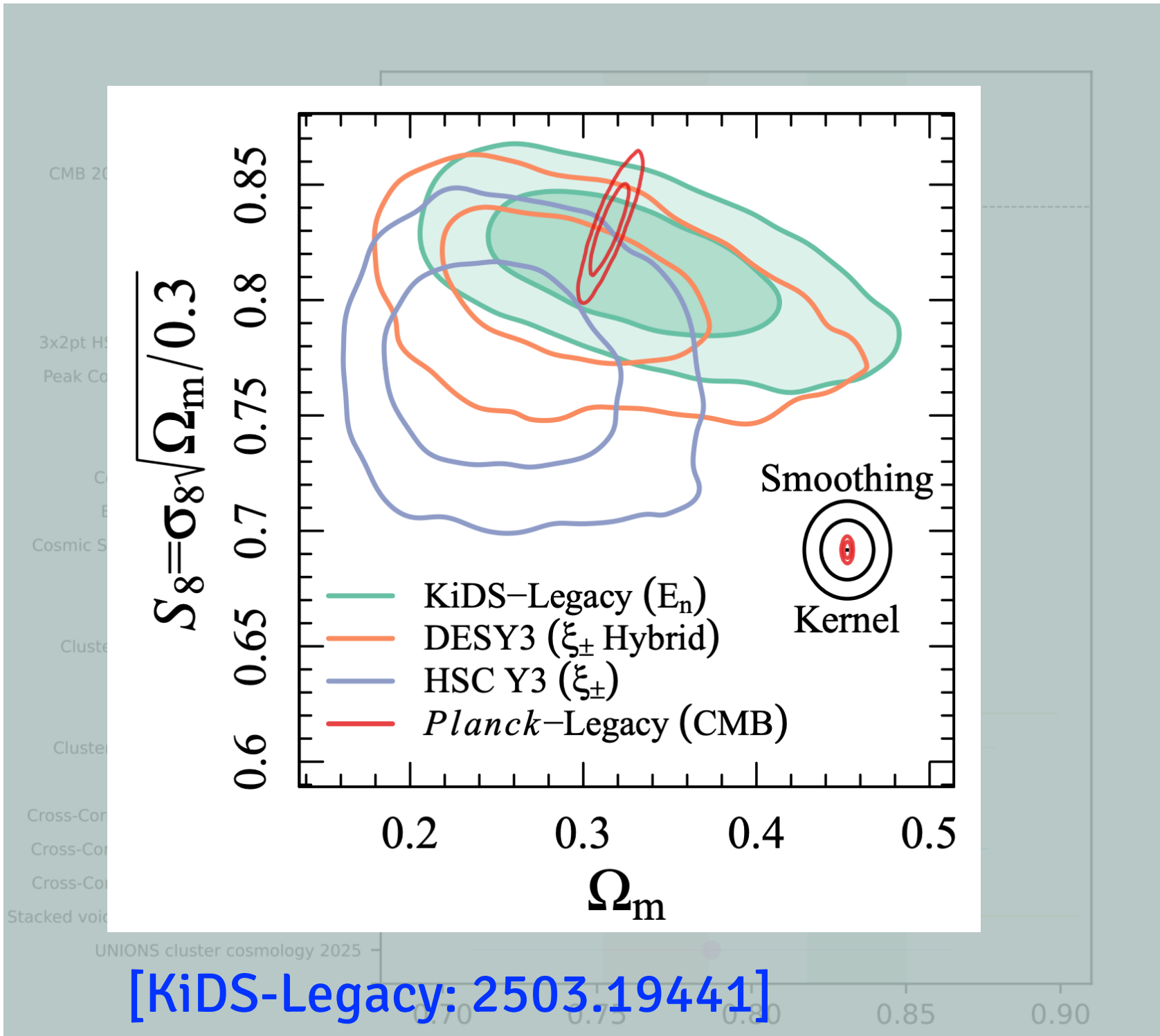
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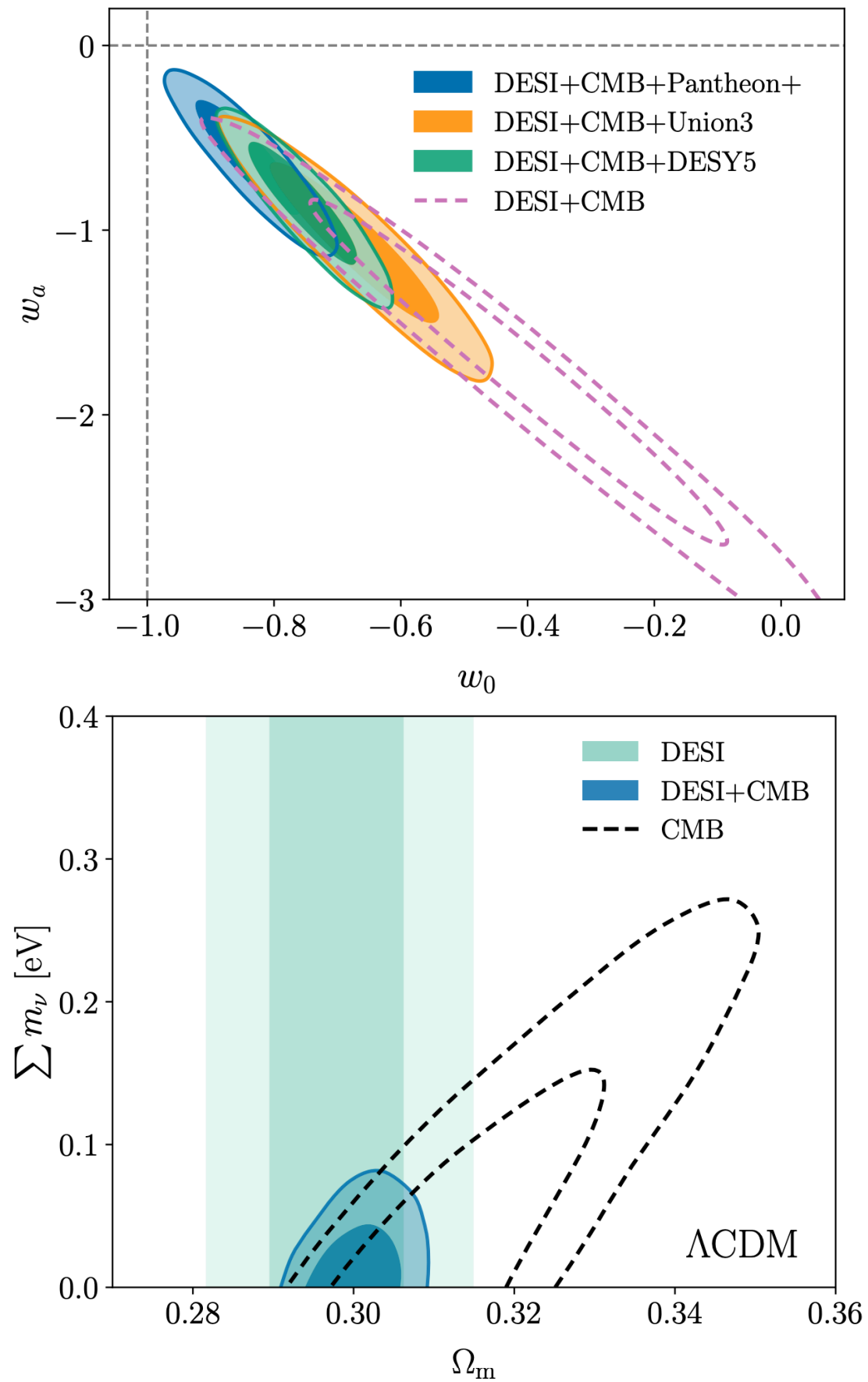
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## Latest DESI results



[DESI BAO DR2: 2503.14738]



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## Data

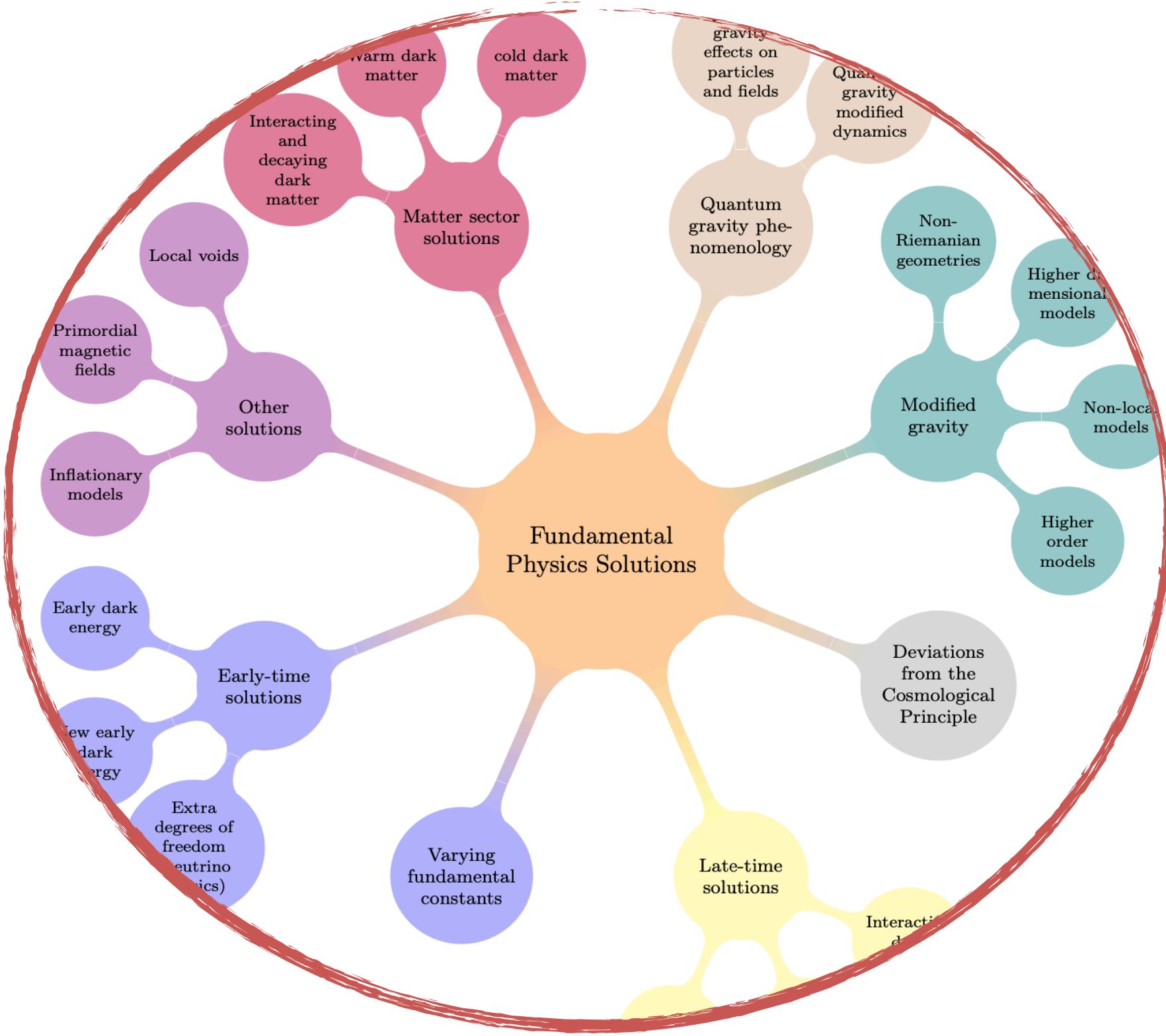




To learn about the universe, we need to **solve the inverse problem**

# Data

# Theory





# Some $\Lambda$ CDM extensions I studied in the past

## Decaying DM

[**GFA**+ 2008.09615]  
[**GFA**+ 2102.12498]  
[Simon, **GFA**+ 2203.07440]

## Early Modified Gravity /Early Dark Energy

[**GFA**, Braglia+ 2308.12345]  
[Murgia, **GFA**+ 2009.10733]

## Interacting Stepped DR

[Schöneberg & **GFA** 2206.11276]  
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## Decaying neutrinos

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## Hundreds of other models, e.g. see reviews:

“In the Realm of the Hubble tension - a Review of Solutions” Di Valentino+ [2103.01183]

“The  $H_0$  Olympics: a fair ranking of proposed models” Schöneberg, GFA+ [2107.10291]

“The CosmoVerse White Paper”, Di Valentino, Levi+ [2504.01669]



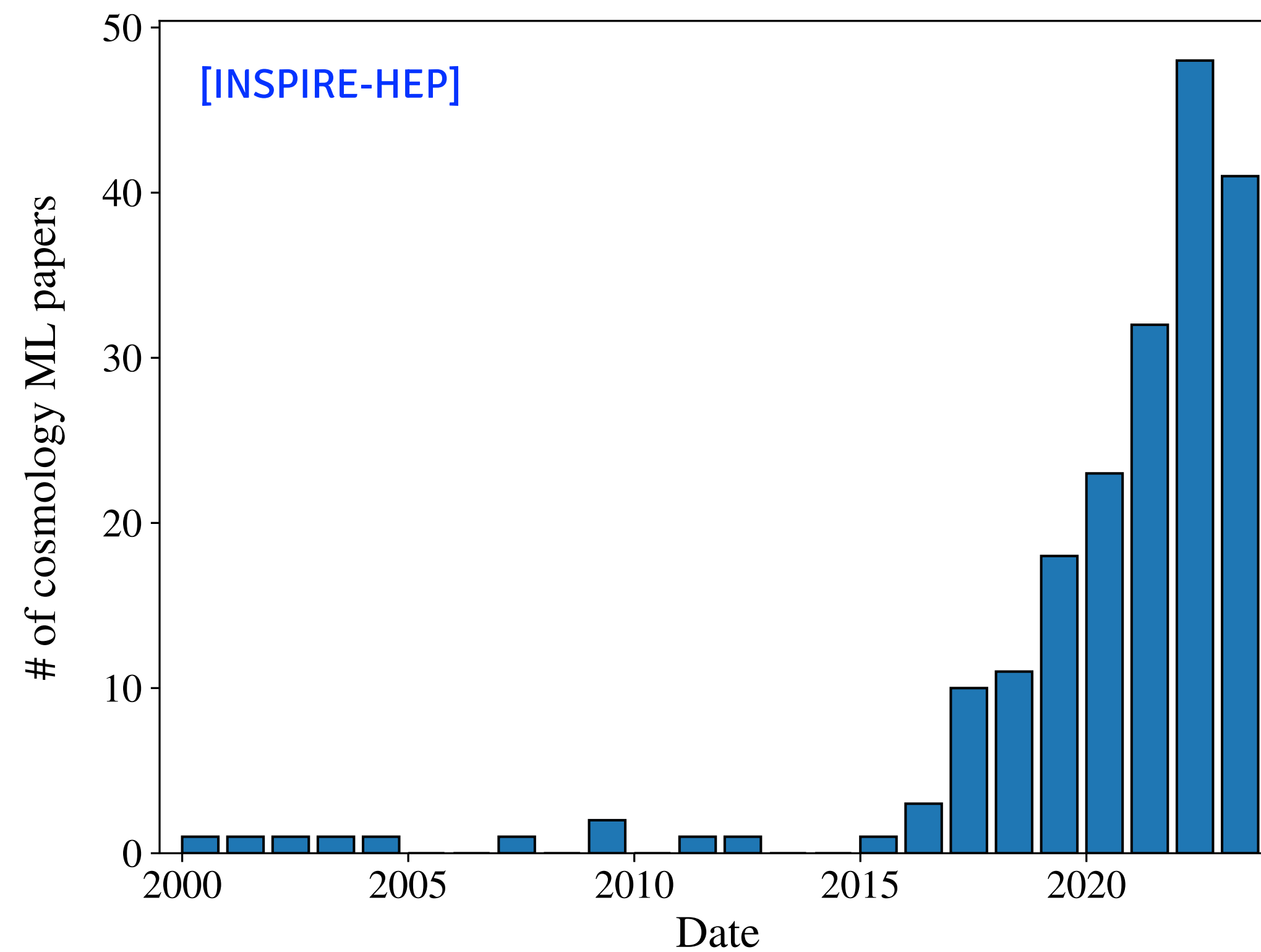
Comparing these vast volumes of cosmic data against the ever-increasing space of theories is a huge challenge



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- Expensive simulations
- High-dimensional parameter spaces





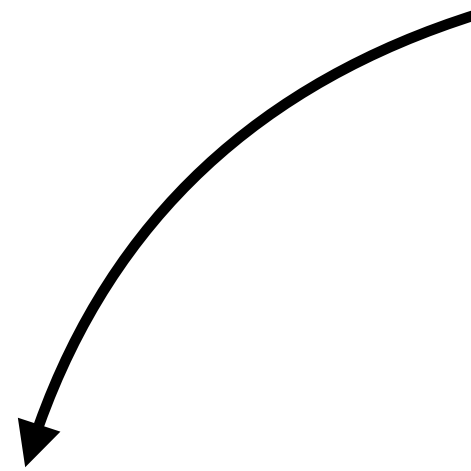
Machine learning is  
having a **strong impact**  
in cosmology



# **Two main approaches in ML**



## Two main approaches in ML



### **Emulators**

to **speed up** model evaluations of  
cosmological observables



## Two main approaches in ML



```
graph TD; A[Two main approaches in ML] --> B[Emulators]; A --> C[New statistical methods];
```

### **Emulators**

to **speed up** model evaluations of cosmological observables

### **New statistical methods**

to improve the sampling in **high-dimensional** parameter spaces

## 1. Emulators

For testing **invisible neutrino decays** with latest cosmic data

## 2. Simulation-based inference

For efficient inference from **Euclid** data, with applications to **evolving dark energy**

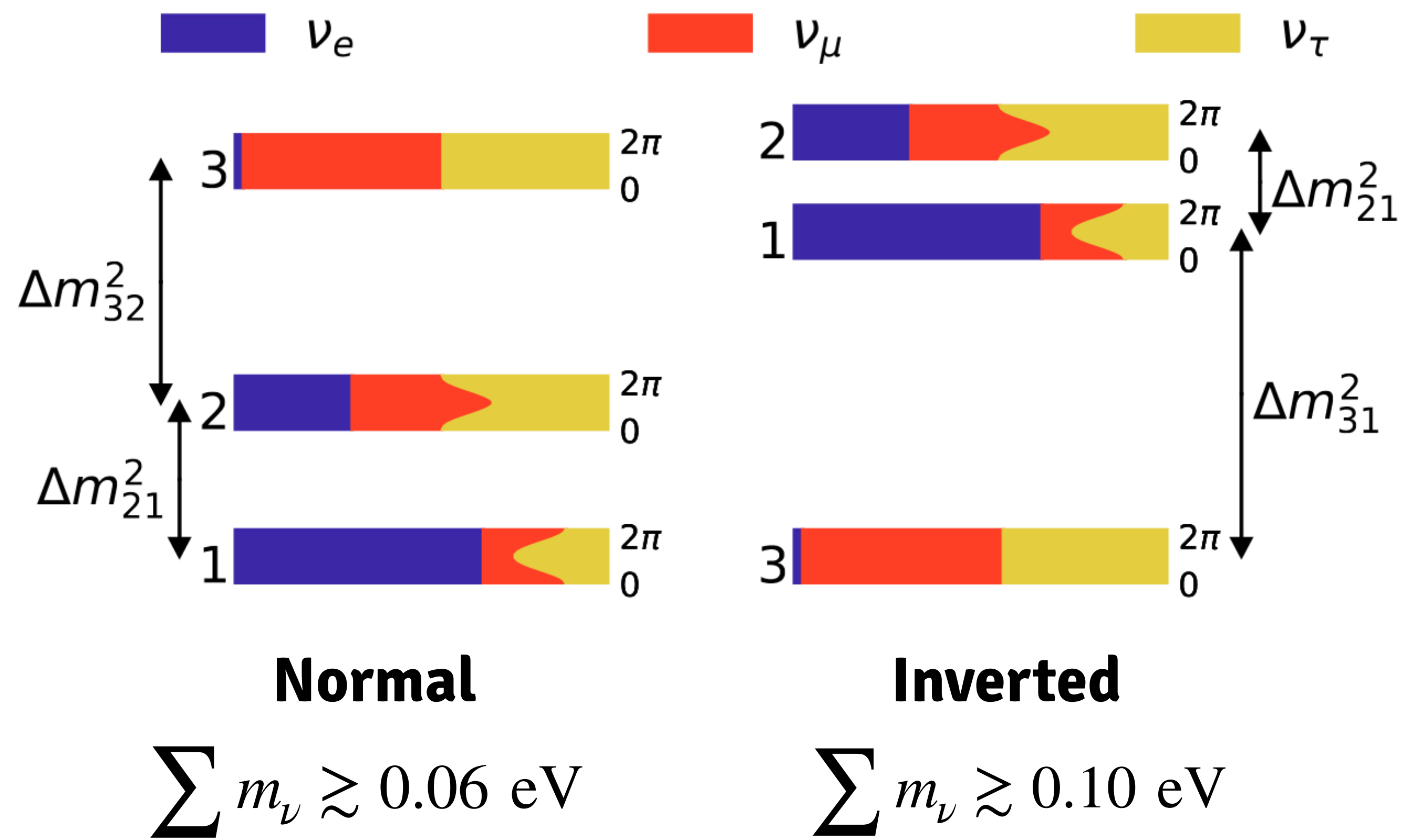


# 1. Emulators

For testing **invisible neutrino decays** with latest cosmic data

Ongoing work, to appear soon  
[arXiv:2506.XXXXX](#)

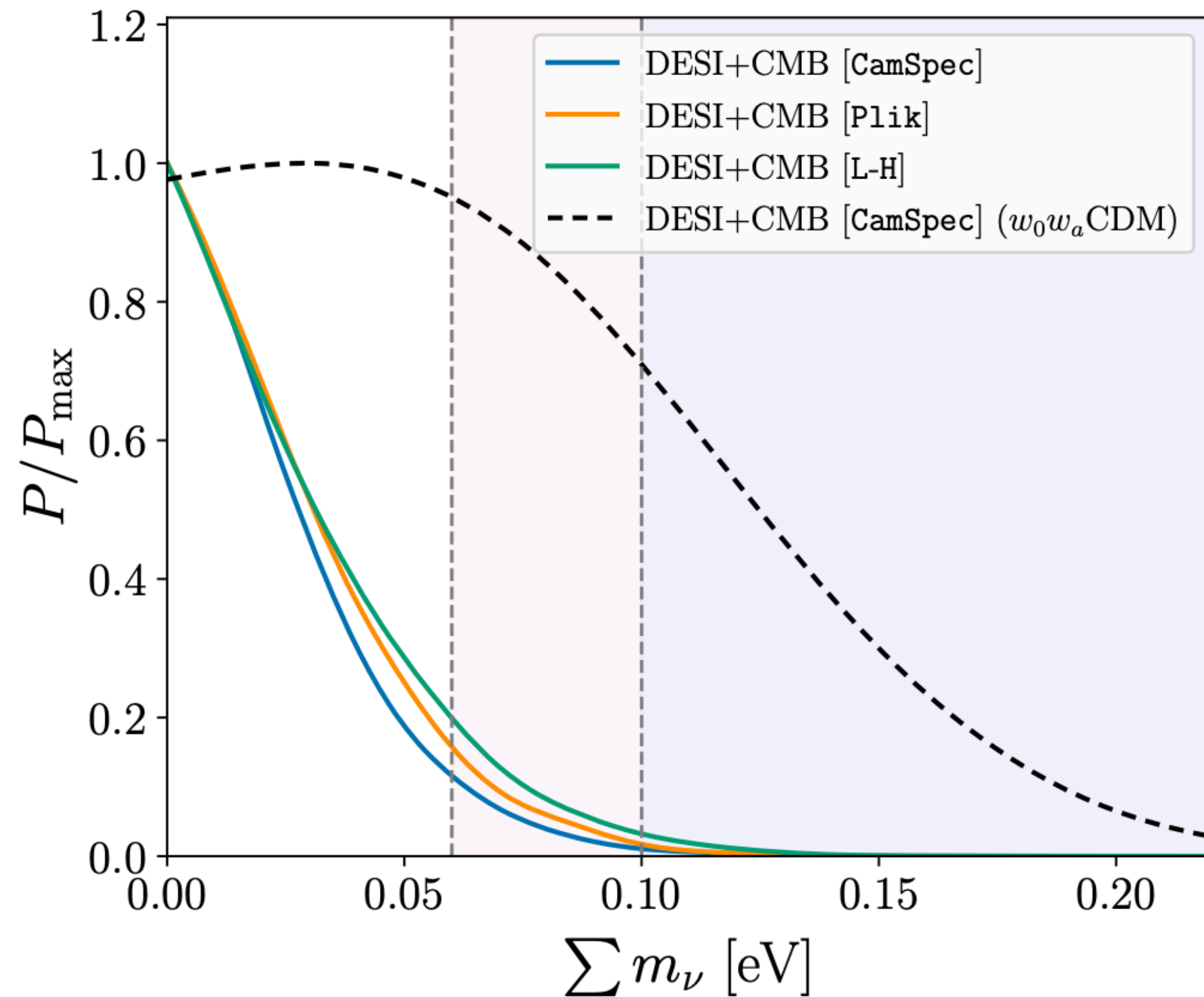
Oscillation experiments have provided convincing evidence that **neutrinos have mass**



[Salas et al. 1806.11051]



# Cosmological bounds

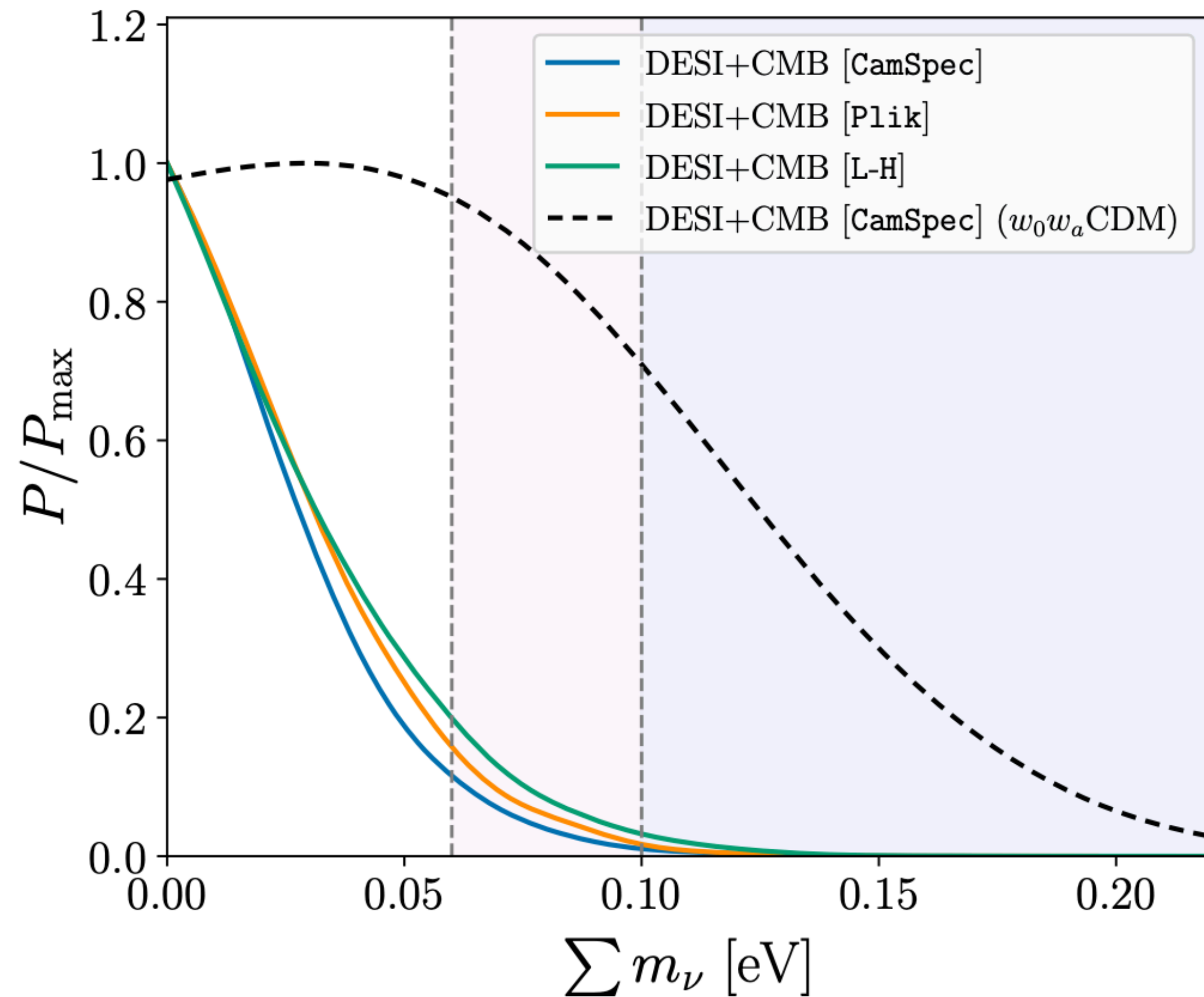


Cosmology has given tightest bound to date

$$\sum m_\nu < 0.064 \text{ eV} \quad (95\%, \text{ DESI+CMB [CamSpec]})$$

DESI DR2 Results II [2503.14738]

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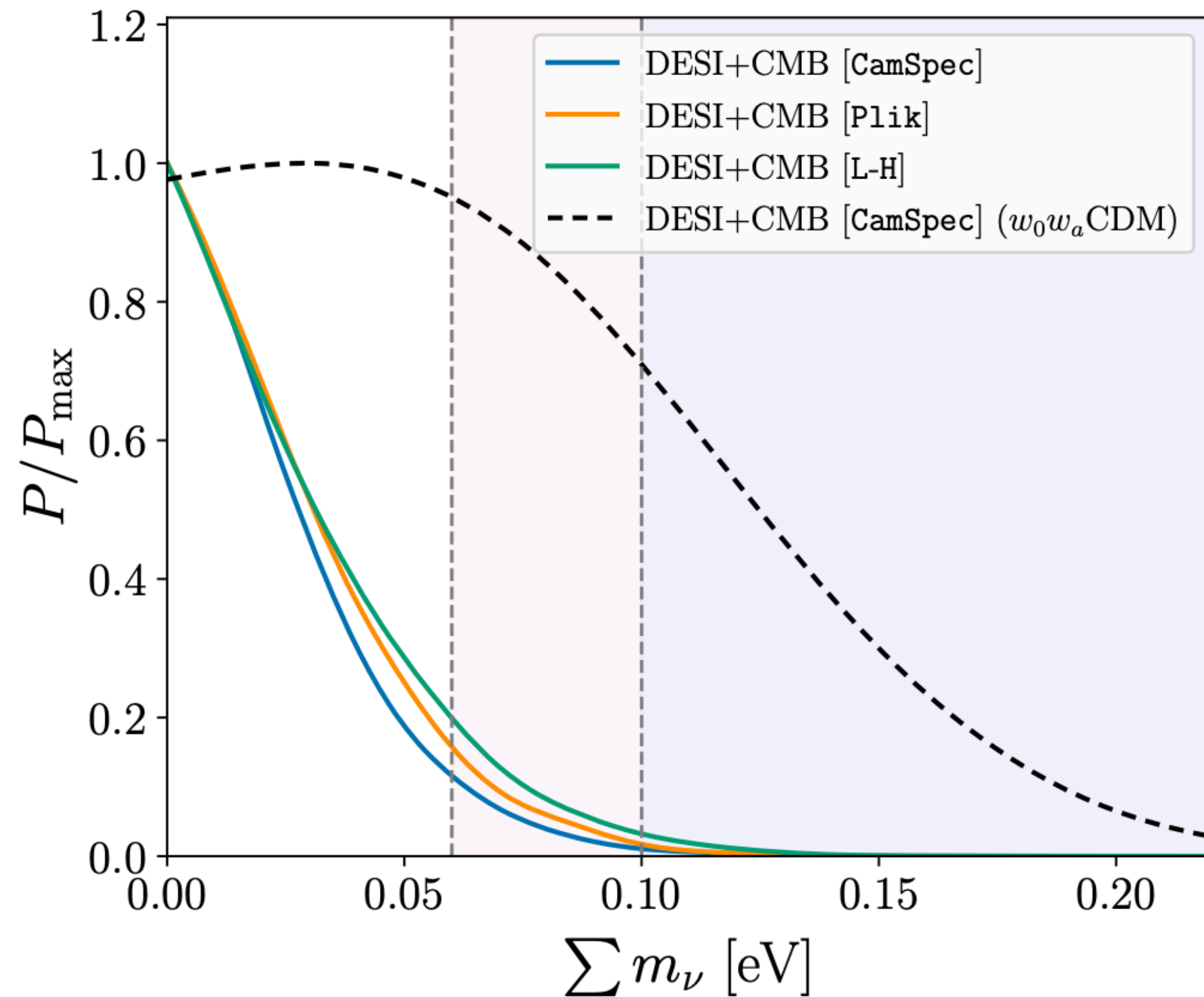
However, these bounds are **model dependent**

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What about changing **neutrino properties**?

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2 neutrinos decay **in the SM** but  $\tau_\nu \sim (G_F^2 m_\nu^5)^{-1} \gtrsim 10^{33} \text{ yr} \gg t_U$



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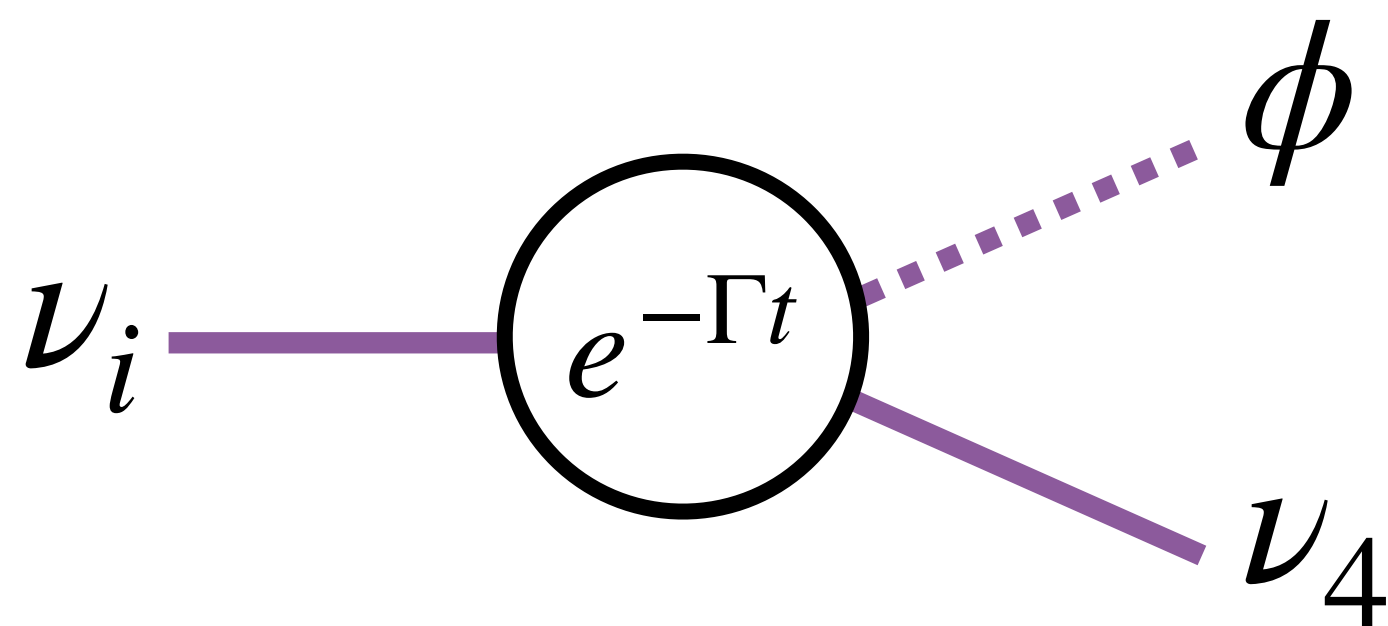
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Decays to **dark radiation**, much less constrained



Appears naturally in many **simple extensions of the seesaw mechanism**

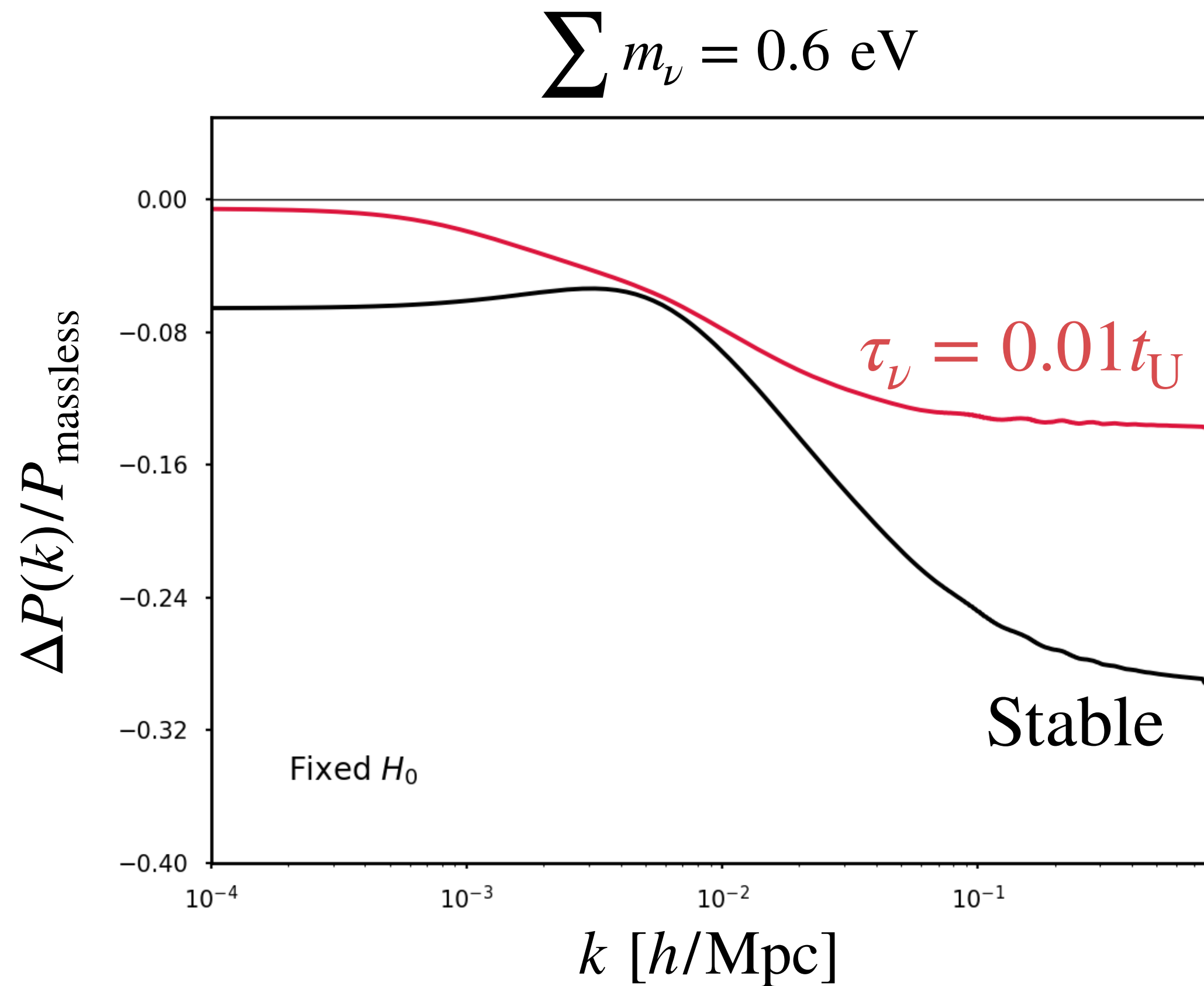
$$\mathcal{L}_{\text{int}} = \lambda i \phi \bar{\nu}_i \gamma_5 \nu_4 + \text{h.c.}$$

[Escudero & Fairbairn \[1907.05425\]](#)

[Escudero et al. \[2007.04994\]](#)

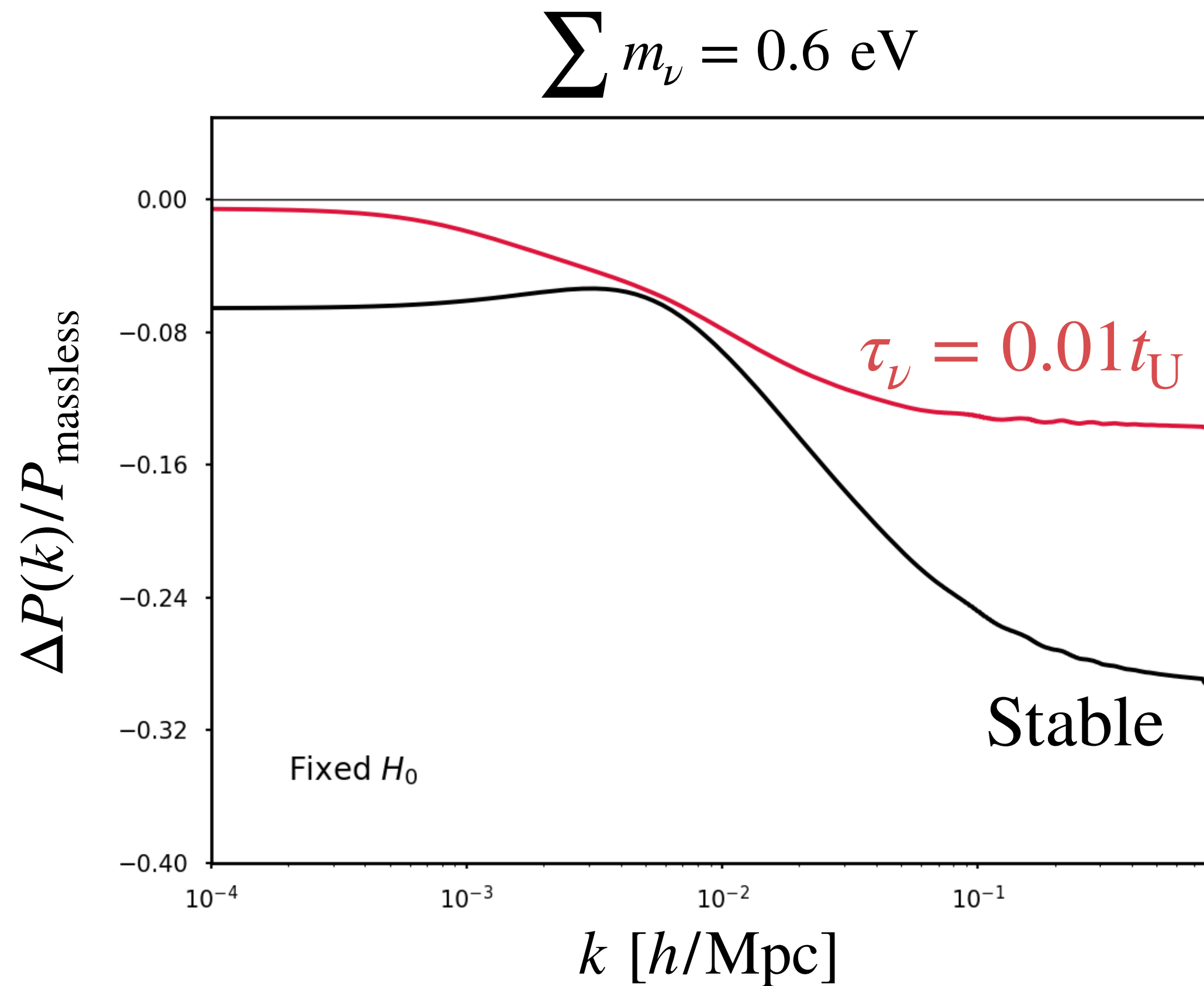


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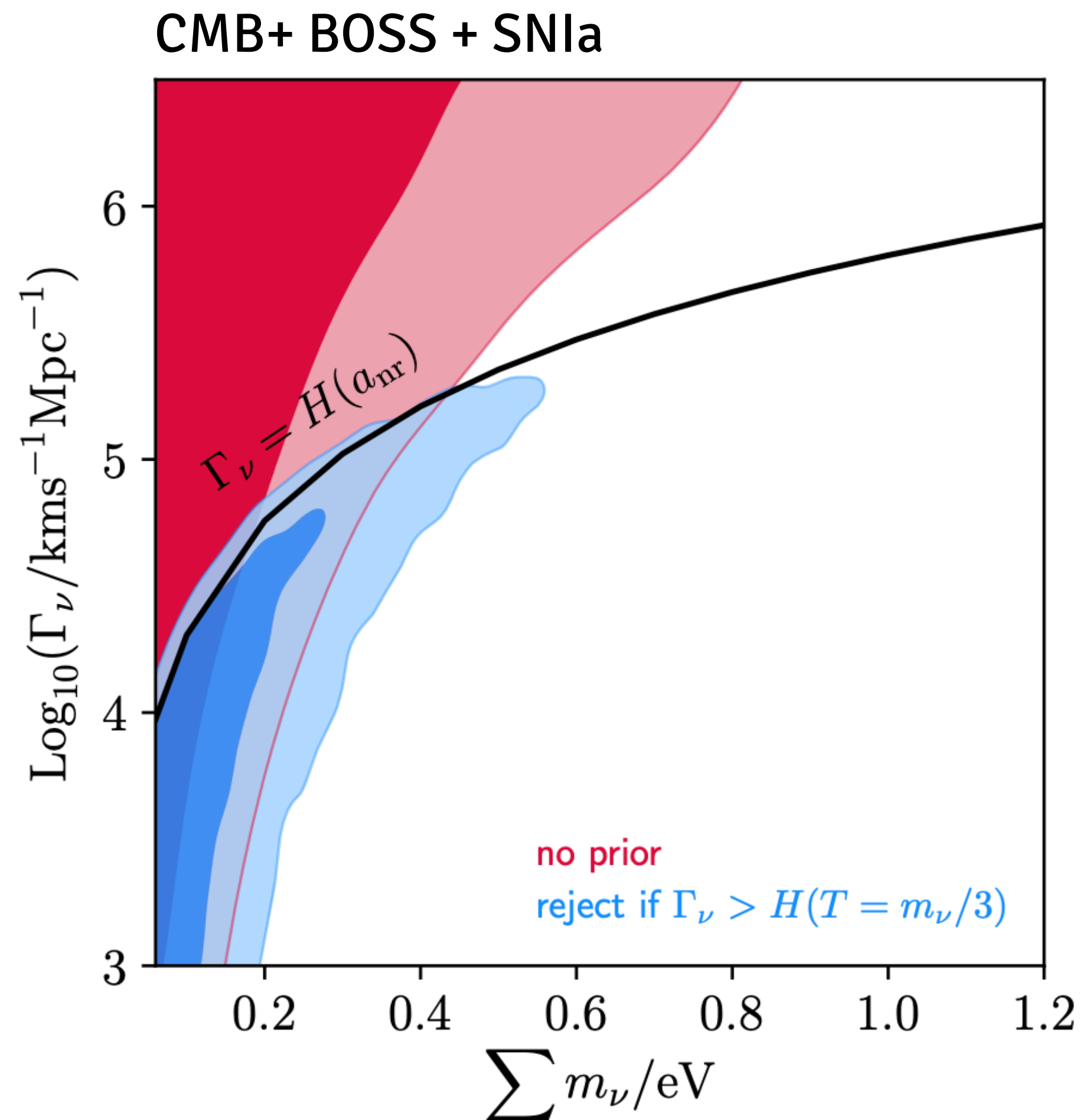


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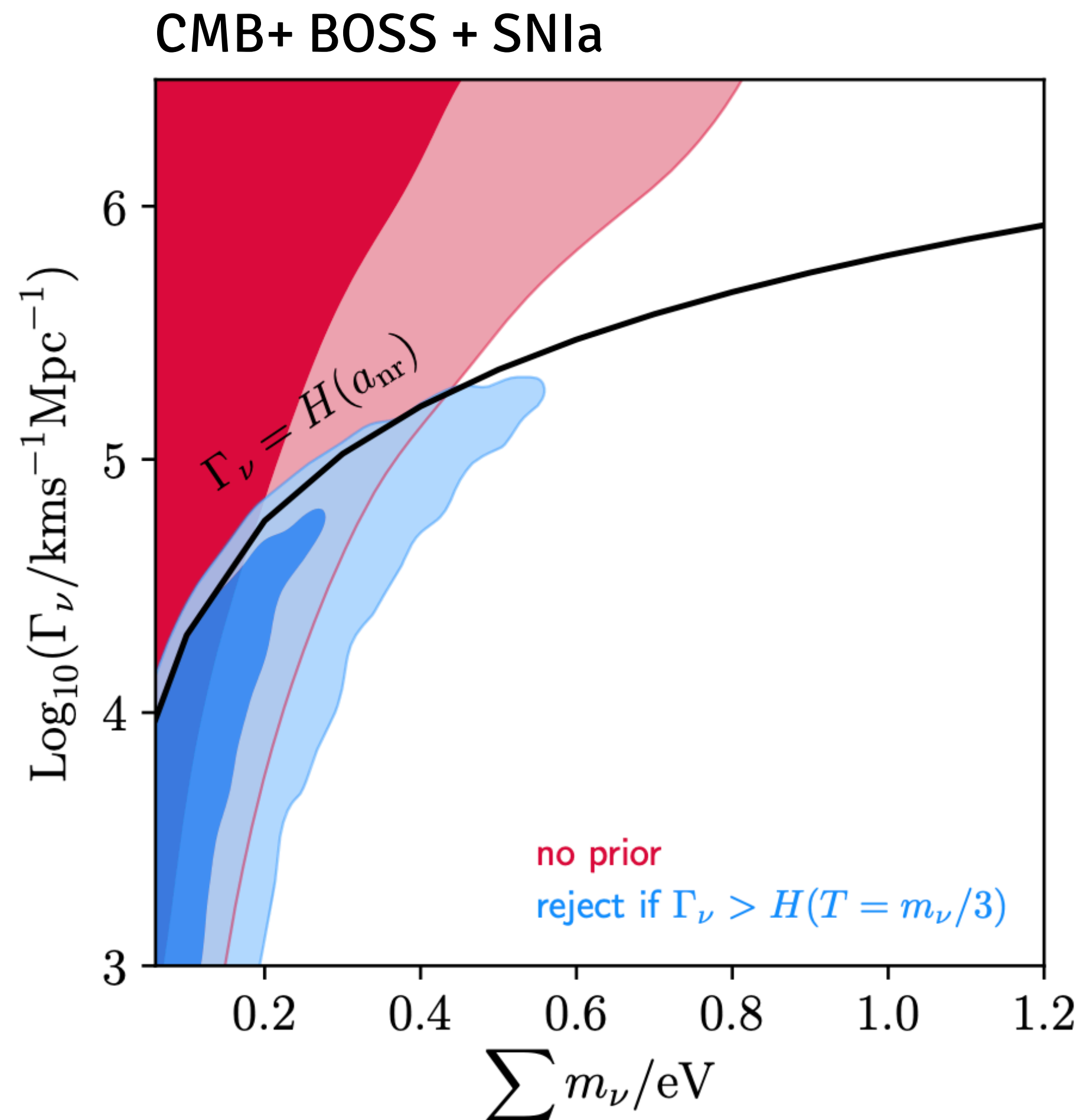
This permits a **relaxation of neutrino mass bounds** from cosmology





Back in 2021, we showed that **non-relativistic neutrino decays to DR** can relax mass bounds up to  $\Sigma m_\nu < 0.4 \text{ eV}$

Abellán et al. [2112.13862]



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## GOAL

Build emulator for neutrino decay model, and use it to **update mass bounds** in light of latest DESI data



# Emulating an Einstein-Boltzmann Solver (EBS)

**Cosmo. pars**

$H_0, \Omega_b, A_s, n_s, \dots$

# Emulating an Einstein-Boltzmann Solver (EBS)

Background/thermo eqs.

Cosmo. pars

$H_0, \Omega_b, A_s, n_s, \dots \longrightarrow$

$$\begin{aligned} H^2 &= \frac{8\pi G}{3} \sum_i \rho_i \\ \frac{d\rho_i}{d\tau} &= \dots, \quad \text{for } i = c, b, \gamma, \nu \\ \frac{dx_e}{d\tau} &= \dots, \quad \frac{dT_b}{d\tau} = \dots \end{aligned}$$

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→

**Perturbation eqs.**

$$\partial_\tau \Delta f_{0,i}(q, k, \tau) = \dots$$

$$\partial_\tau \Delta f_{1,i}(q, k, \tau) = \dots$$

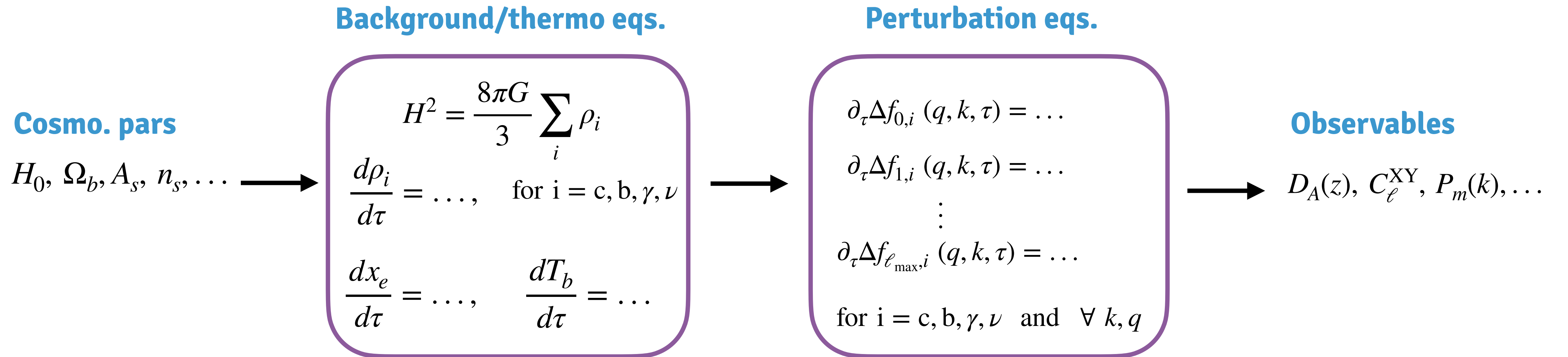
$$\vdots$$

$$\partial_\tau \Delta f_{\ell_{\max},i}(q, k, \tau) = \dots$$

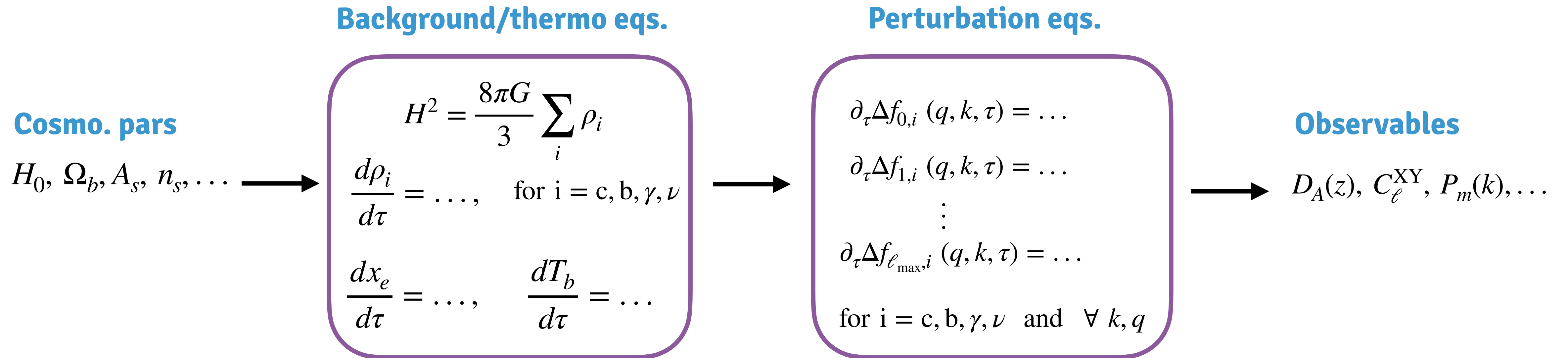
for  $i = c, b, \gamma, \nu$  and  $\forall k, q$



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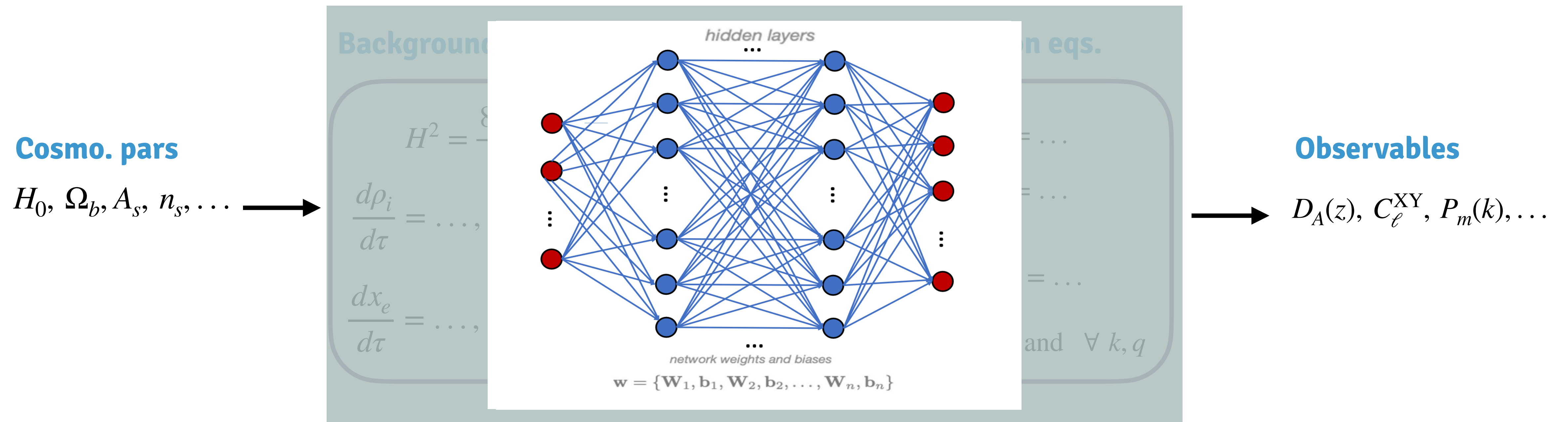


# Emulating an Einstein-Boltzmann Solver (EBS)



A single call to an EBS (e.g. CLASS) can be **time-consuming in  $\Lambda$ CDM extensions**.  
 Moreover, one often needs  **$\sim 10^6$  model evaluations** for accurate inference.

# Emulating an Einstein-Boltzmann Solver (EBS)



**IDEA:** Replace the calculation of the full system of linear Einstein-Boltzmann eqs. by a **trained emulator**, e.g. a neural network (NN)



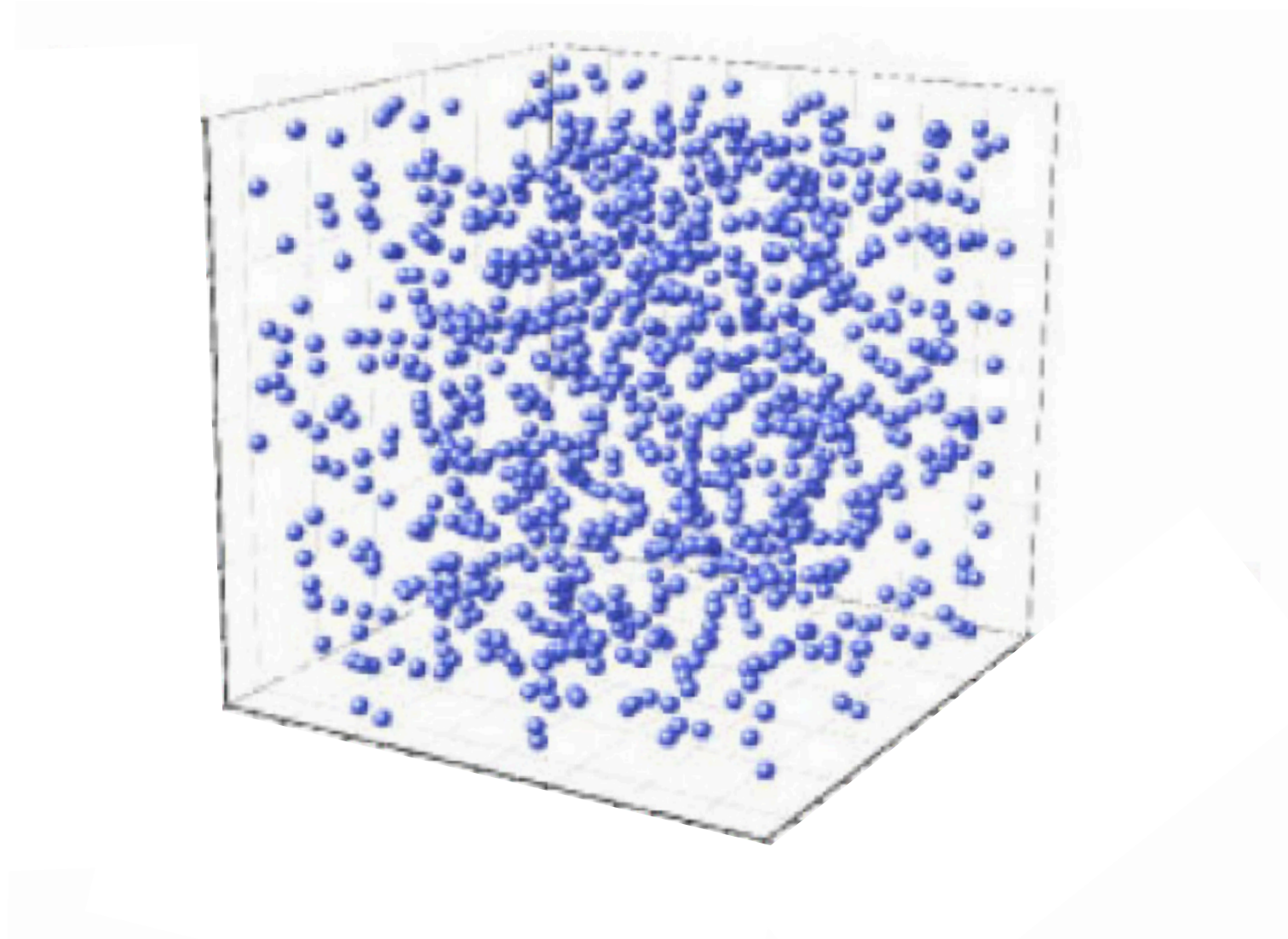
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Many EBS emulators available on the market (e.g. [CosmoPower](#), [CosmicNet](#), [Capse.jl](#))  
We rely on [CONNECT](#) [Nygaard et al. 2205.15726]

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## Latin Hypercube (LHC) sampling

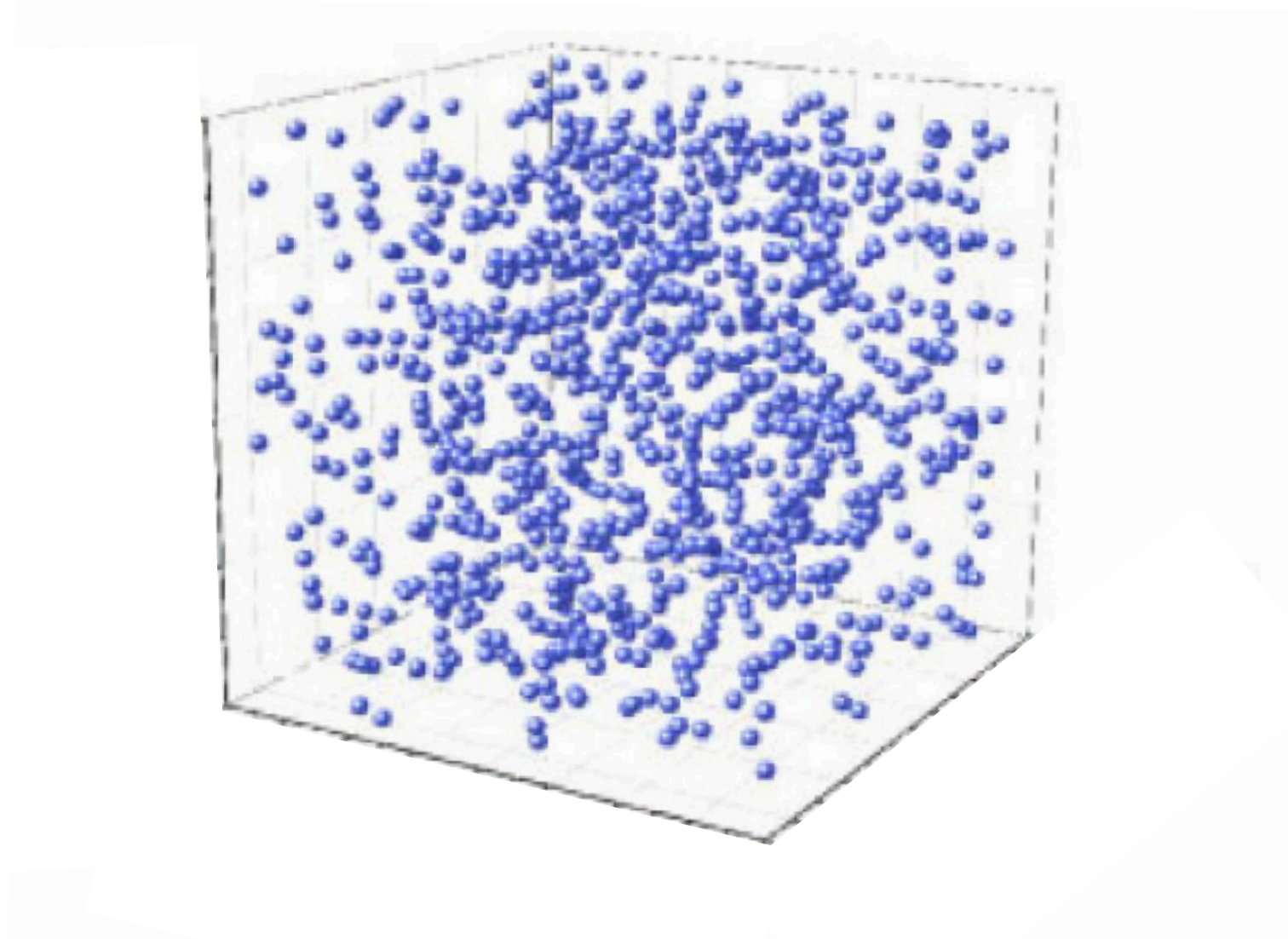


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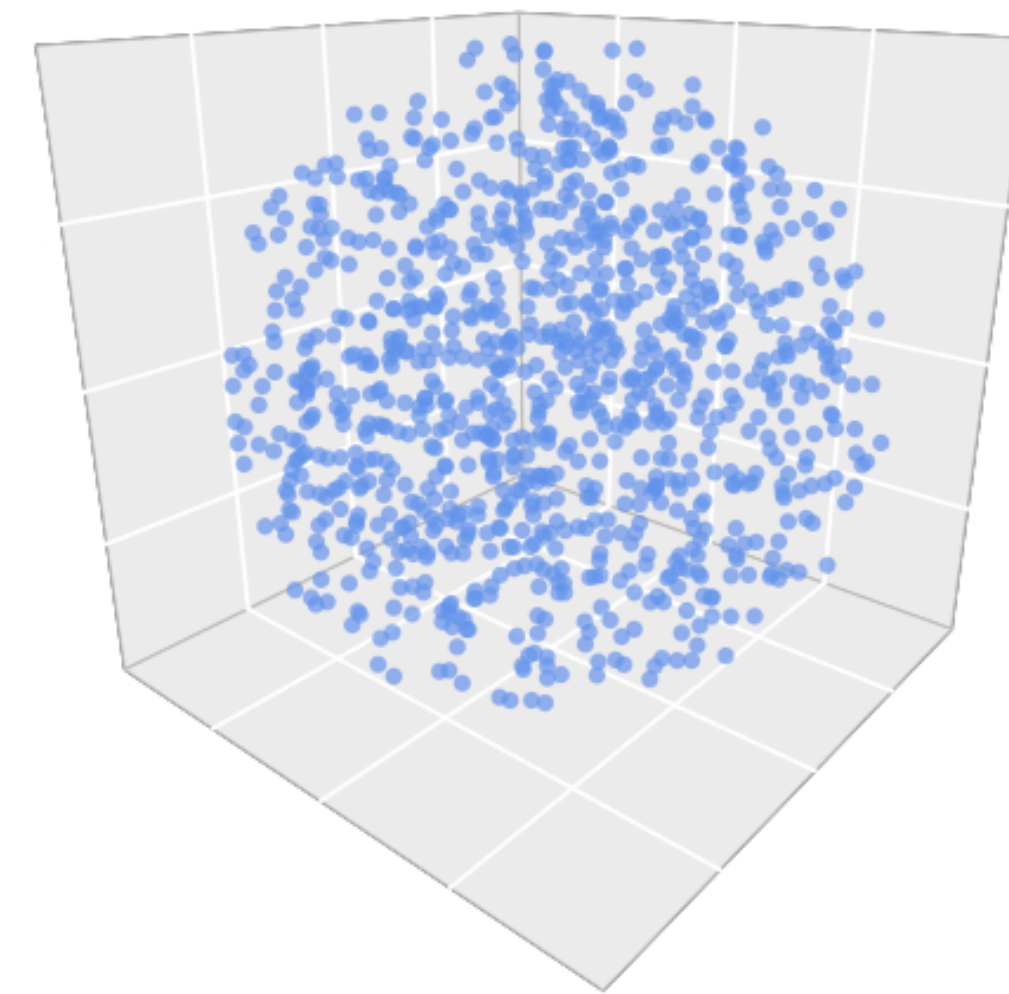
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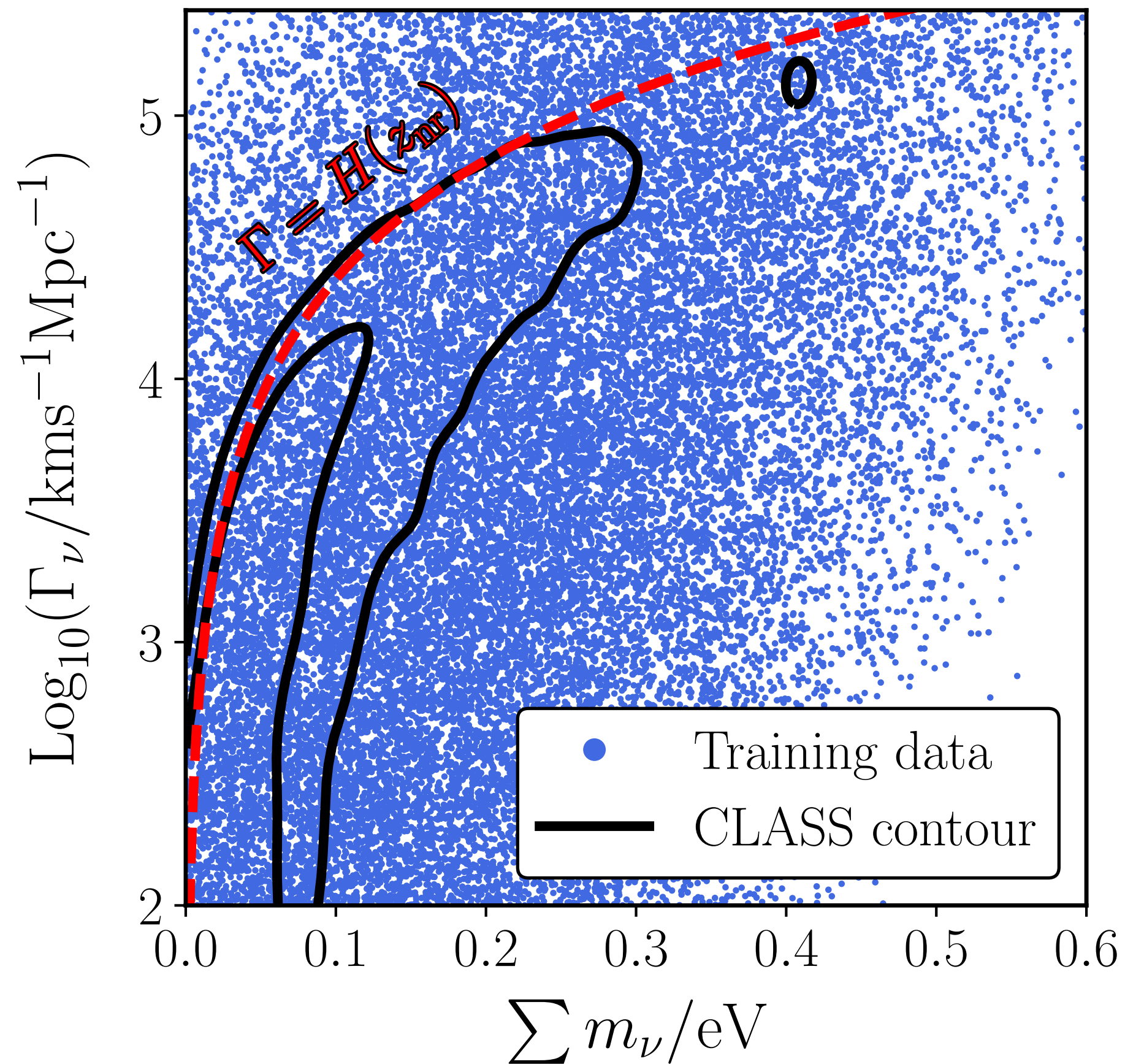
## Hypersphere sampling



Allows to concentrate points in  
**high-likelihood regions**  
→ **more efficient and accurate**



# Building emulator for decaying neutrinos

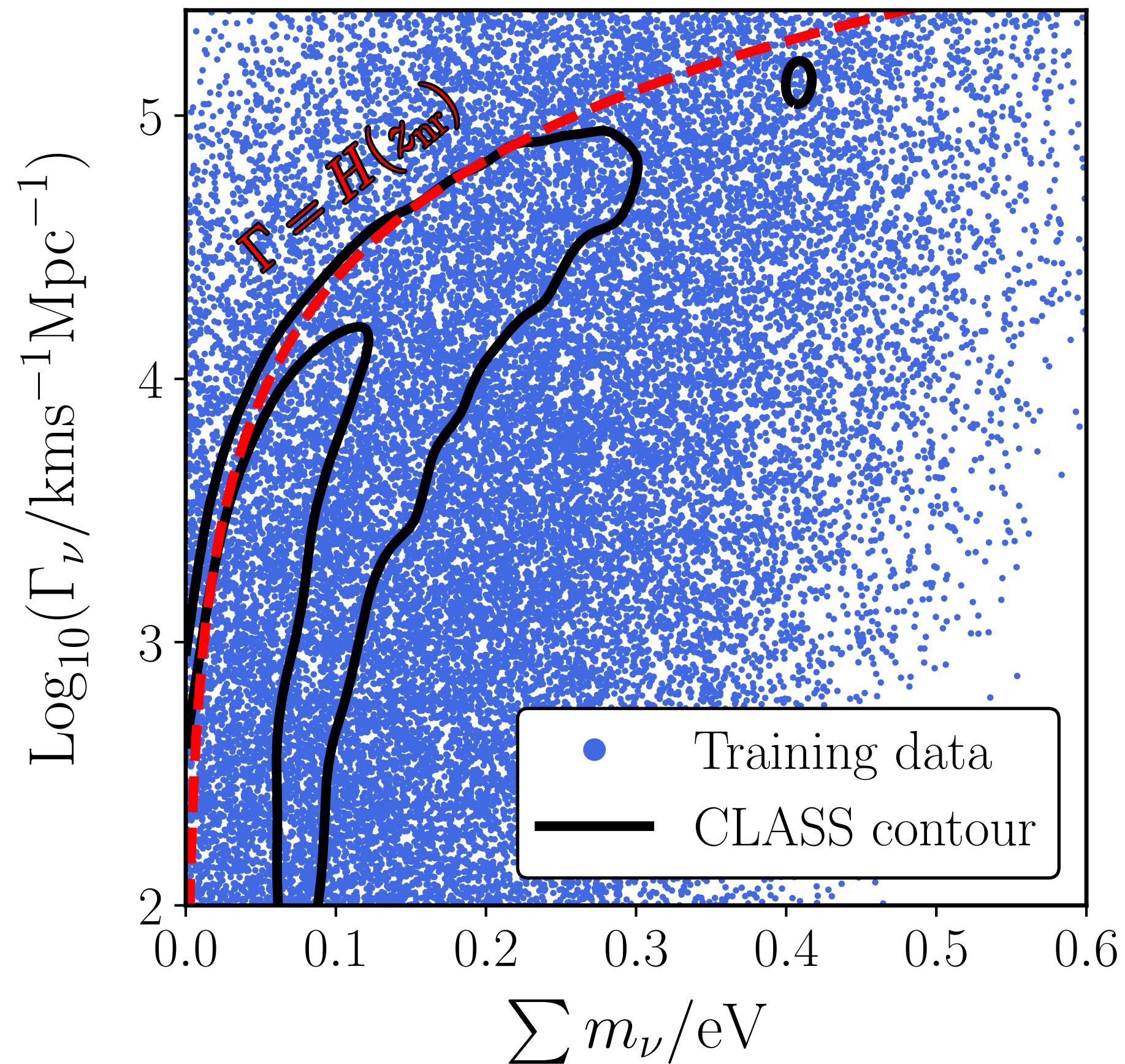


**Training data:**  $2.5 \times 10^4$  samples of  $\{\theta, \mathbf{x}\}$  in the 8-dimensional hypersphere

$$\theta = \{\omega_b, \omega_c, H_0, \ln(10^{10} A_s), n_s, \tau_{\text{reio}}, m_\nu, \log_{10} \Gamma_\nu\}$$

$$\mathbf{x} = \{C_\ell^{\text{TT}}, C_\ell^{\text{EE}}, C_\ell^{\text{TE}}, C_\ell^{\phi\phi}, H(z), D_A(z)\}$$

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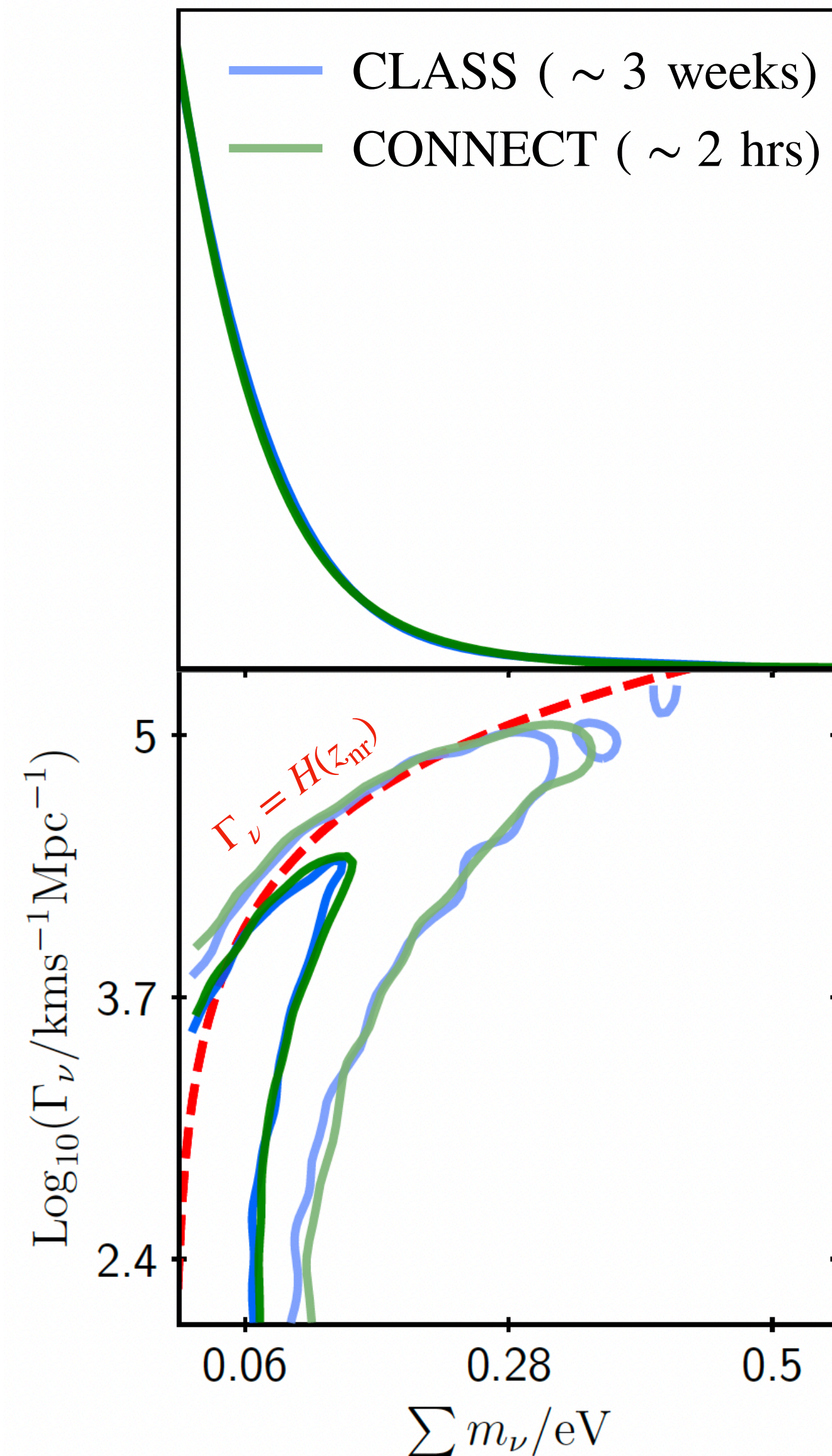
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Data generation took  $\sim 1$  day on 128 CPUs  
(training the NNs was much faster)



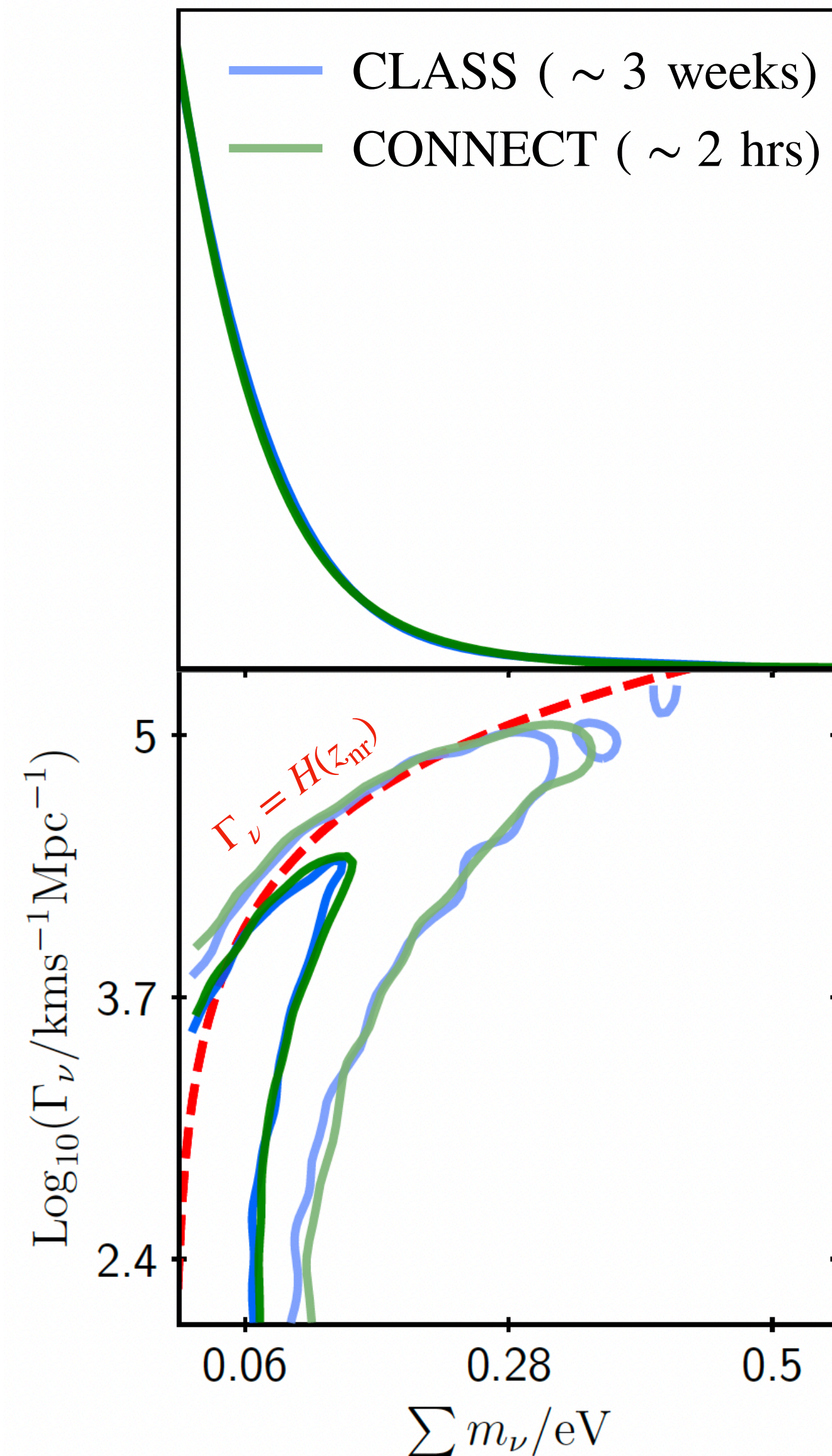
# Cosmological constraints



CONNECT posteriors are in good agreement with CLASS, while being  $\times 250$  faster



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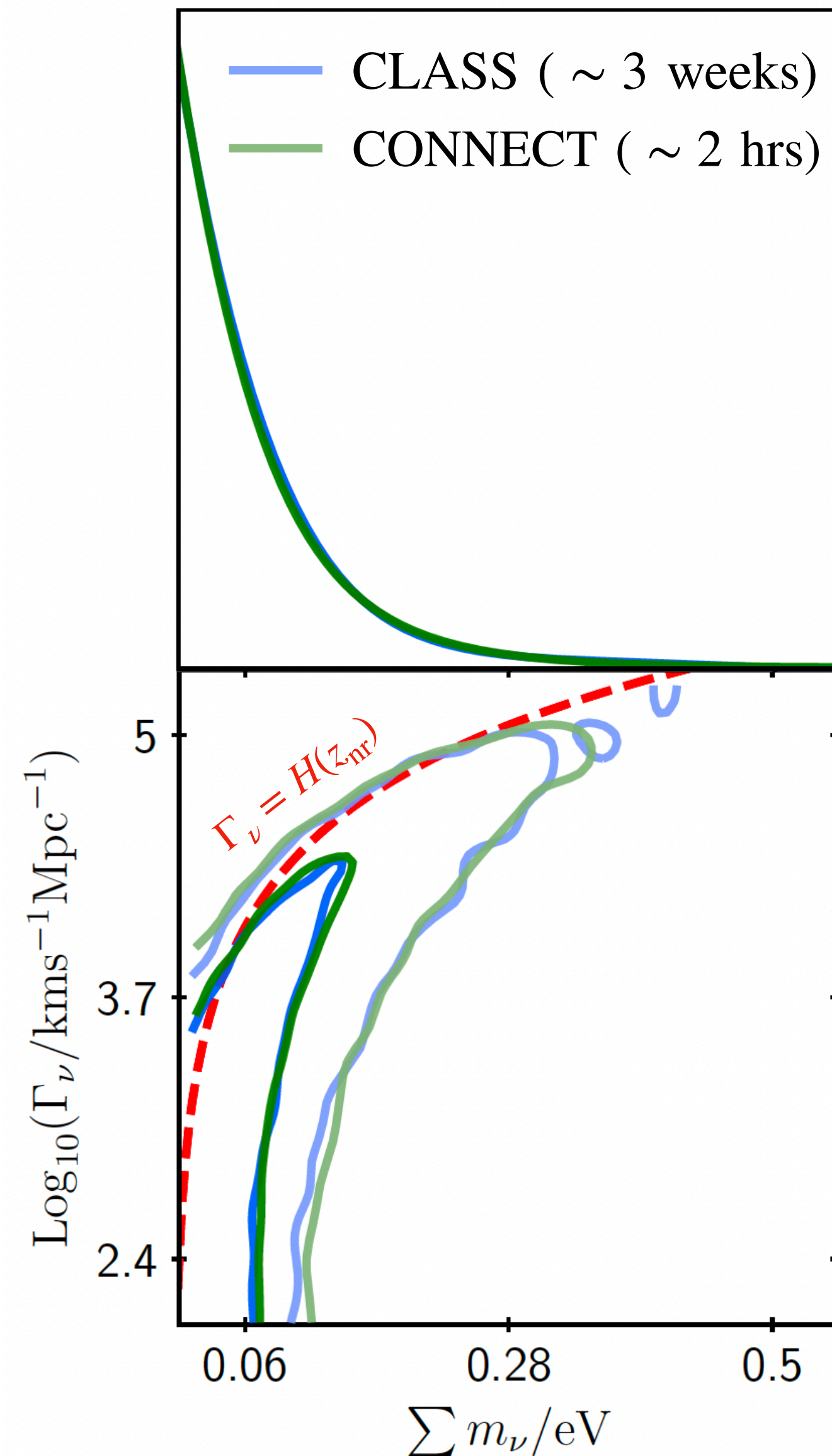


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**New mass bound:**

$$\sum m_\nu < 0.24 \text{ eV} \quad (95\%, \text{ DESI DR2+CMB [Plik]})$$

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**Next step:** derive bounds for neutrino decays with realistic mass splittings  $\nu_i \rightarrow \nu_j + \phi$



Based on [arXiv:2403.14750](#)  
[arXiv:2506.XXXX](#)

with Guadalupe Cañas-Herrera, Matteo  
Martinelli, Oleg Savchenko, Noemi Anau  
Montel & Christoph Weniger

## 2. **Simulation-based inference**

For efficient inference from  
**Euclid** data, with applications  
to **evolving dark energy**



# Bayesian inference

$\mathbf{x}_0$  : Data

$\theta$  : Parameters

$$\begin{array}{c} \text{Posterior} \\ p(\theta | \mathbf{x}_0) \end{array} \propto \begin{array}{c} \text{Likelihood} \\ p(\mathbf{x}_0 | \theta) \end{array} \begin{array}{c} \text{Prior} \\ p(\theta) \end{array}$$

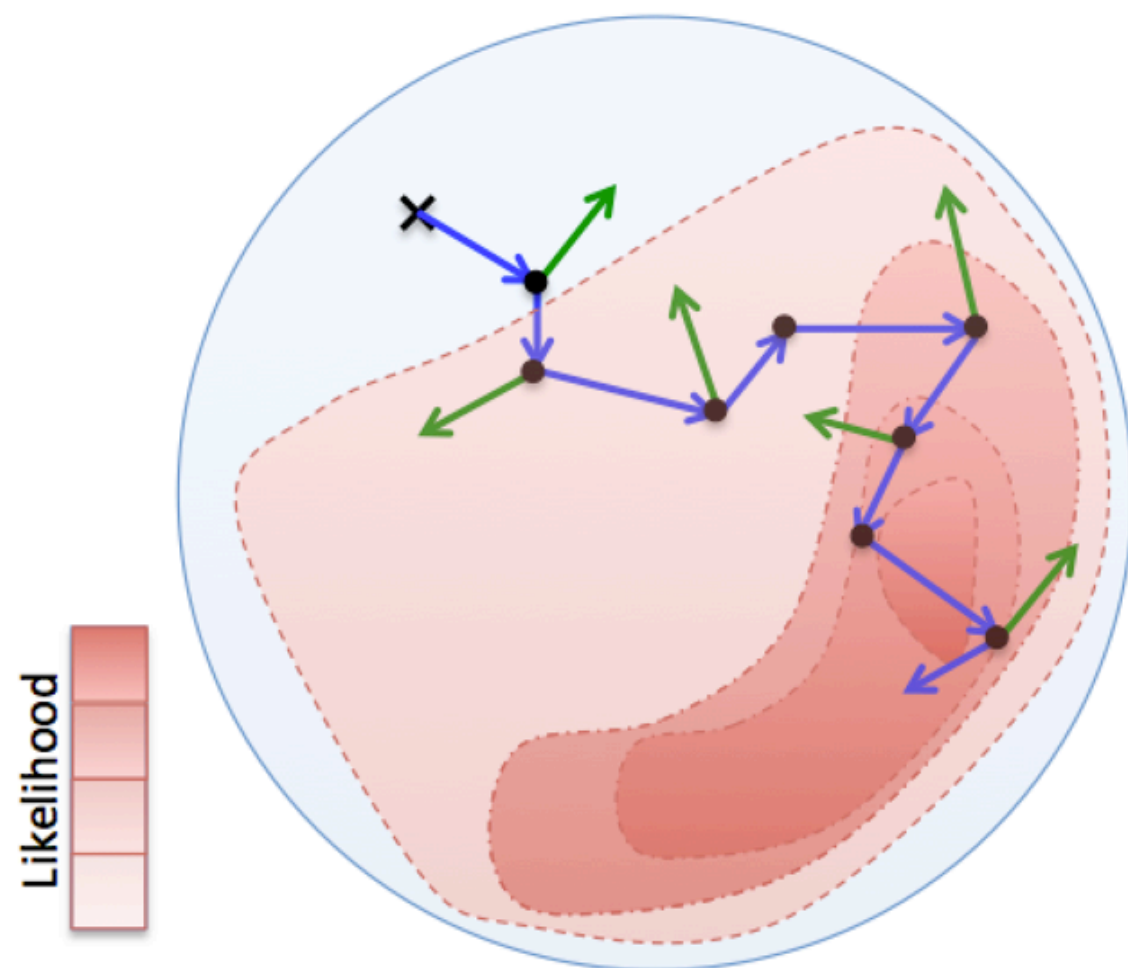
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Metropolis-Hastings algorithm

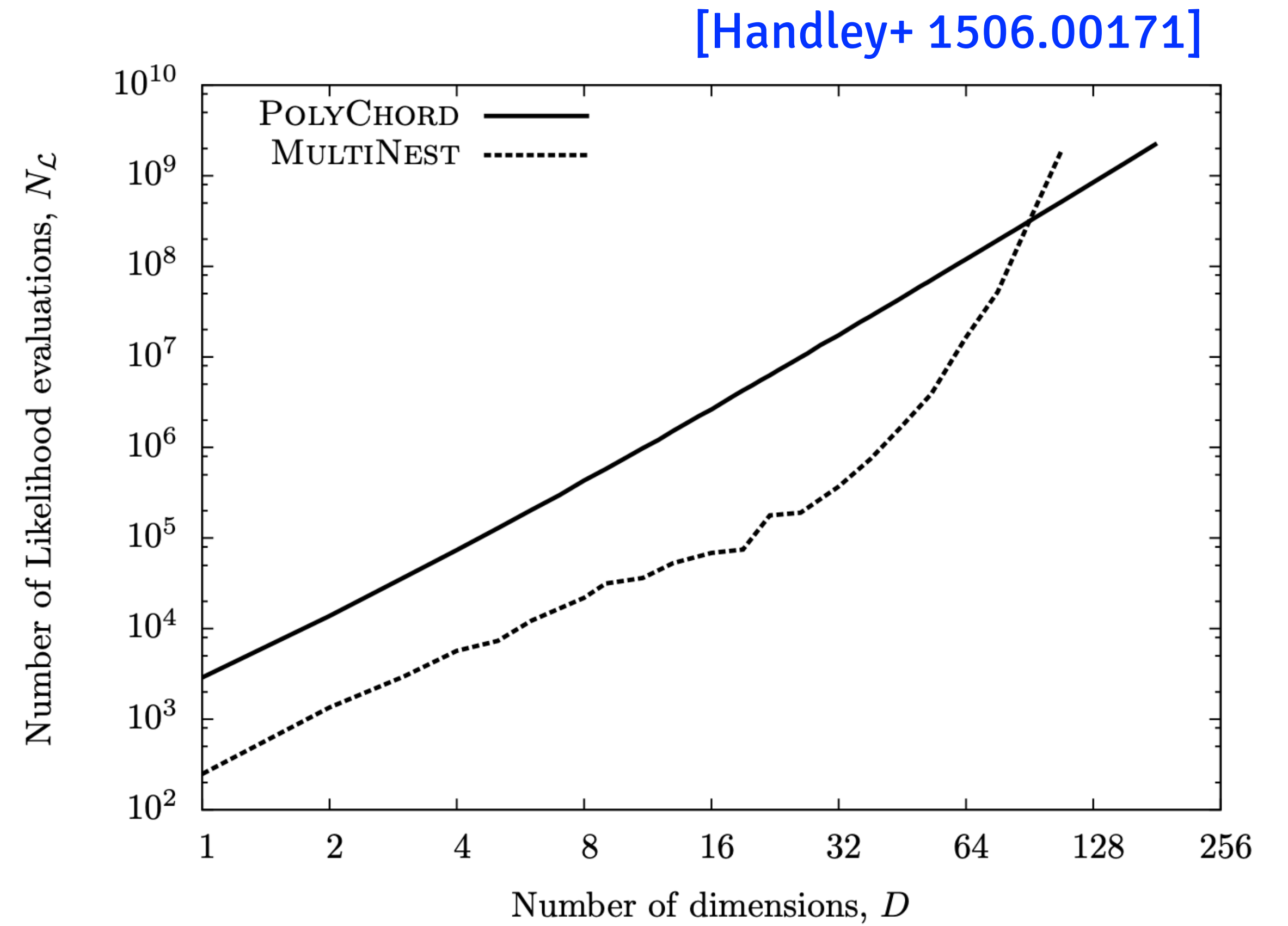


Traditional **likelihood-based** methods allow to get samples from the **full joint posterior** for some fixed data  $\mathbf{x}_0$

$$\theta \sim p(\theta | \mathbf{x}_0), \quad \text{for } \theta \in \mathbb{R}^D$$

# Current challenges

- MCMC methods **scale poorly** with the dimensionality



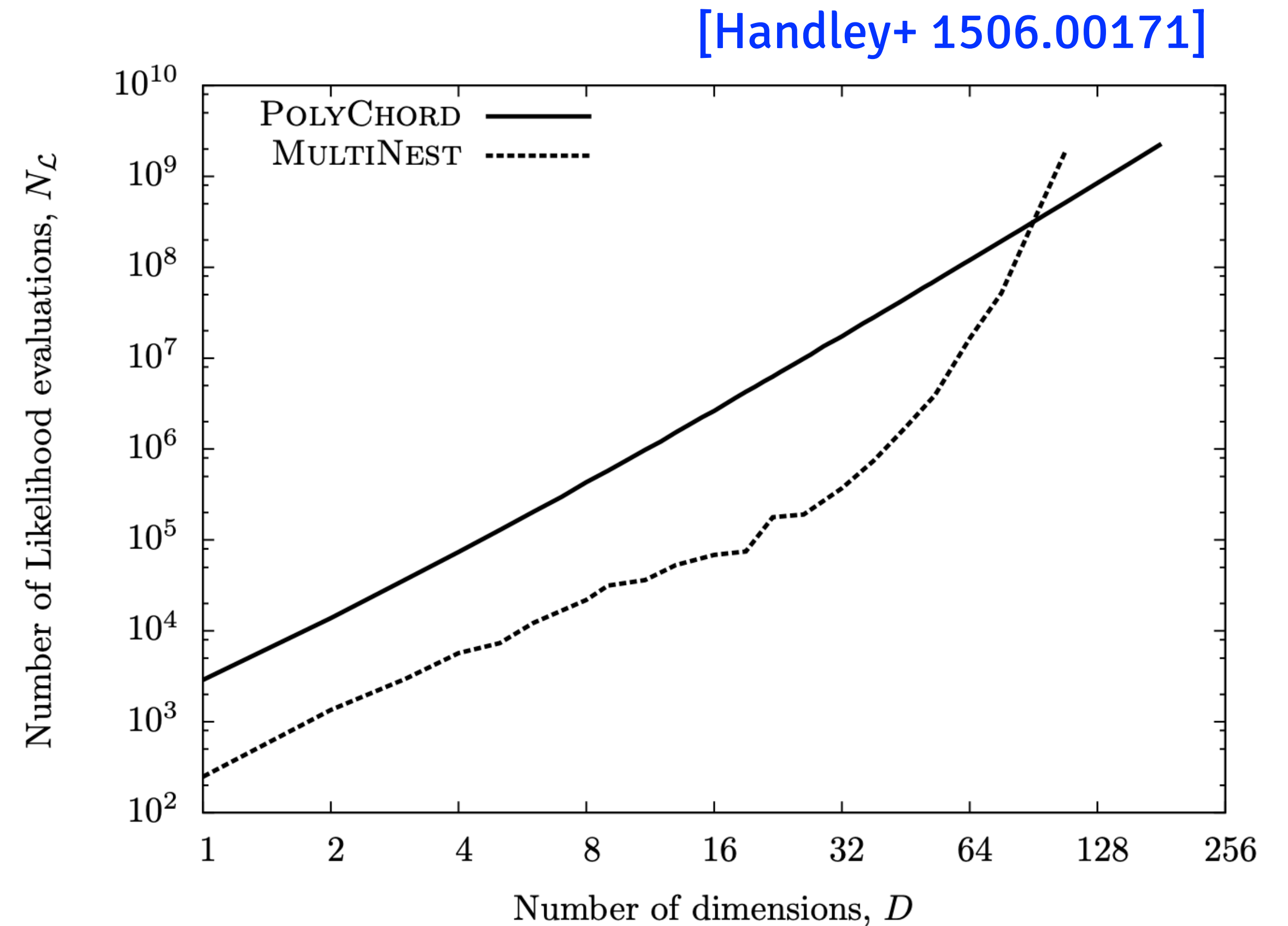


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For surveys like Euclid we expect  
 $\sim 50 - 100$  nuisance params!



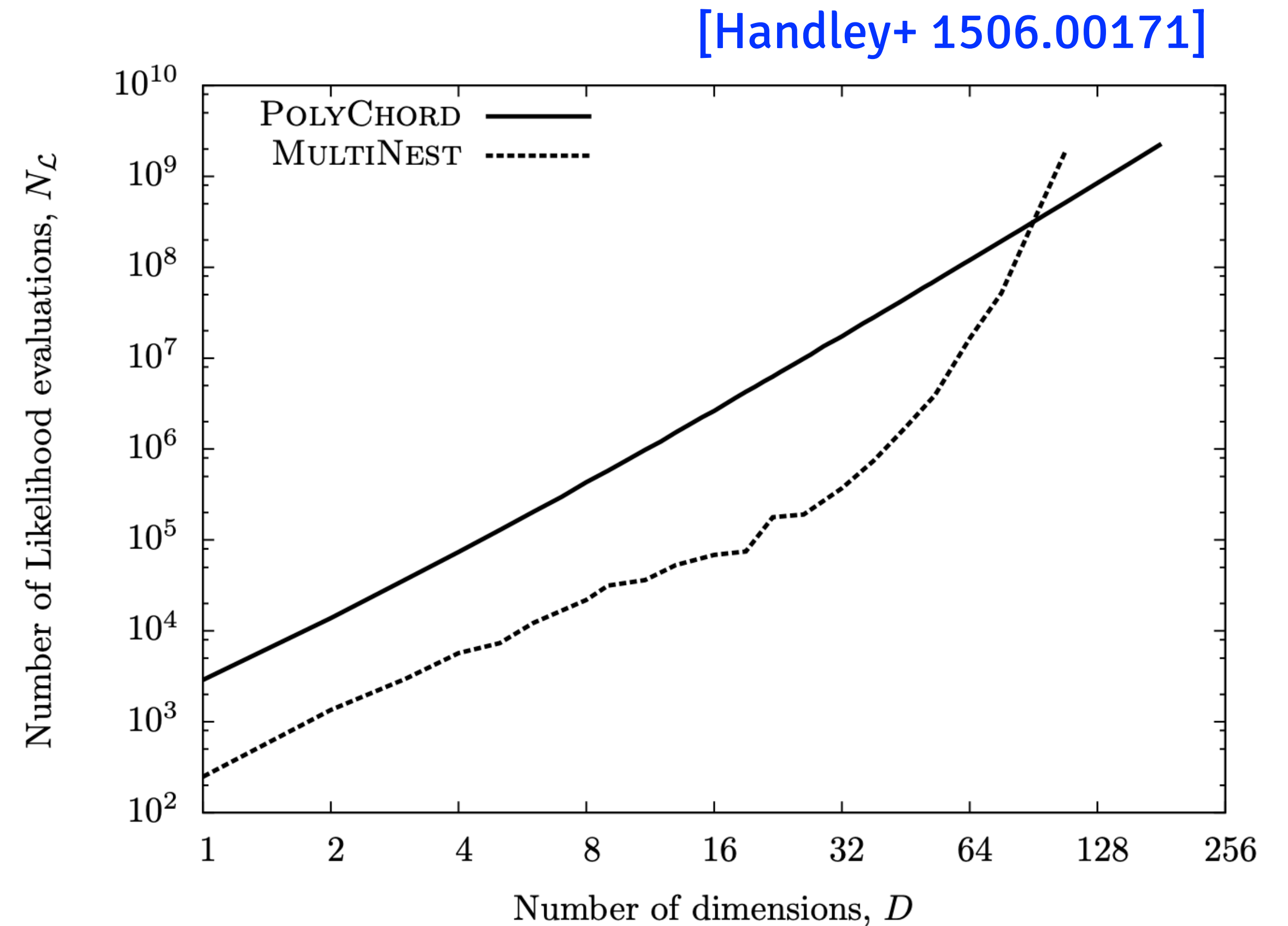
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- Often the full **likelihood** function is **intractable**



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(a.k.a. likelihood-free or implicit inference)

“Can we still do Bayesian inference if all we can do is simulate the data?”



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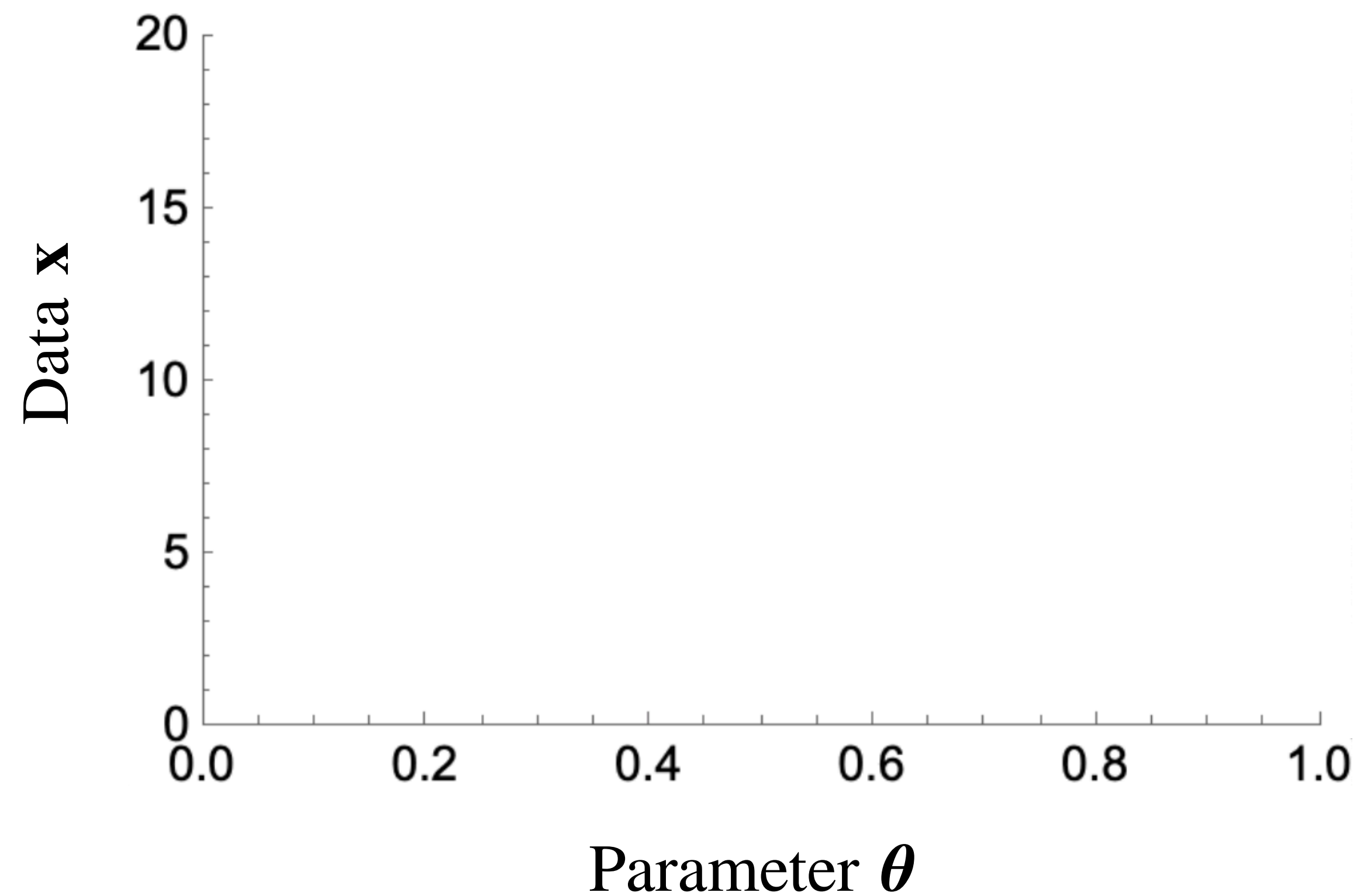
**Simulator** mapping from  
parameters  $\theta$  to data  $\mathbf{x}$



$\mathbf{x} \sim p(\mathbf{x} | \theta)$   
**(implicit likelihood)**

# Simulation-based inference (SBI)

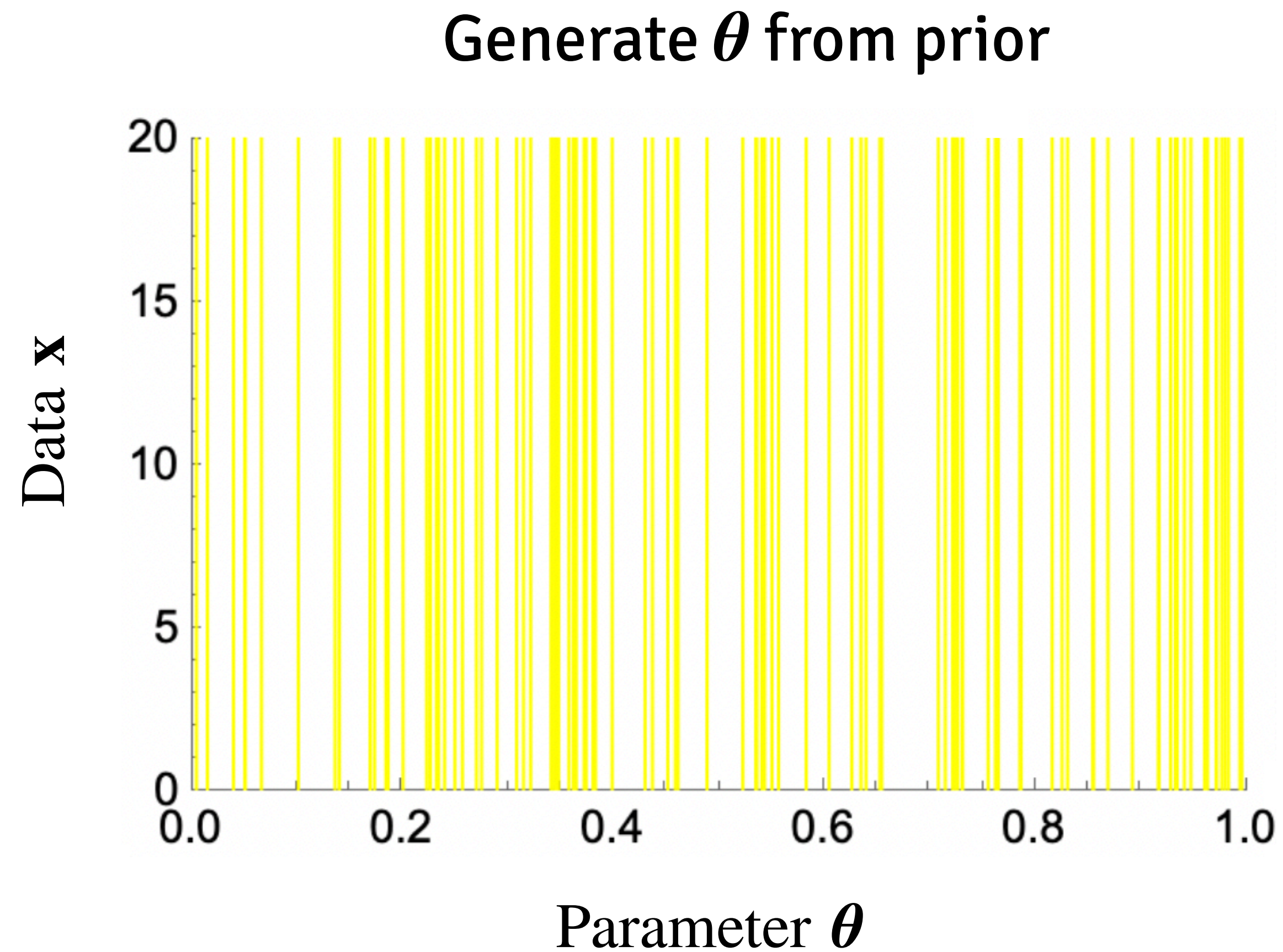
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[Credit: B. Wandelt]

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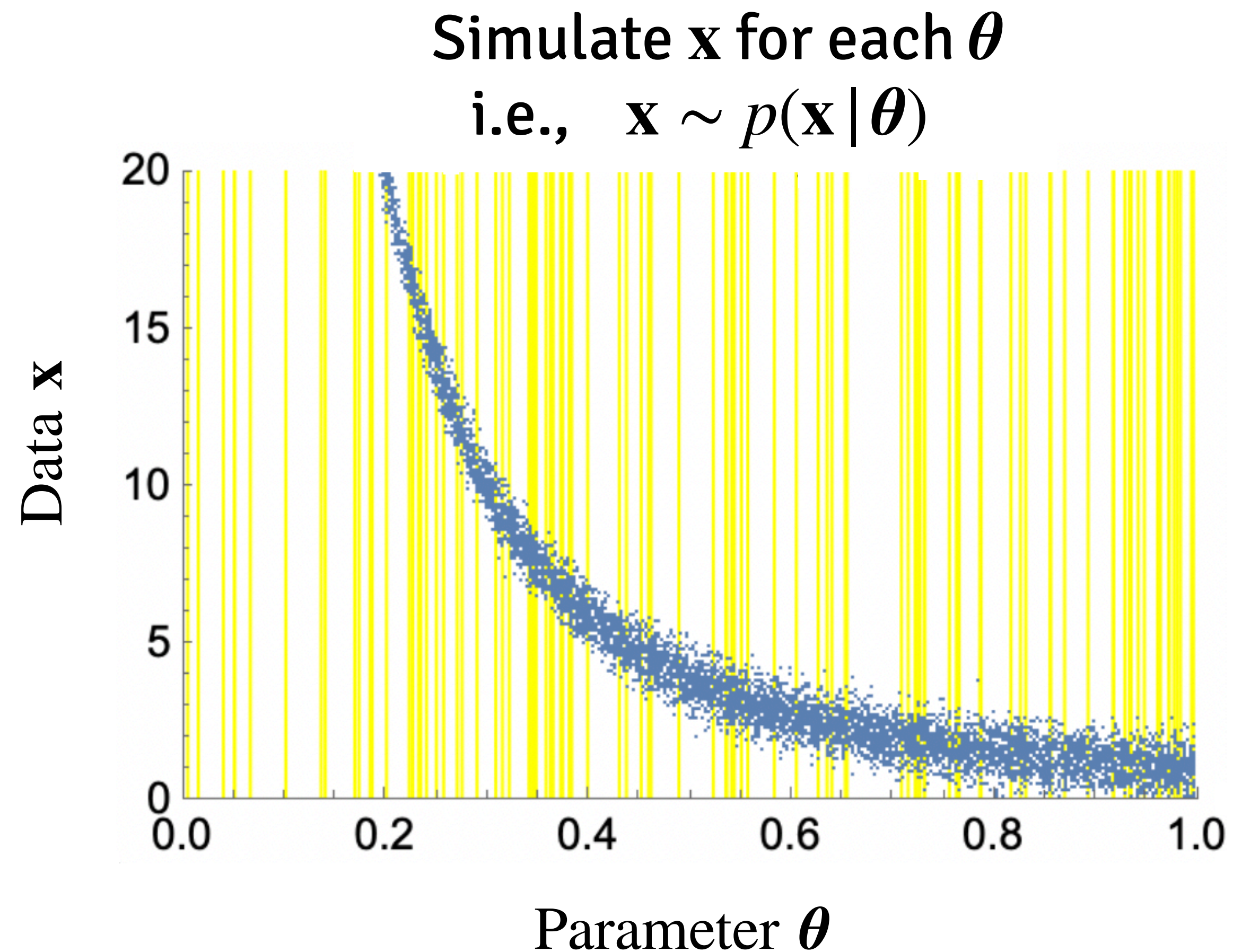


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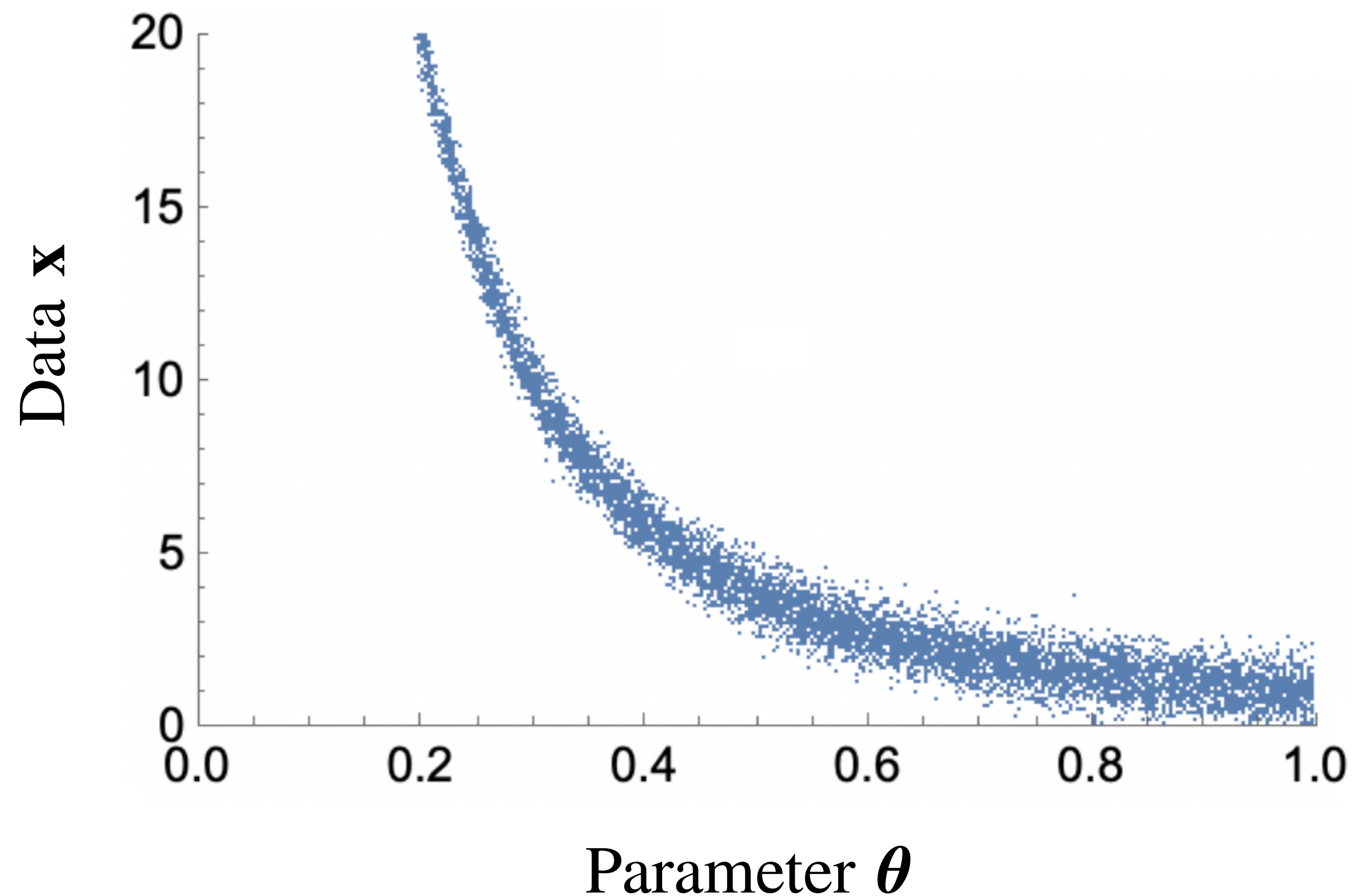


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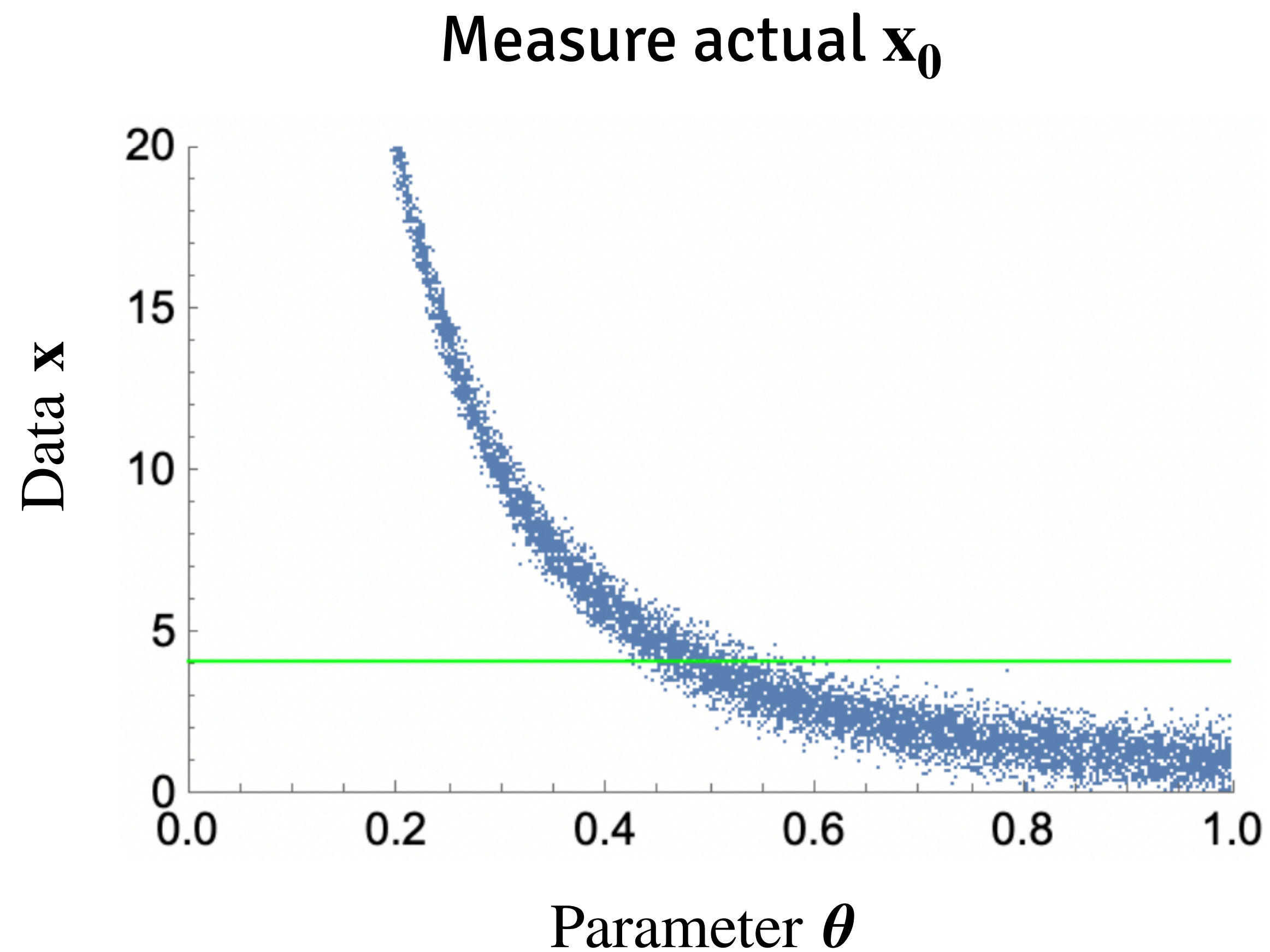


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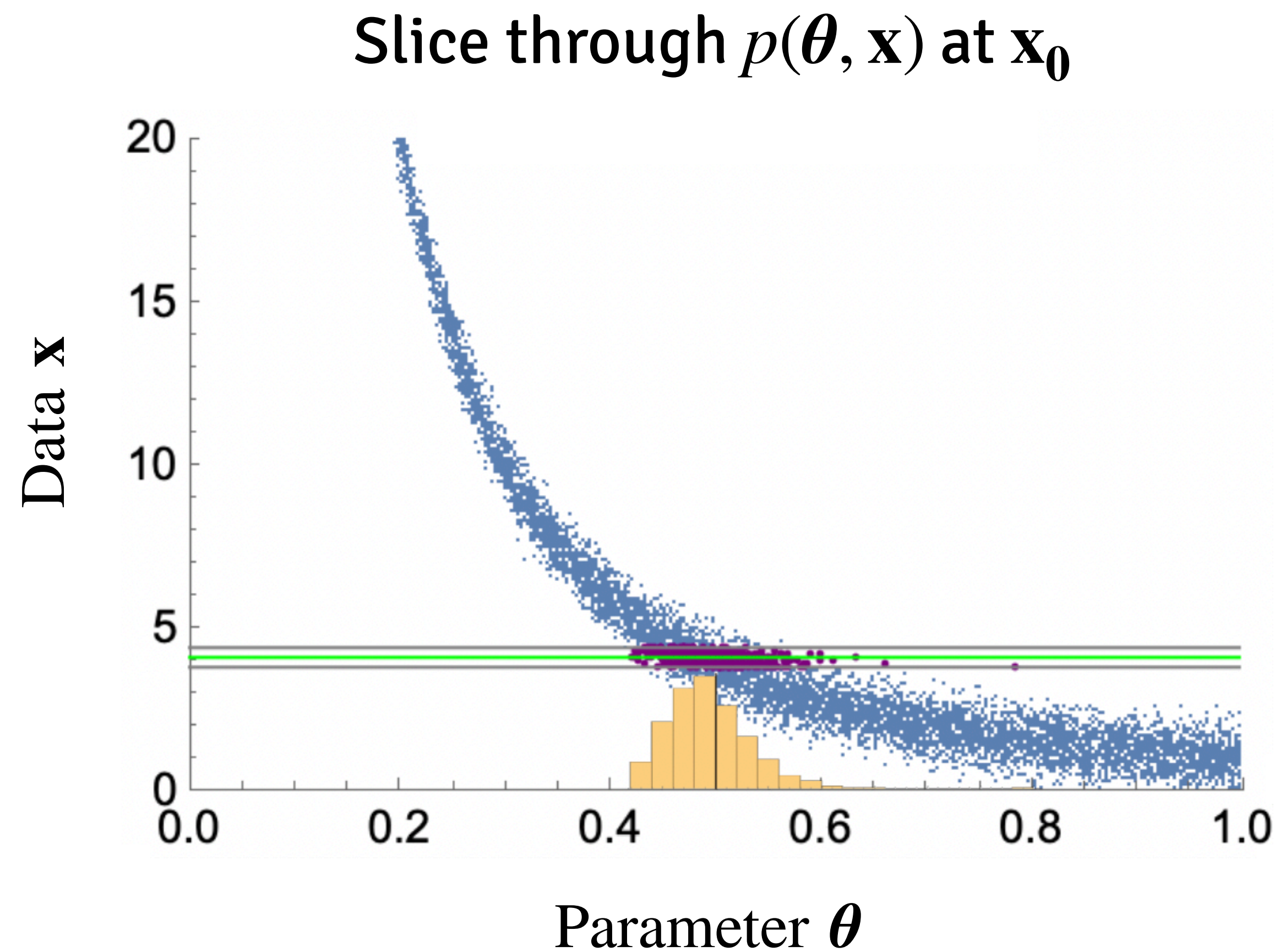


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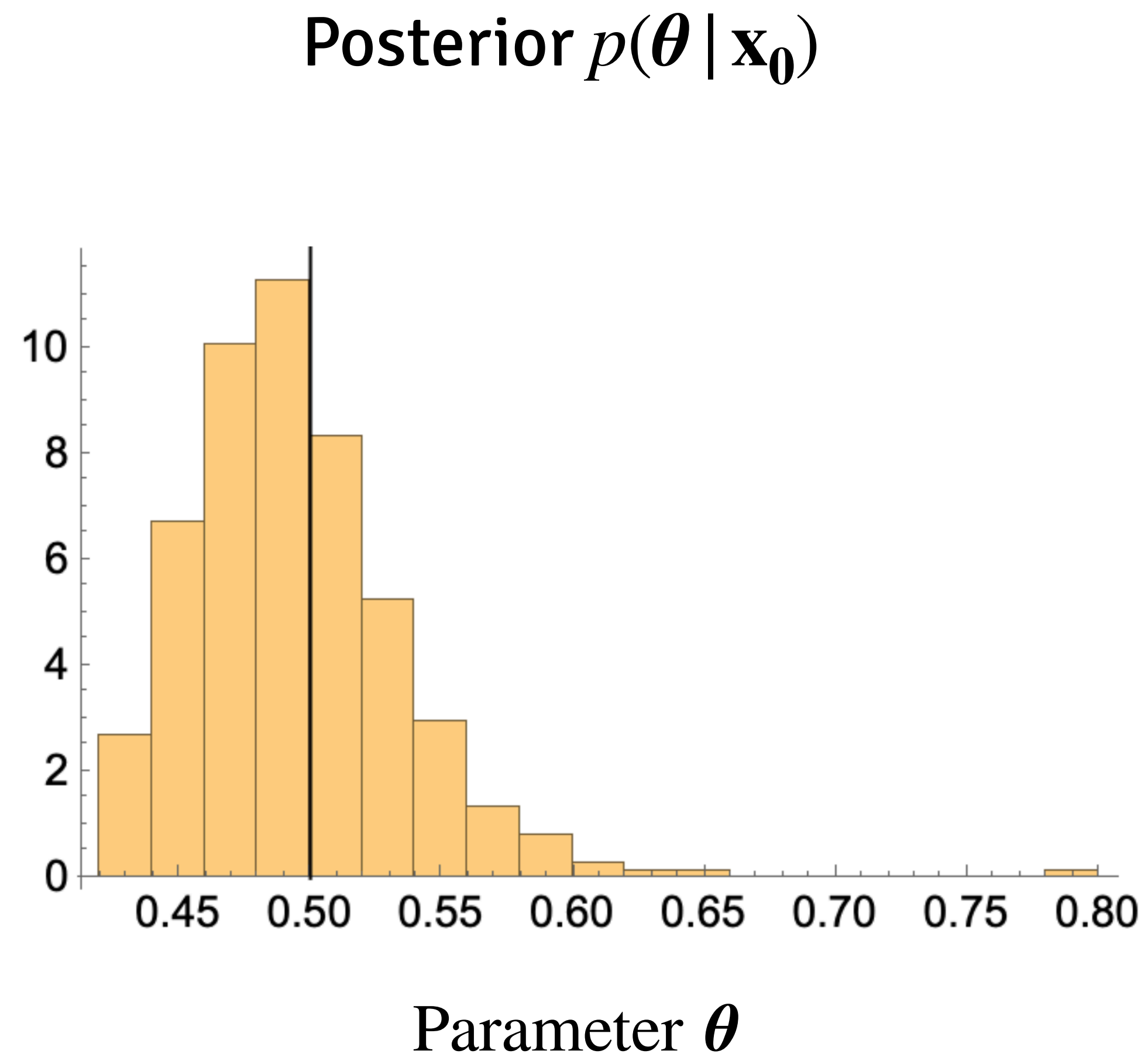
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# Usual steps in SBI

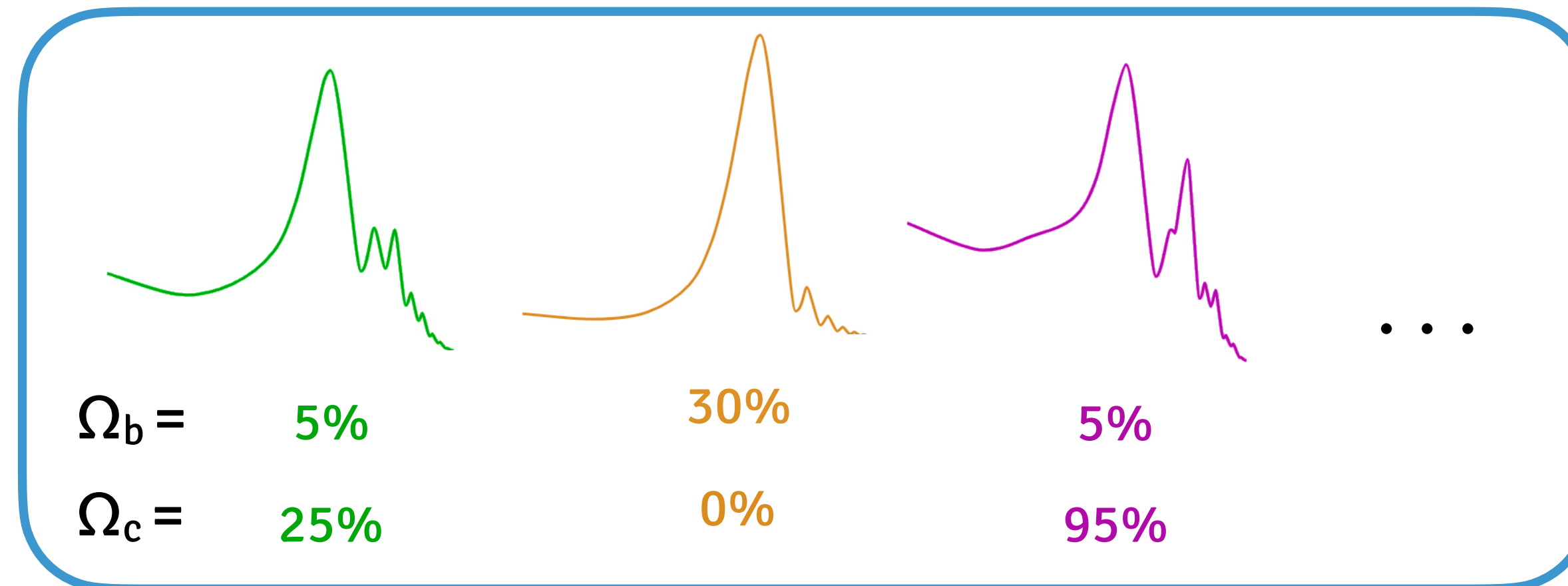
I. **Simulation:** get  $N$  samples  $\{(\mathbf{x}^{(1)}, \boldsymbol{\theta}^{(1)}), (\mathbf{x}^{(2)}, \boldsymbol{\theta}^{(2)}), \dots, (\mathbf{x}^{(N)}, \boldsymbol{\theta}^{(N)})\}$



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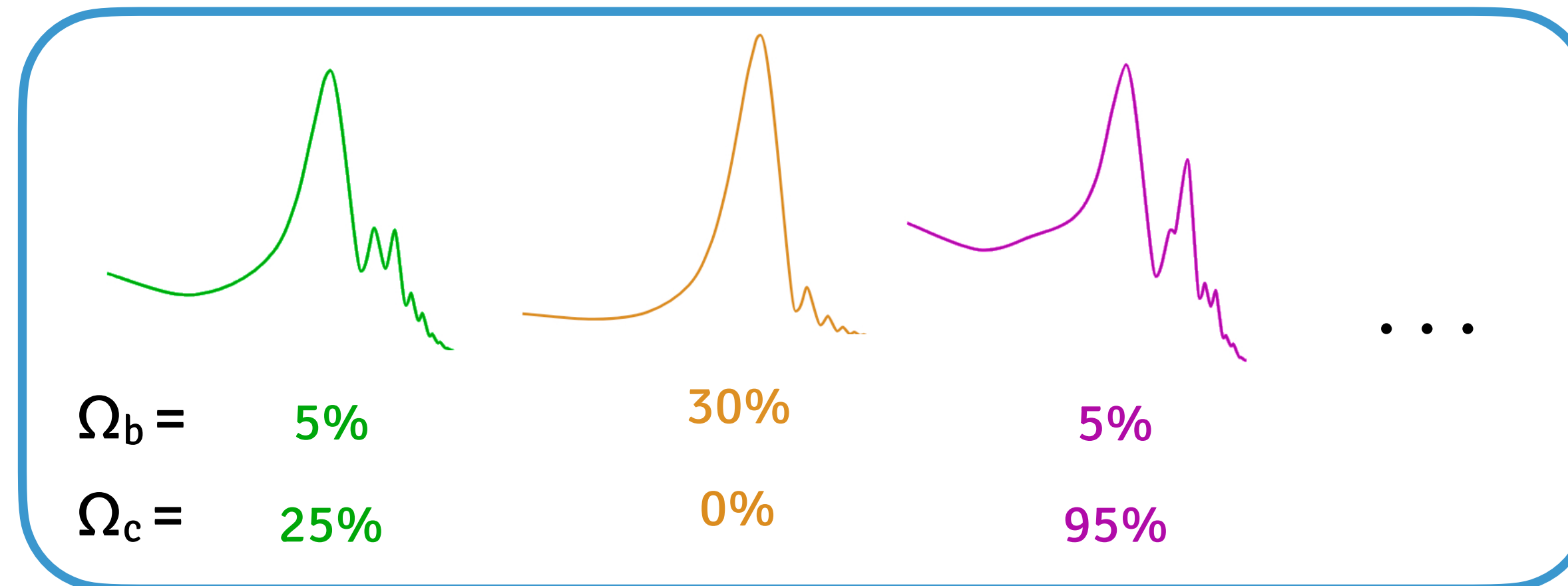
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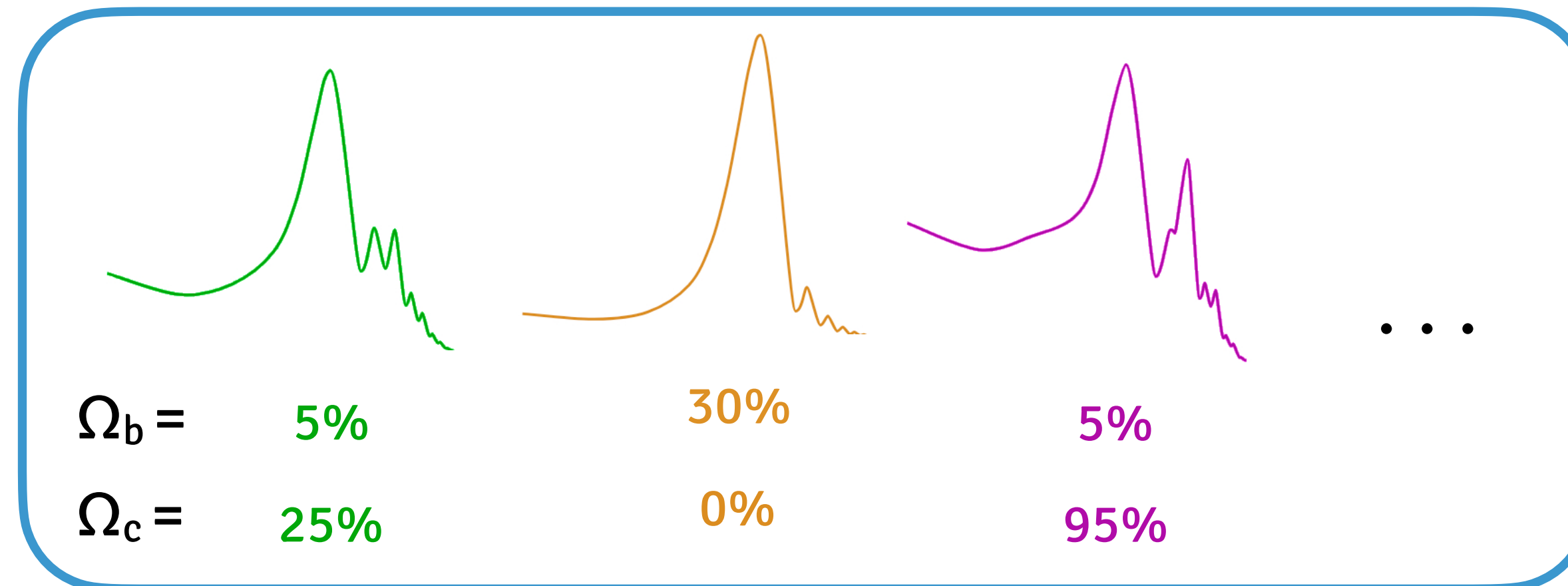


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Ex: CMB simulator



II. **Training:** train a NN to learn posterior  $f_{\phi}(\boldsymbol{\theta}, \mathbf{x}) \simeq p(\boldsymbol{\theta} | \mathbf{x})$

III. **Inference:** evaluate trained network at  $\mathbf{x} = \mathbf{x}_0$  to get  $p(\boldsymbol{\theta} | \mathbf{x}_0)$



SBI comes in many “flavors”:

Neural posterior estimation (**NPE**)  $\longrightarrow p(\theta | \mathbf{x})$

Neural likelihood estimation (**NLE**)  $\longrightarrow p(\mathbf{x} | \theta)$

Neural ratio estimation (**NRE**)  $\longrightarrow p(\theta | \mathbf{x})/p(\theta)$

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Neural ratio estimation (**NRE**)  $\longrightarrow p(\theta | \mathbf{x})/p(\theta)$

We focus on a recent algorithm:

**MNRE = Marginal Neural Ratio Estimation**

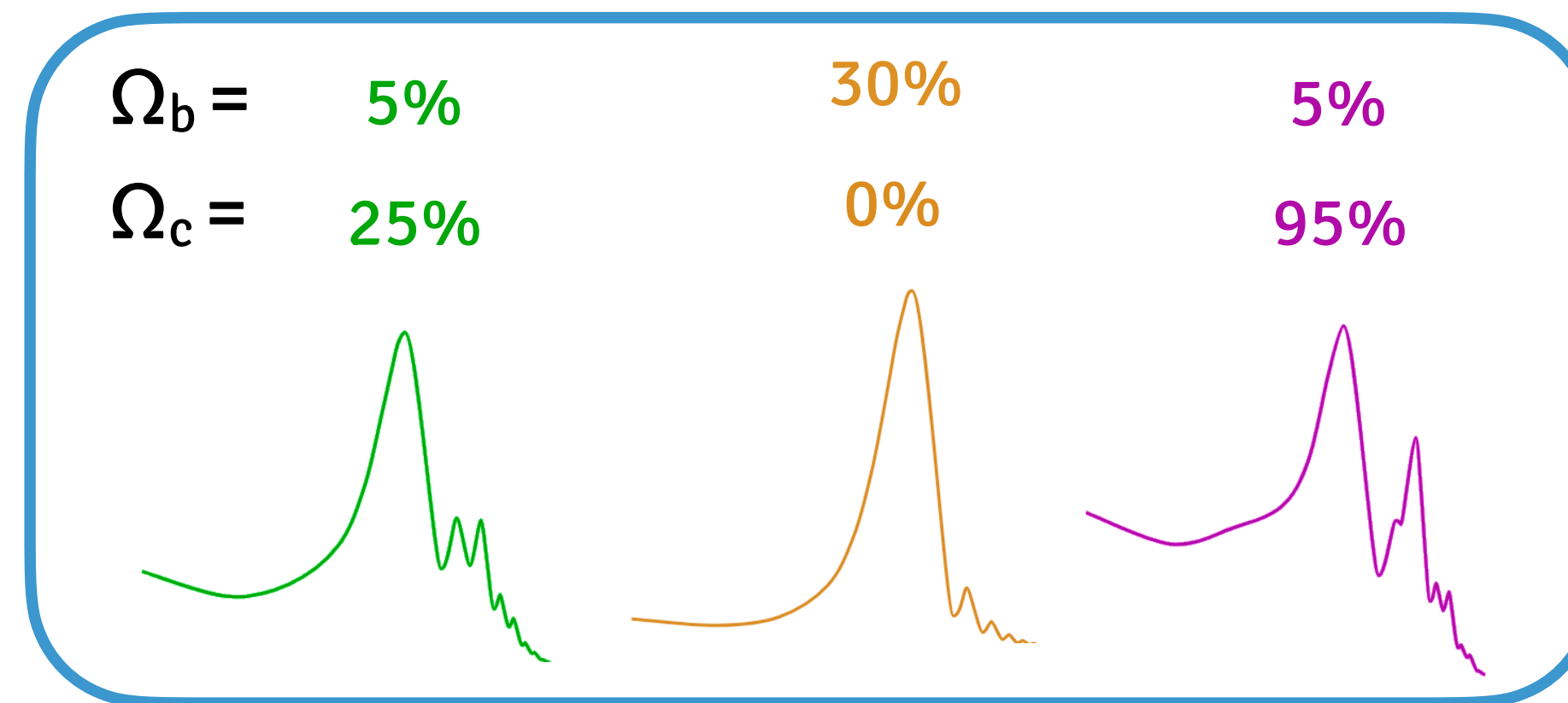
Implemented in Swyft [Miller et al. 2011.13951]

$$\frac{p(\mathbf{x}, \boldsymbol{\theta})}{p(\mathbf{x})p(\boldsymbol{\theta})} = \frac{p(\boldsymbol{\theta} | \mathbf{x})}{p(\boldsymbol{\theta})}$$

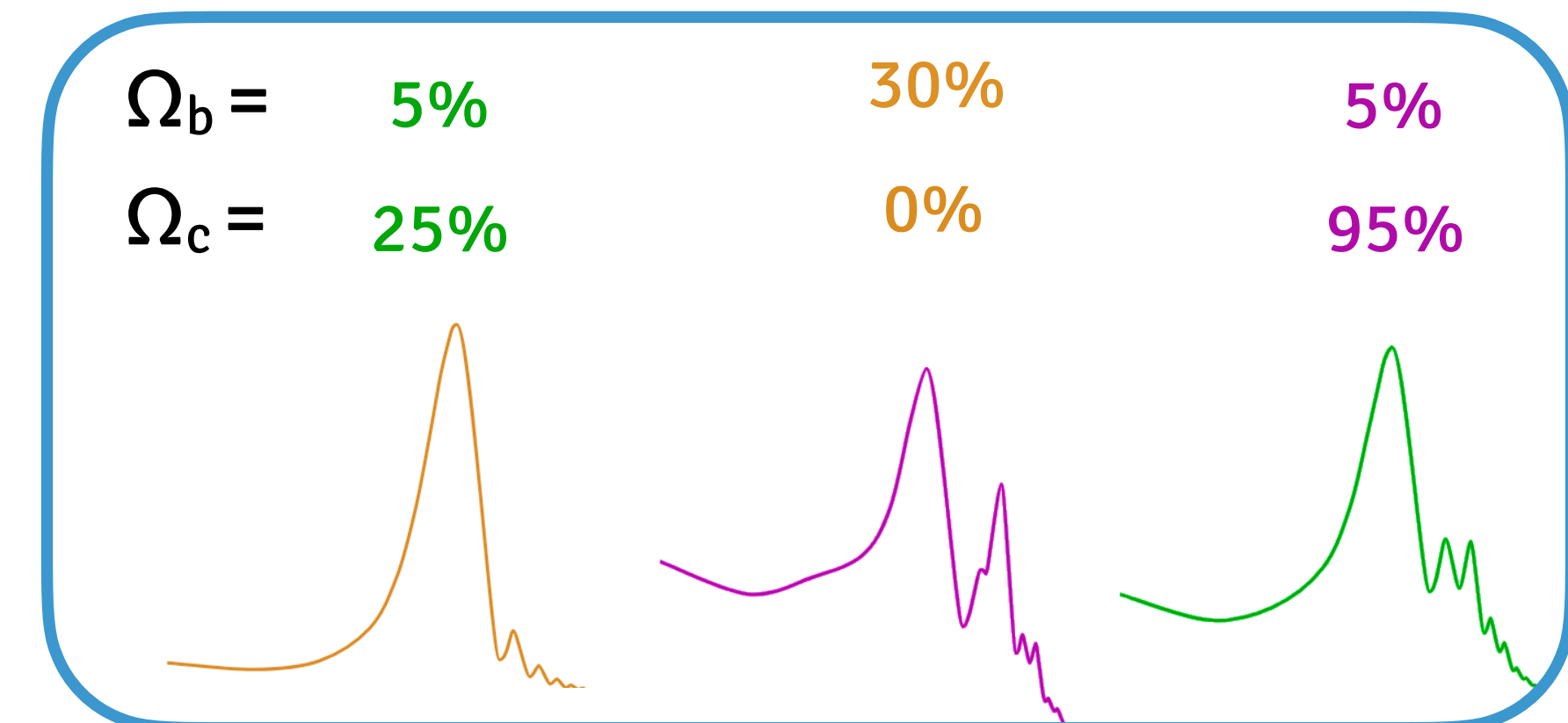
## MNRE in a nutshell

Train NNs to solve a **binary classification problem**:

$$(\mathbf{x}, \boldsymbol{\theta}) \sim p(\mathbf{x}, \boldsymbol{\theta})$$



$$(\mathbf{x}, \boldsymbol{\theta}) \sim p(\mathbf{x})p(\boldsymbol{\theta})$$



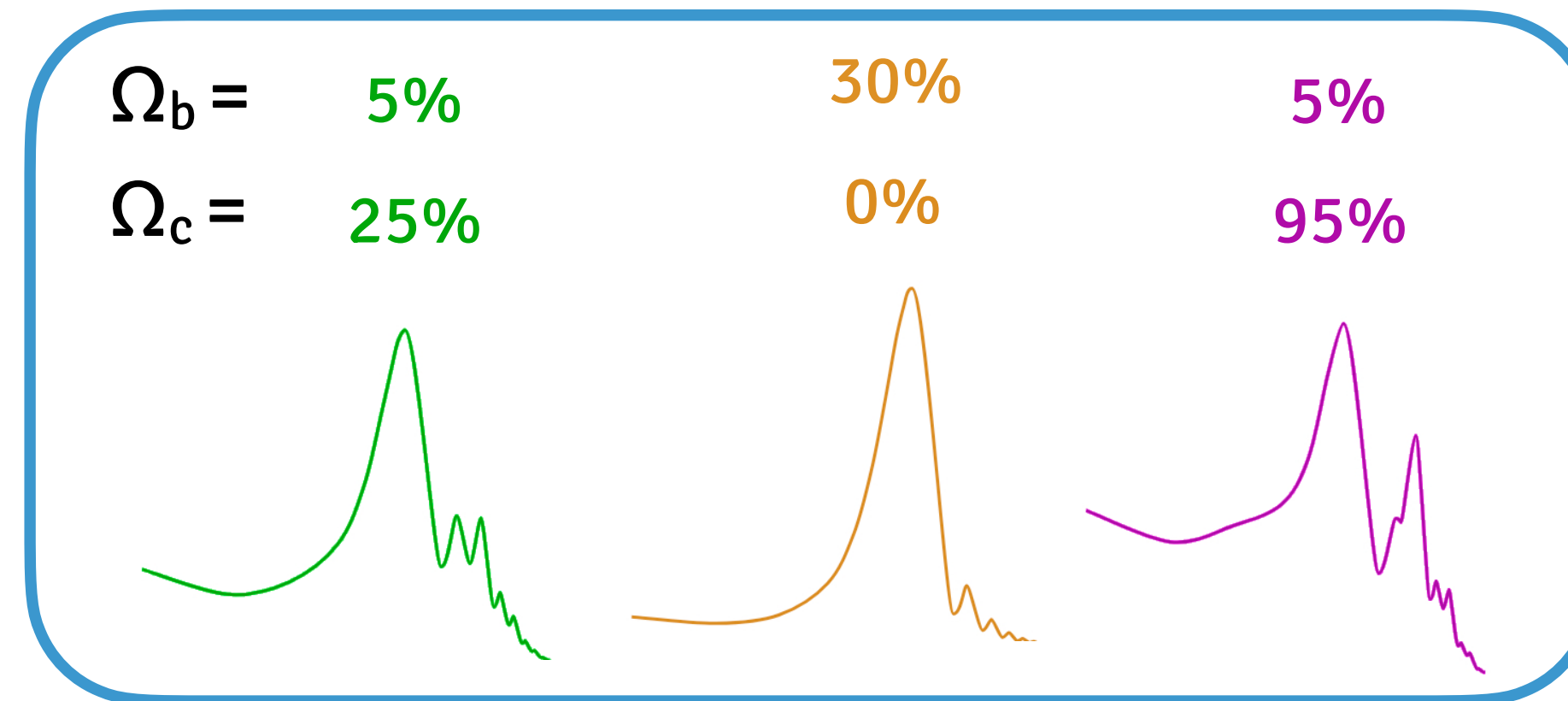
# Neural Ratio Estimation

$$\frac{p(\mathbf{x}, \boldsymbol{\theta})}{p(\mathbf{x})p(\boldsymbol{\theta})} = \frac{p(\boldsymbol{\theta} | \mathbf{x})}{p(\boldsymbol{\theta})}$$

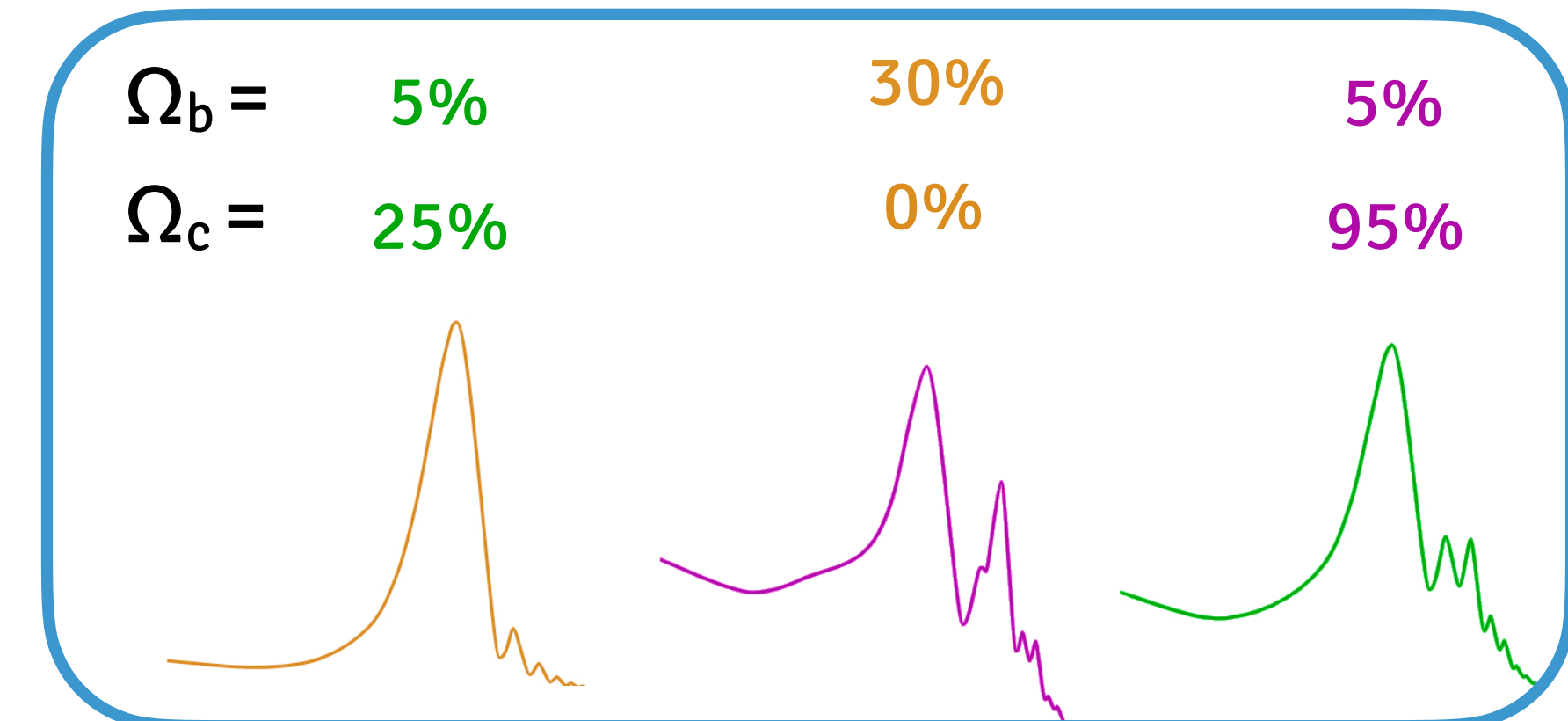
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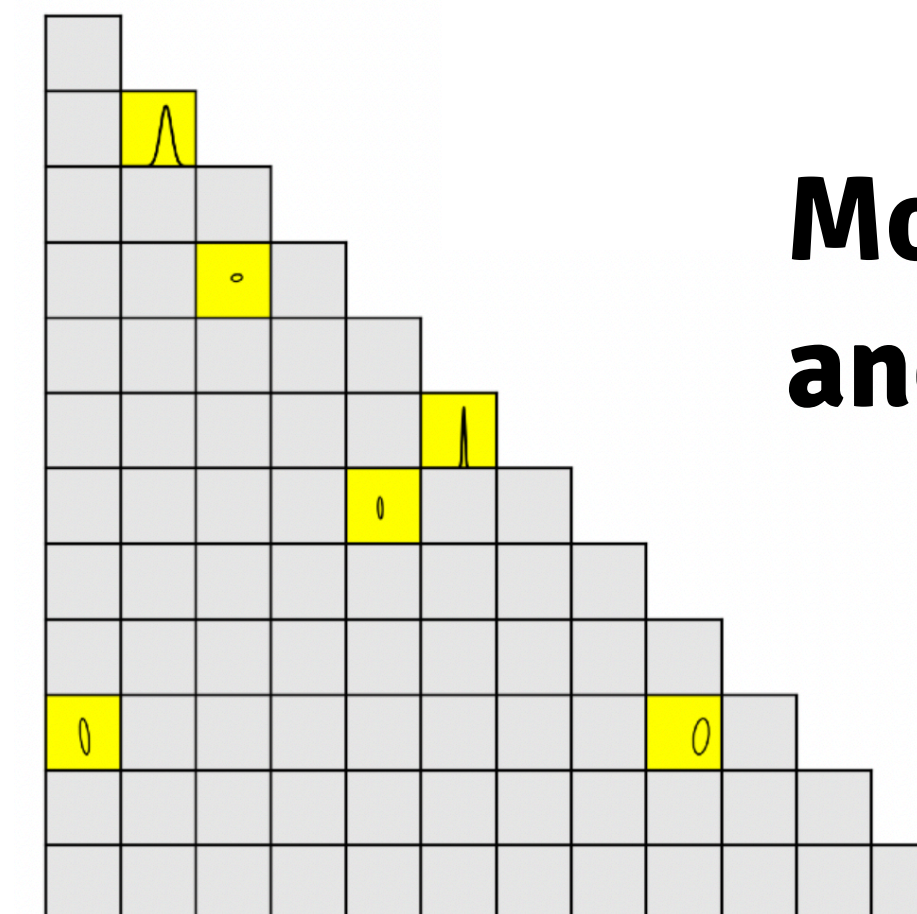


$$(\mathbf{x}, \boldsymbol{\theta}) \sim p(\mathbf{x})p(\boldsymbol{\theta})$$



## Focus on marginals

Instead of estimating all parameters, **cherry-pick** the ones we care about



**More flexible  
and efficient!**



SBI has already been applied to different LSS surveys:

 **BOSS** [[Lemos et al. 2310.15256](#)]

 **DES** [[Jeffrey et al. 2403.02314](#)]

 **KiDS** [[von Wietersheim-Kramsta et al. 2404.15402](#)]

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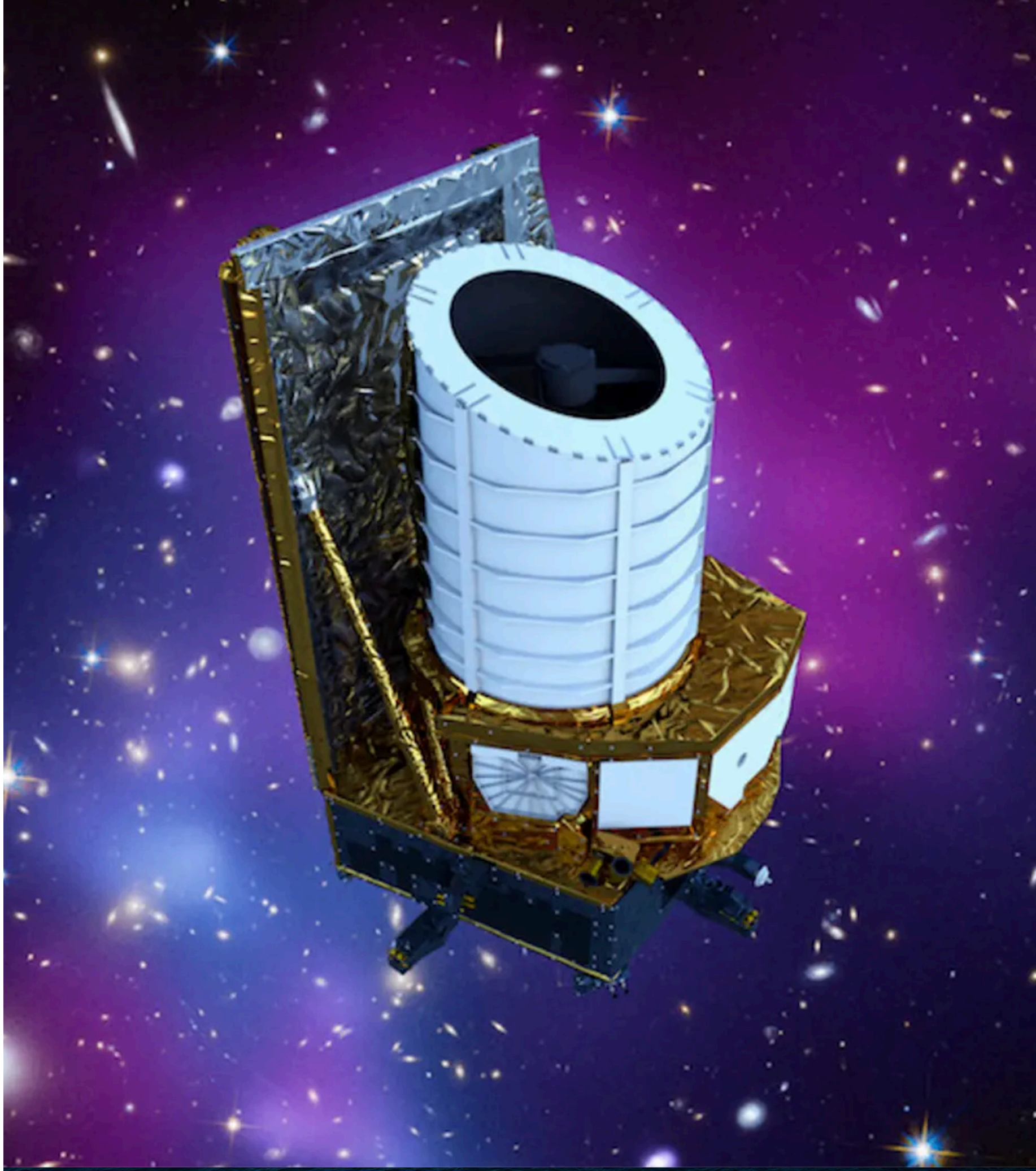
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**Our goal:** apply MNRE to **Euclid** photometric observables

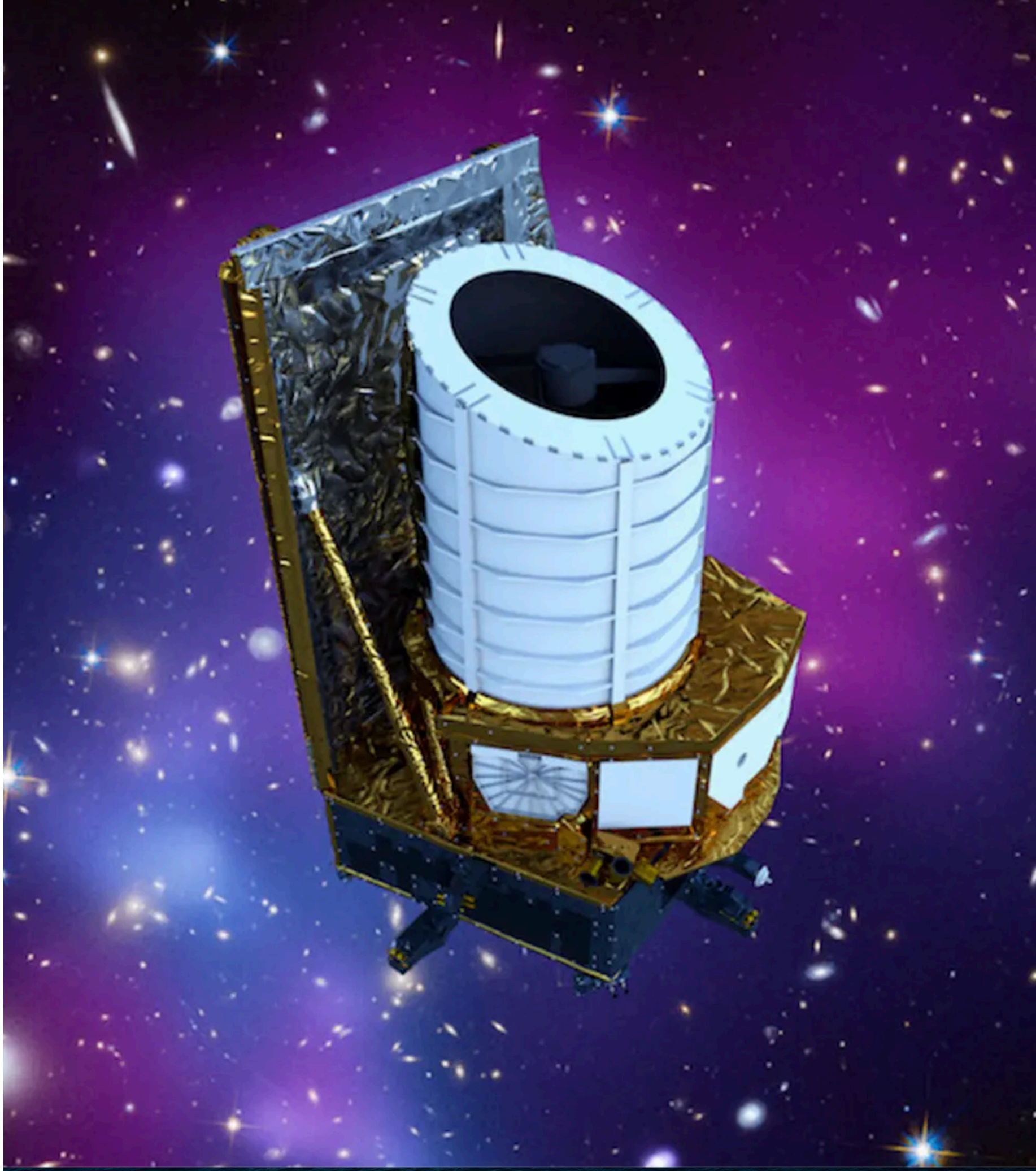
[ESA's Euclid space satellite]



On July 1<sup>st</sup> 2023, **Euclid** was launched to L2



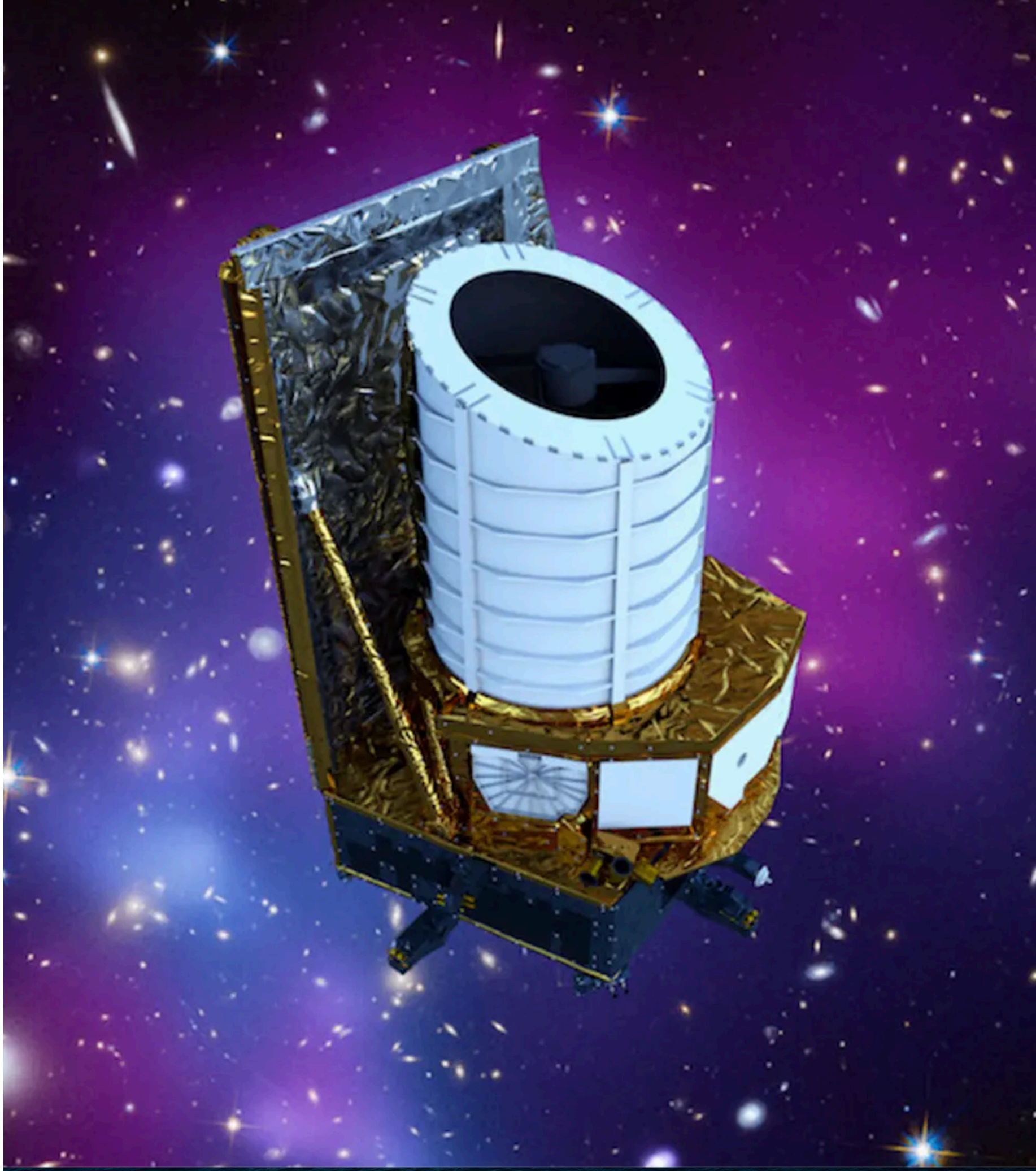
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- For 6 years, Euclid will measure the **shapes and redshifts of billions of galaxies**, across  $\sim 1/3$  of the sky



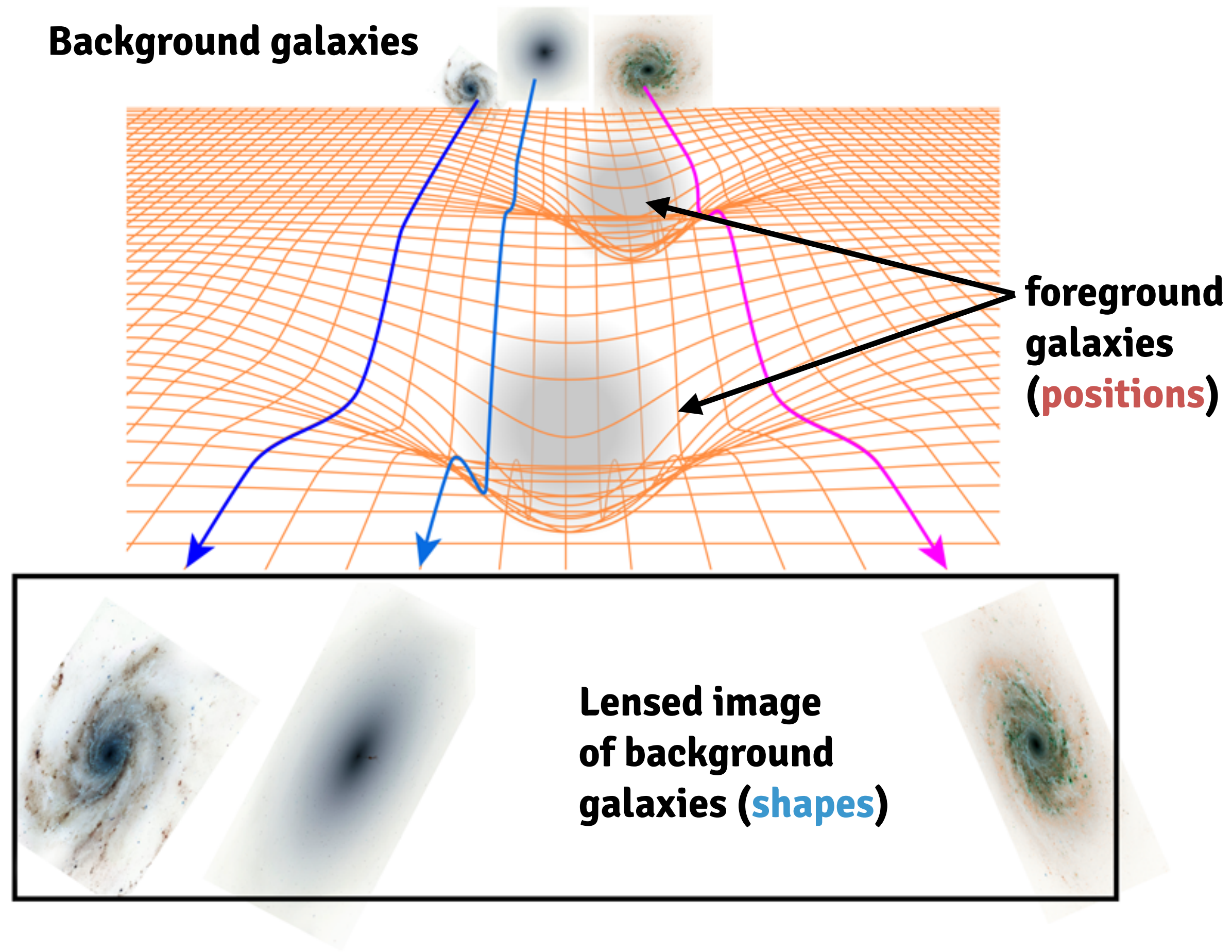
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- First **public data** release expected in **2026**



# Which are the Euclid primary observables?

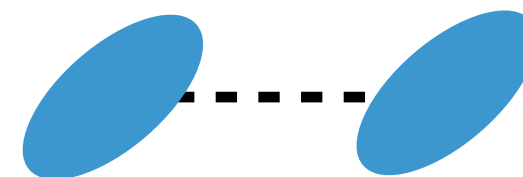


# 3x2pt photometric probes

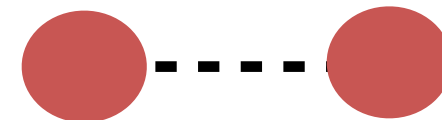
Summarise maps of galaxy **positions/shapes** using three 2-point statistics (**3x2pt**) measured at **10 tomographic redshift bins**



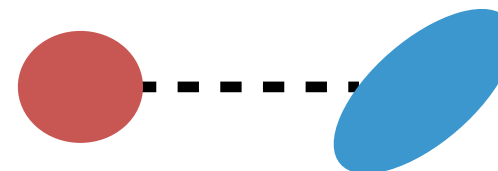
**Cosmic Shear**



**Galaxy clustering**

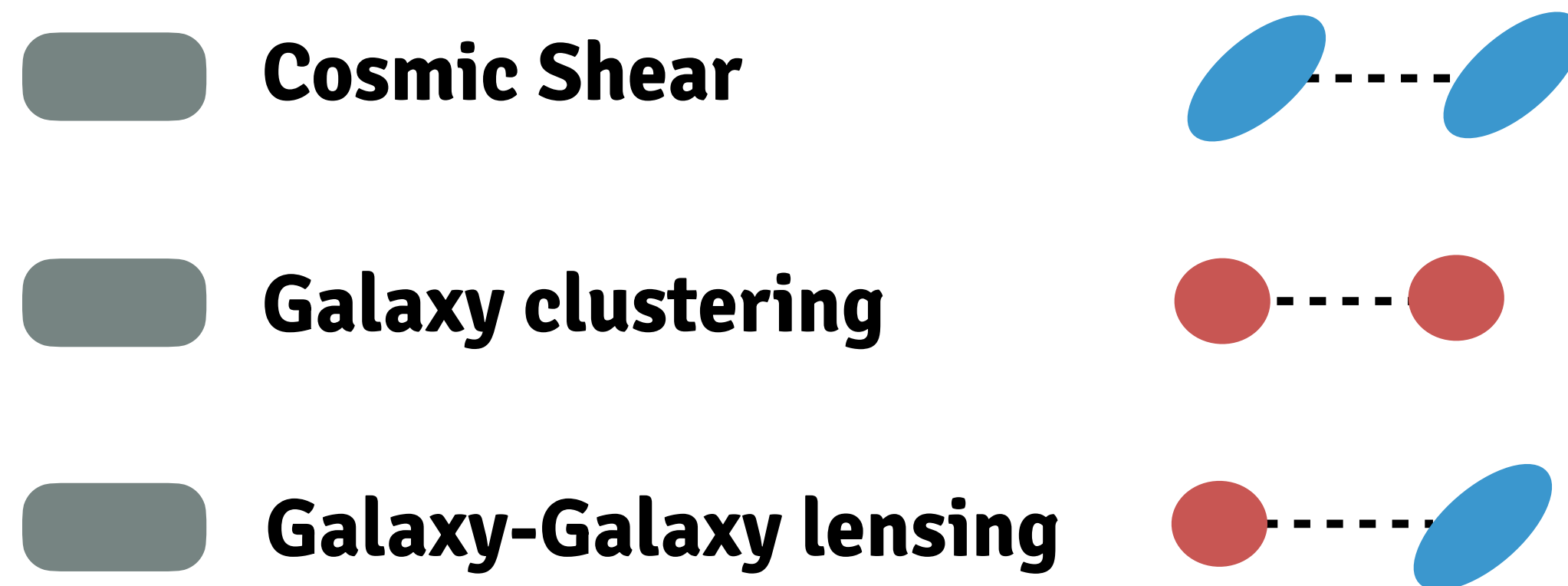


**Galaxy-Galaxy lensing**



# 3x2pt photometric probes

Summarise maps of galaxy **positions/shapes** using three 2-point statistics (**3x2pt**) measured at **10 tomographic redshift bins**




...described by angular **power spectra**  $C_{ij}^{XY}(\ell) = \int dz \, W_i^X(z) W_j^Y(z) P_m(k_\ell, z)$



# Swyft analysis of Euclid 3x2pt

## 1. Simulator:

We generate **50k realisations** of  
3x2pt spectra with gaussian noise

$$\hat{C}_{ij}^{AB}(\ell) = C_{ij}^{AB}(\ell) + n_{ij}^{AB}(\ell)$$


$\mathcal{N}(0, \mathbf{C})$

# Swyft analysis of Euclid 3x2pt

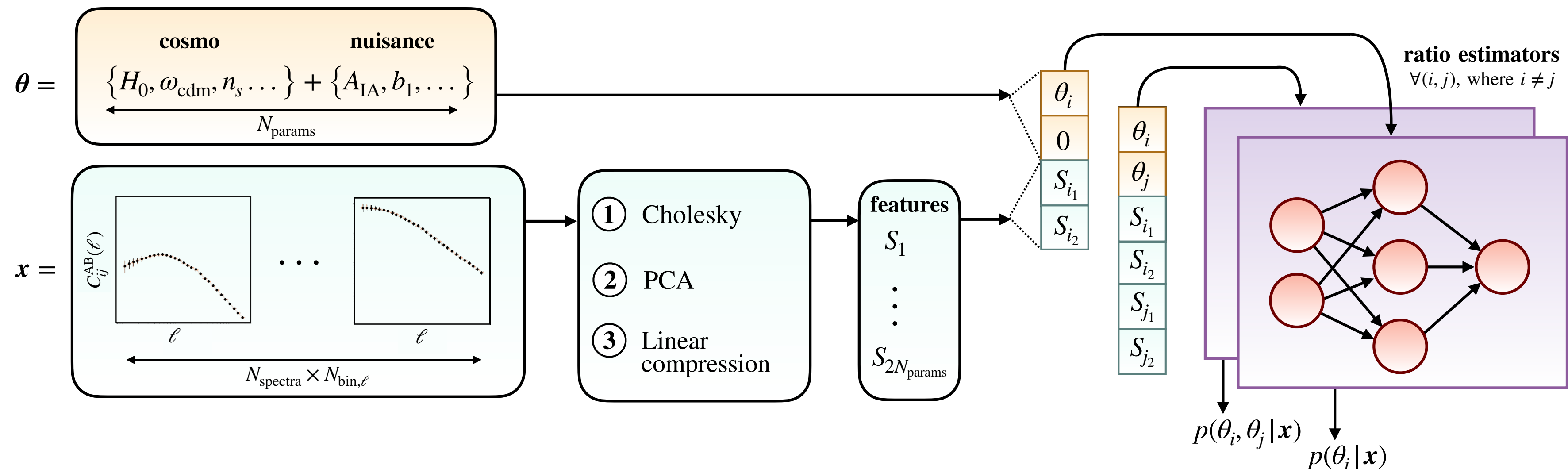
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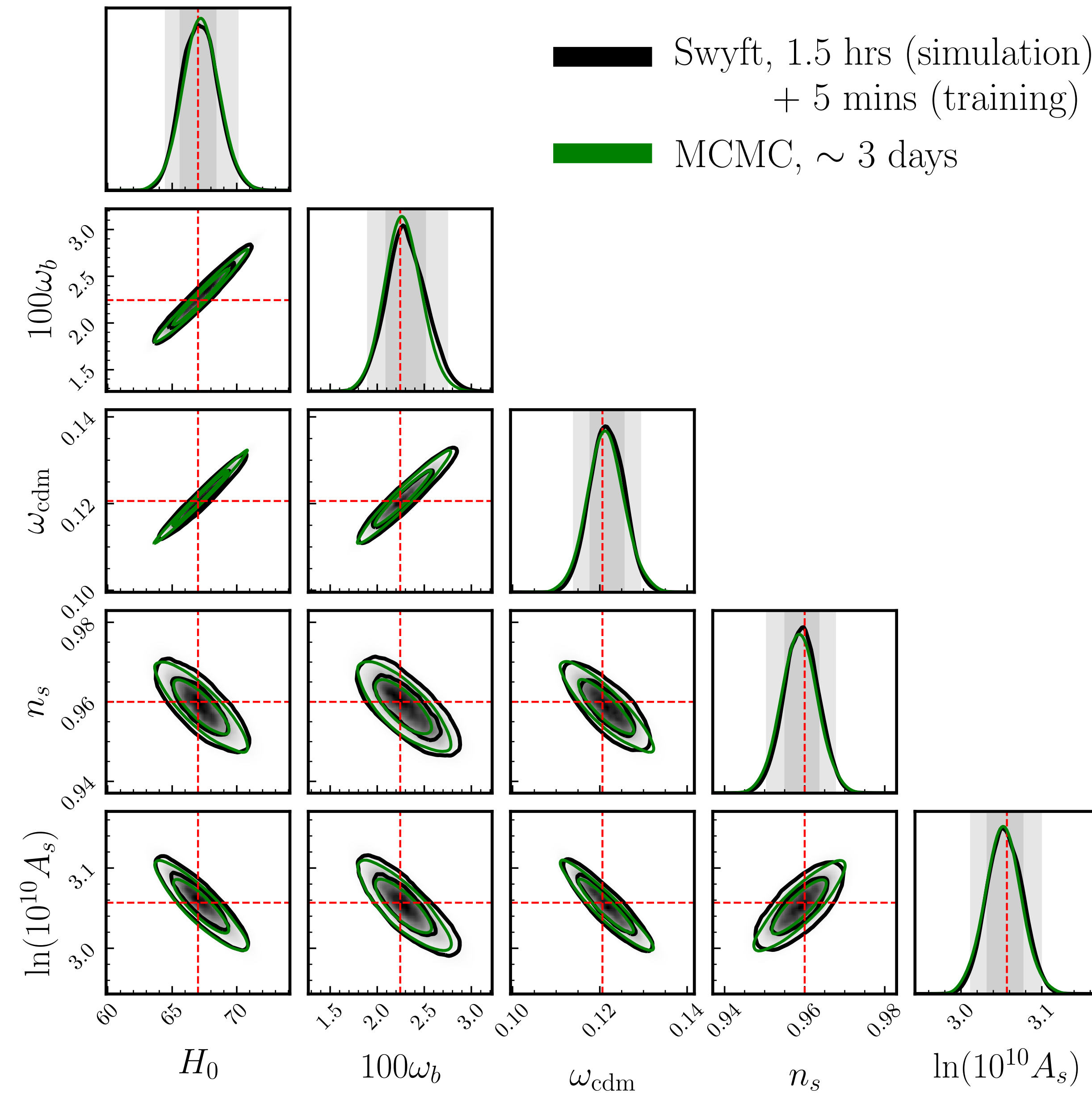
$$\hat{C}_{ij}^{AB}(\ell) = C_{ij}^{AB}(\ell) + n_{ij}^{AB}(\ell)$$

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## 2. Network: We pre-compress spectra into features



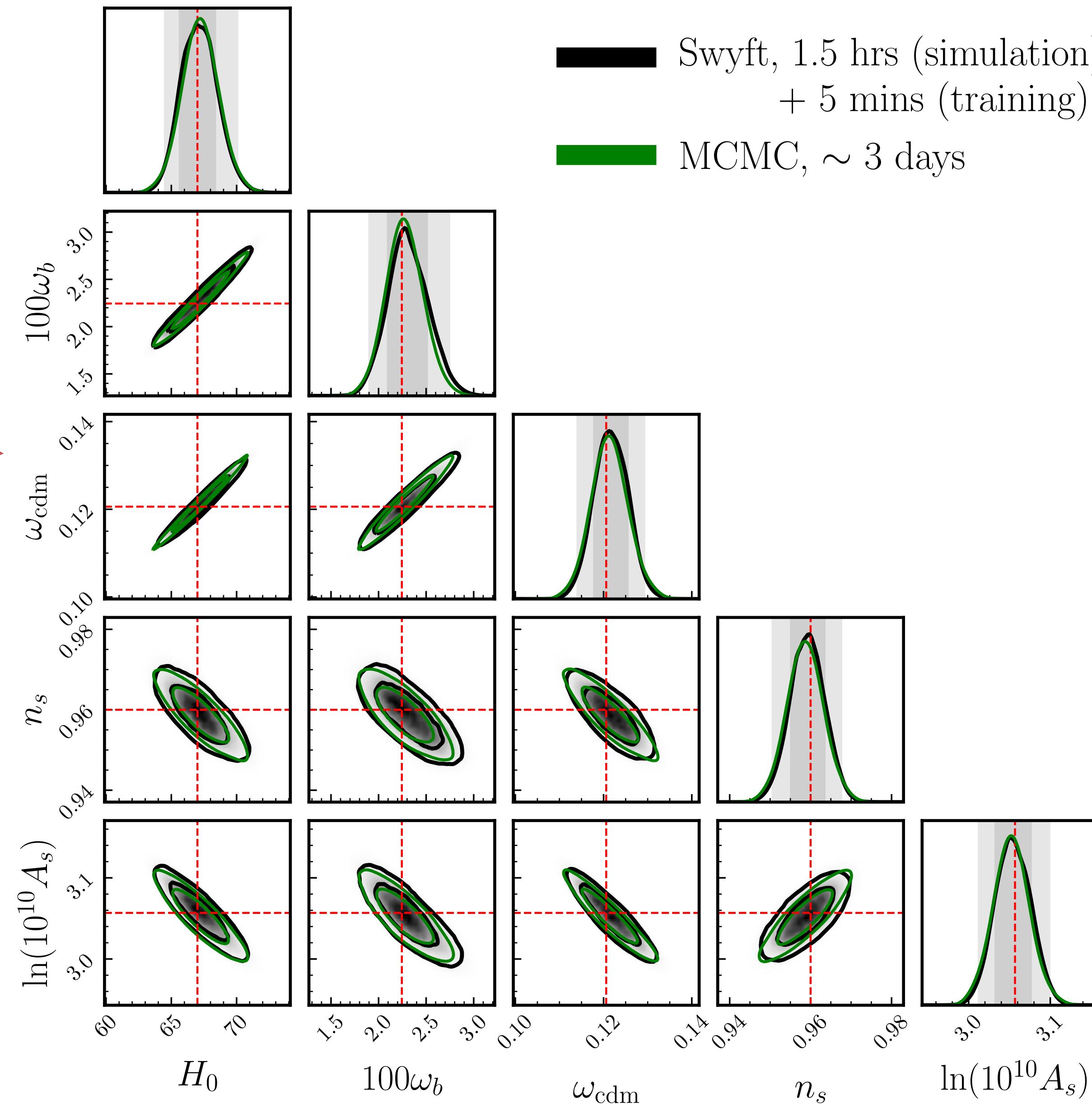
# Forecast $\Lambda$ CDM posteriors





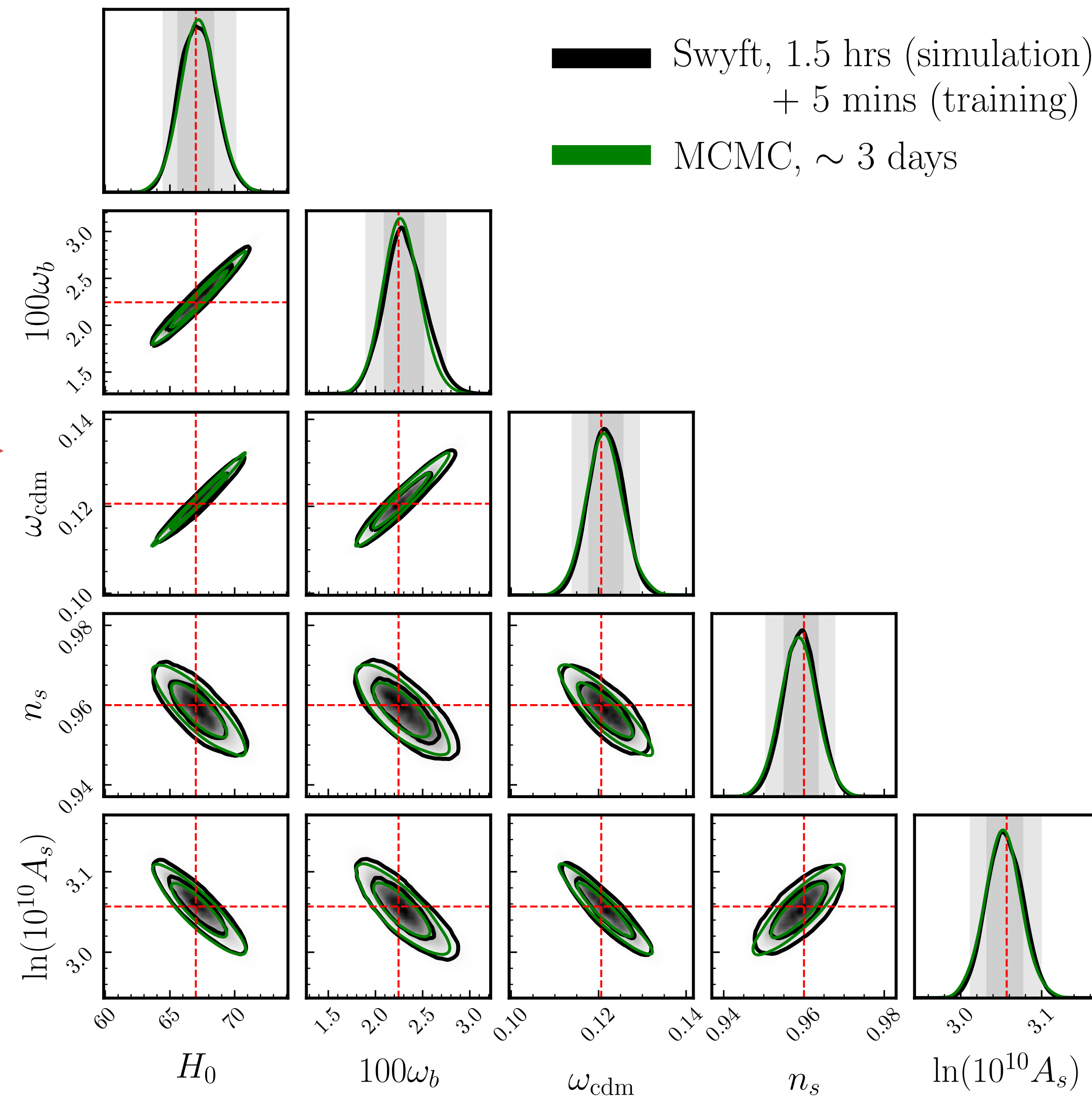
# Forecast $\Lambda$ CDM posteriors

— Swyft, 1.5 hrs (simulation)  
+ 5 mins (training)  
— MCMC,  $\sim 3$  days



MNRE & MCMC are in excellent agreement!

# Forecast $\Lambda$ CDM posteriors



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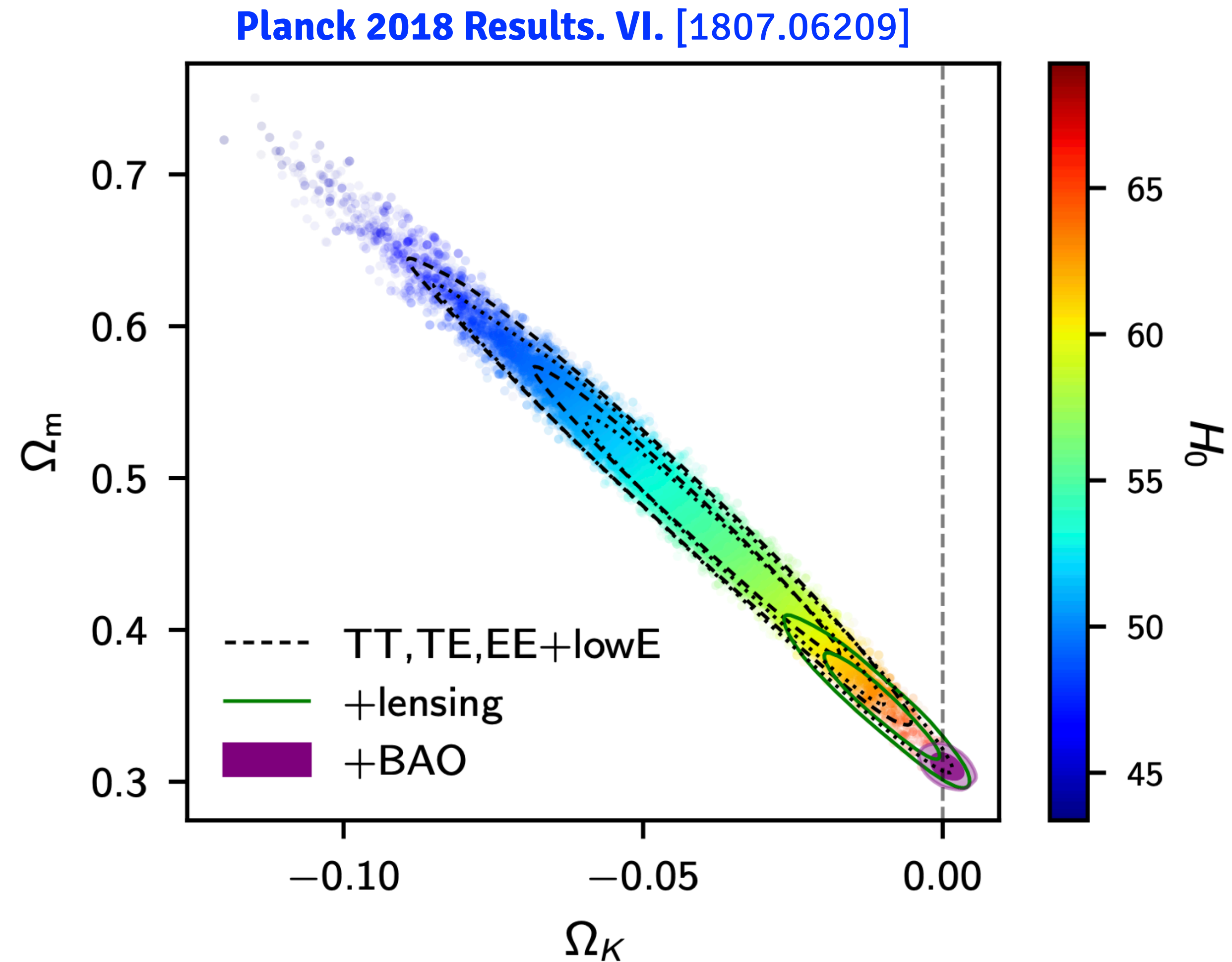
Dramatic reduction in CPU time!

**What about combining different cosmological probes?**

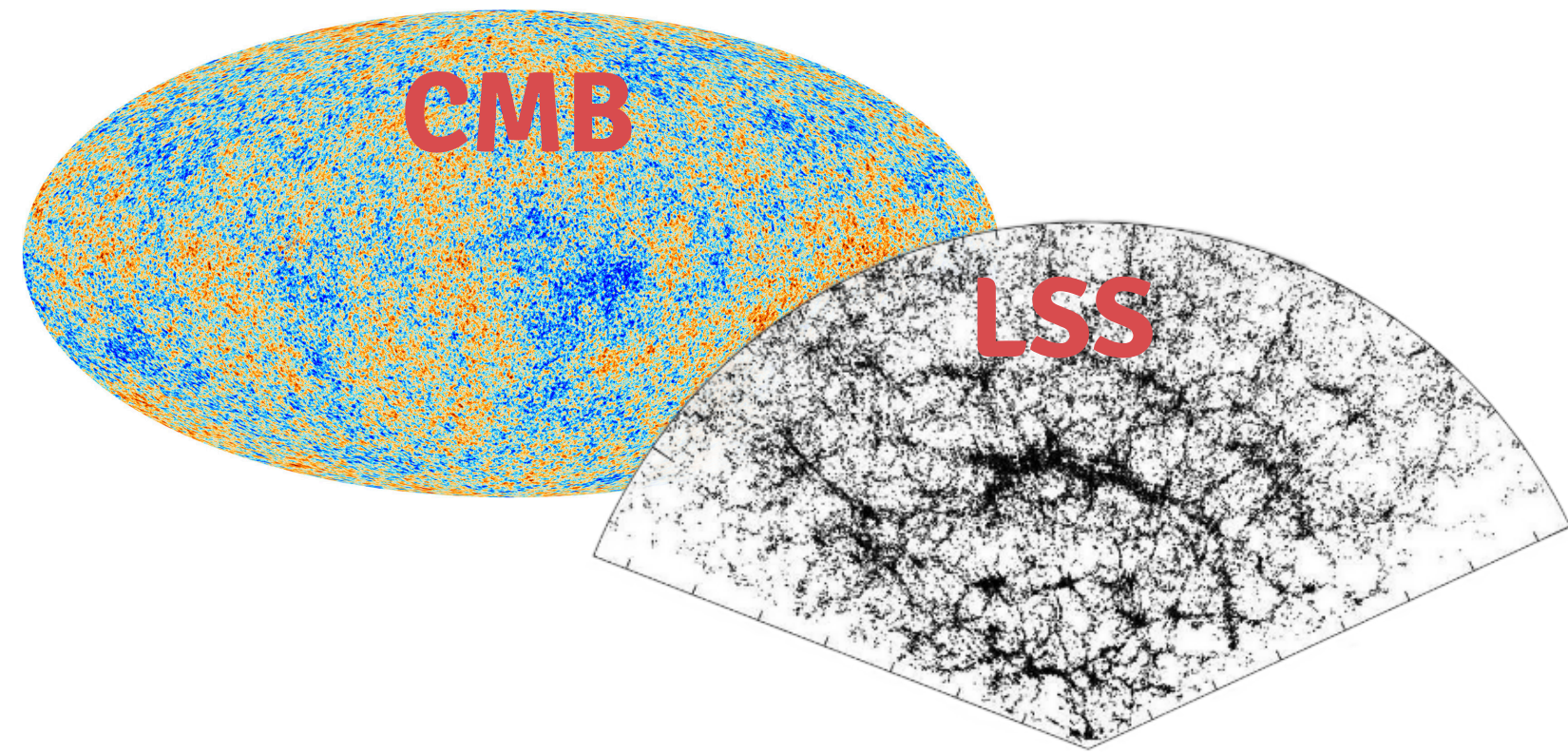


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**Canonical example:**



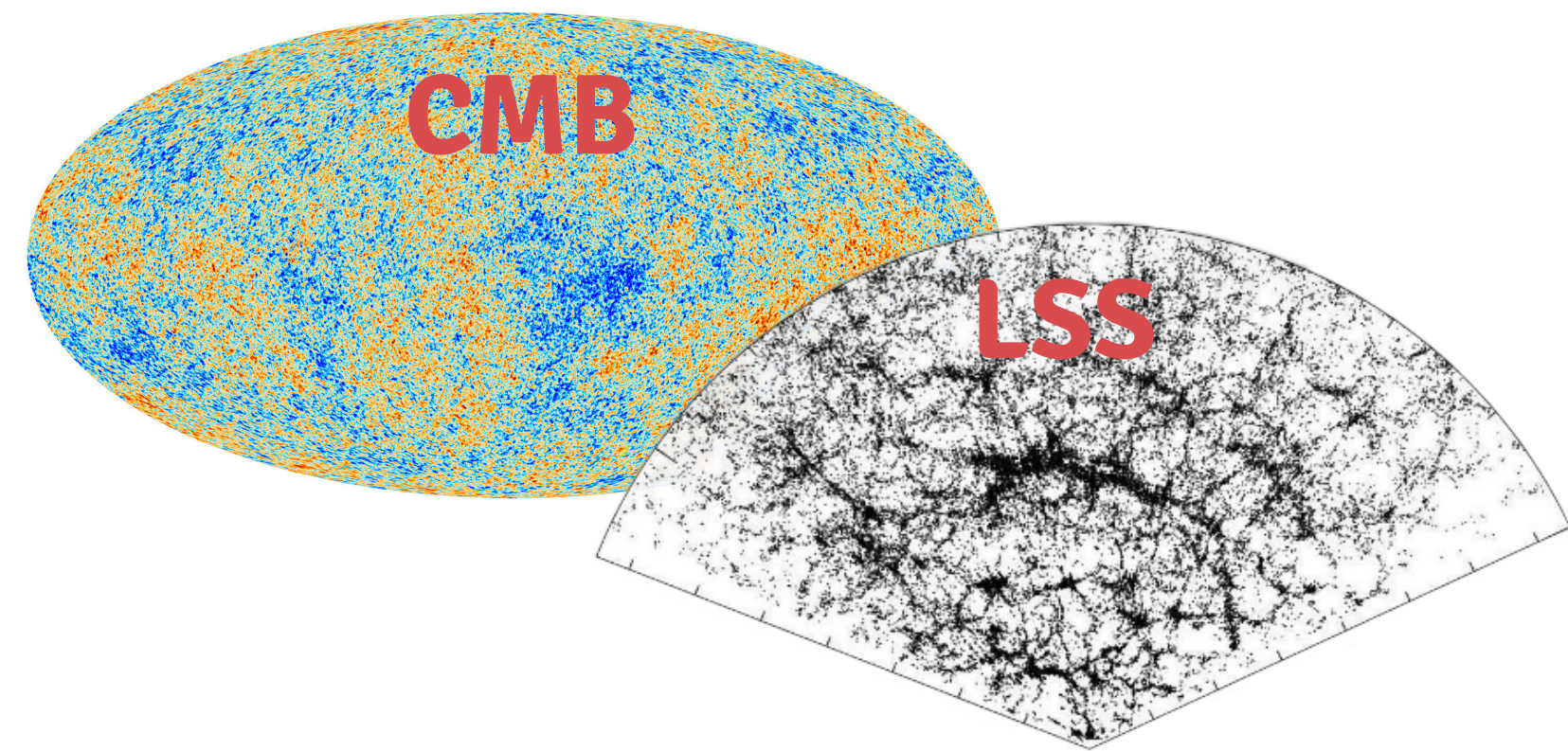
# Joint analyses of CMB & LSS



Very **complementary**  
(high- $z$  vs. low- $z$ , linear vs. non-linear)



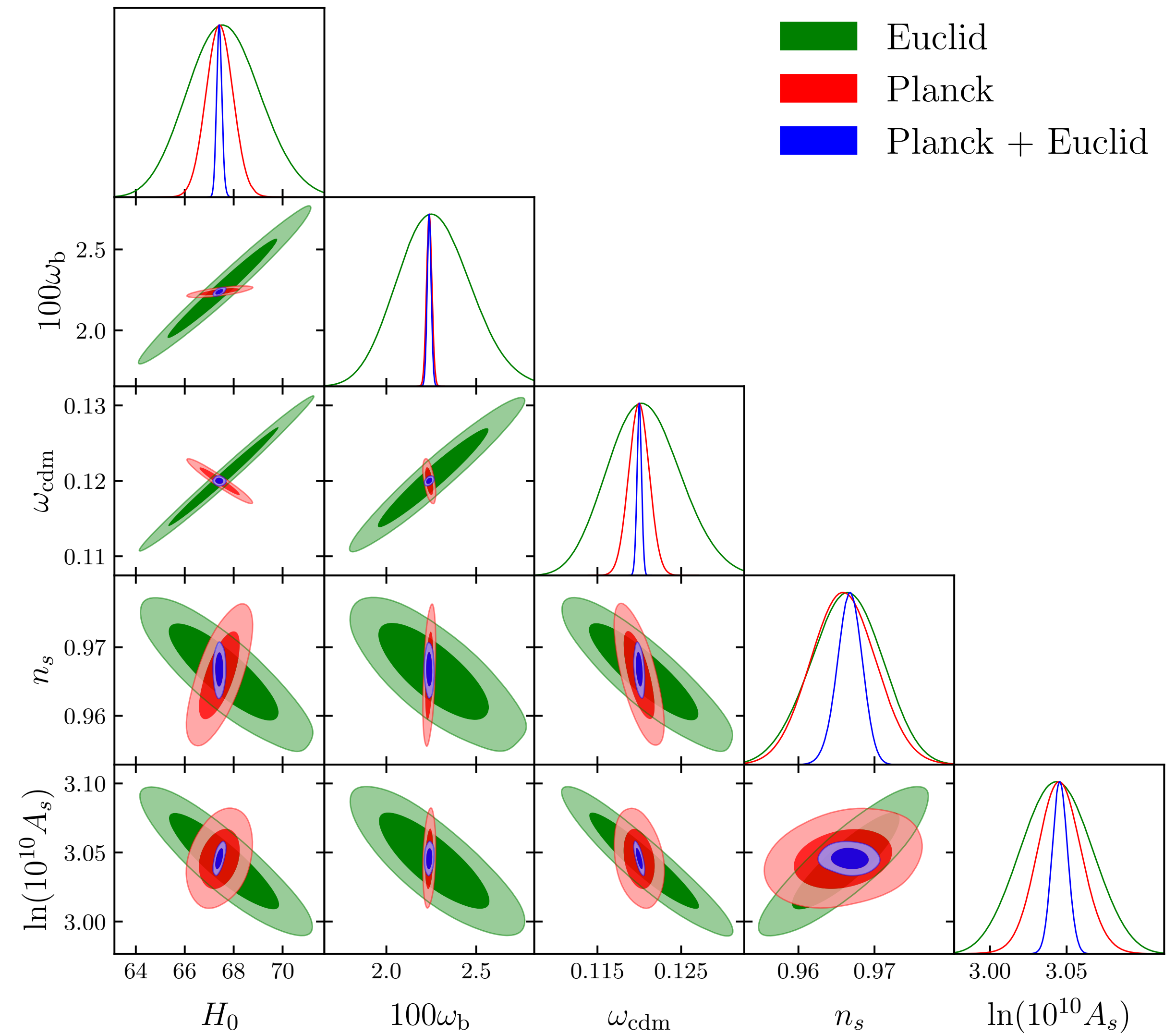
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Break parameter degeneracies



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## Can we do CMB+LSS analyses in SBI?

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**BUT** we can easily build an “effective” simulator using posterior samples from a previous MCMC run

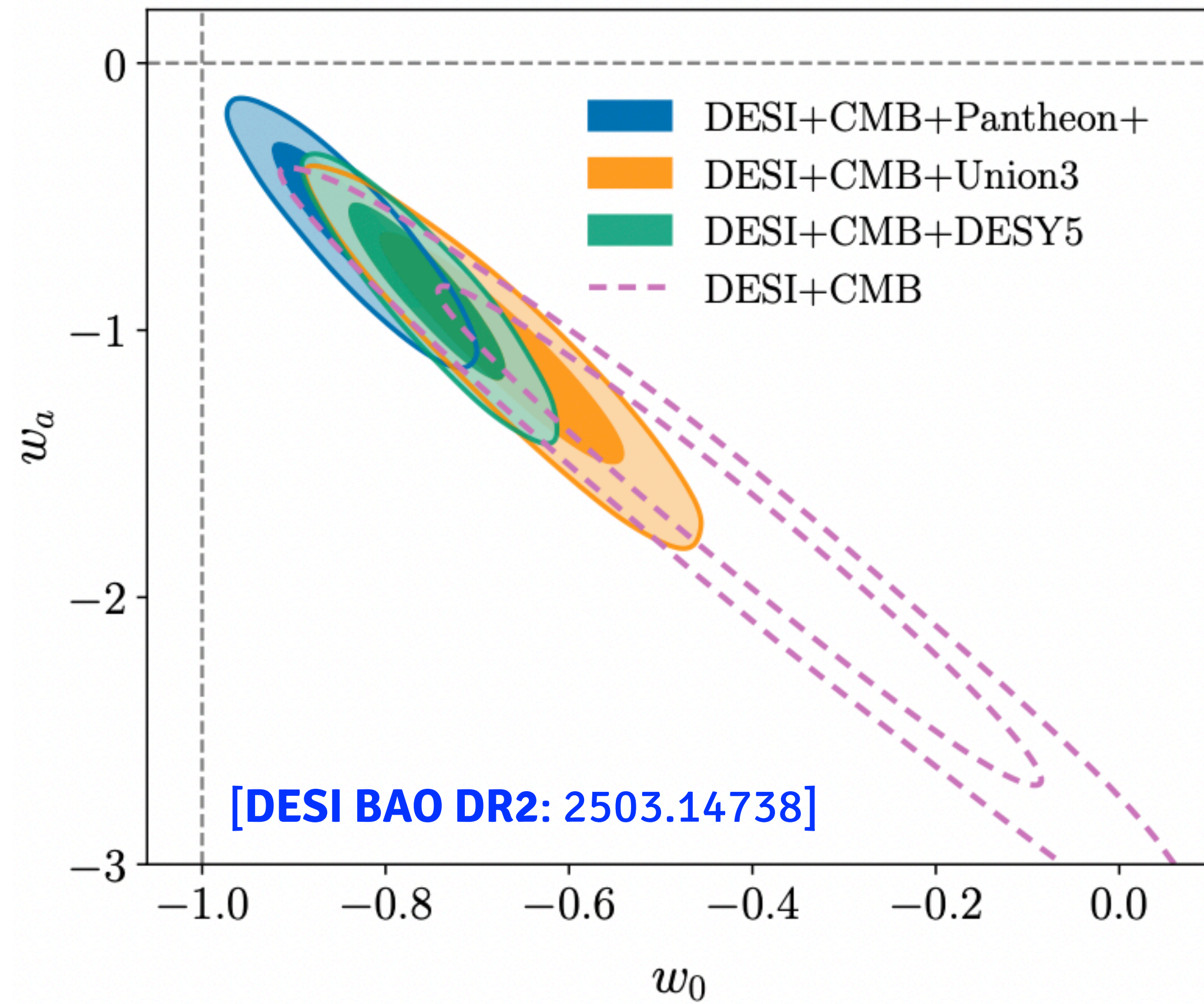
$$a = \theta - \theta'$$

prior samples  $\nearrow$   $\nwarrow$  posterior samples

$$f_{\phi}(\theta | a = 0) \simeq p(\theta | \mathbf{x}_0)$$

# Application to evolving dark energy

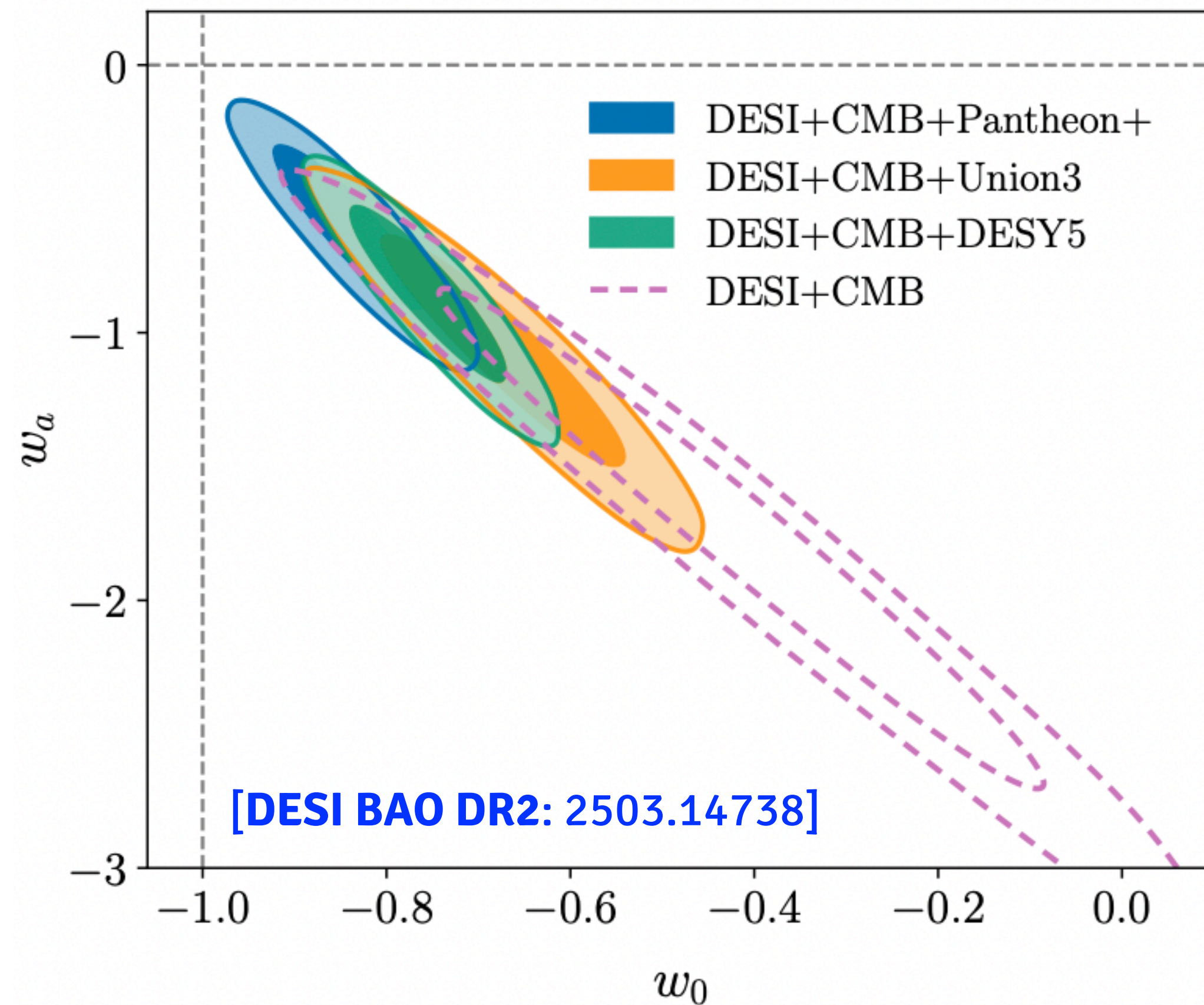
$$w_{\text{CPL}}(a) = w_0 + w_a(1 - a)$$





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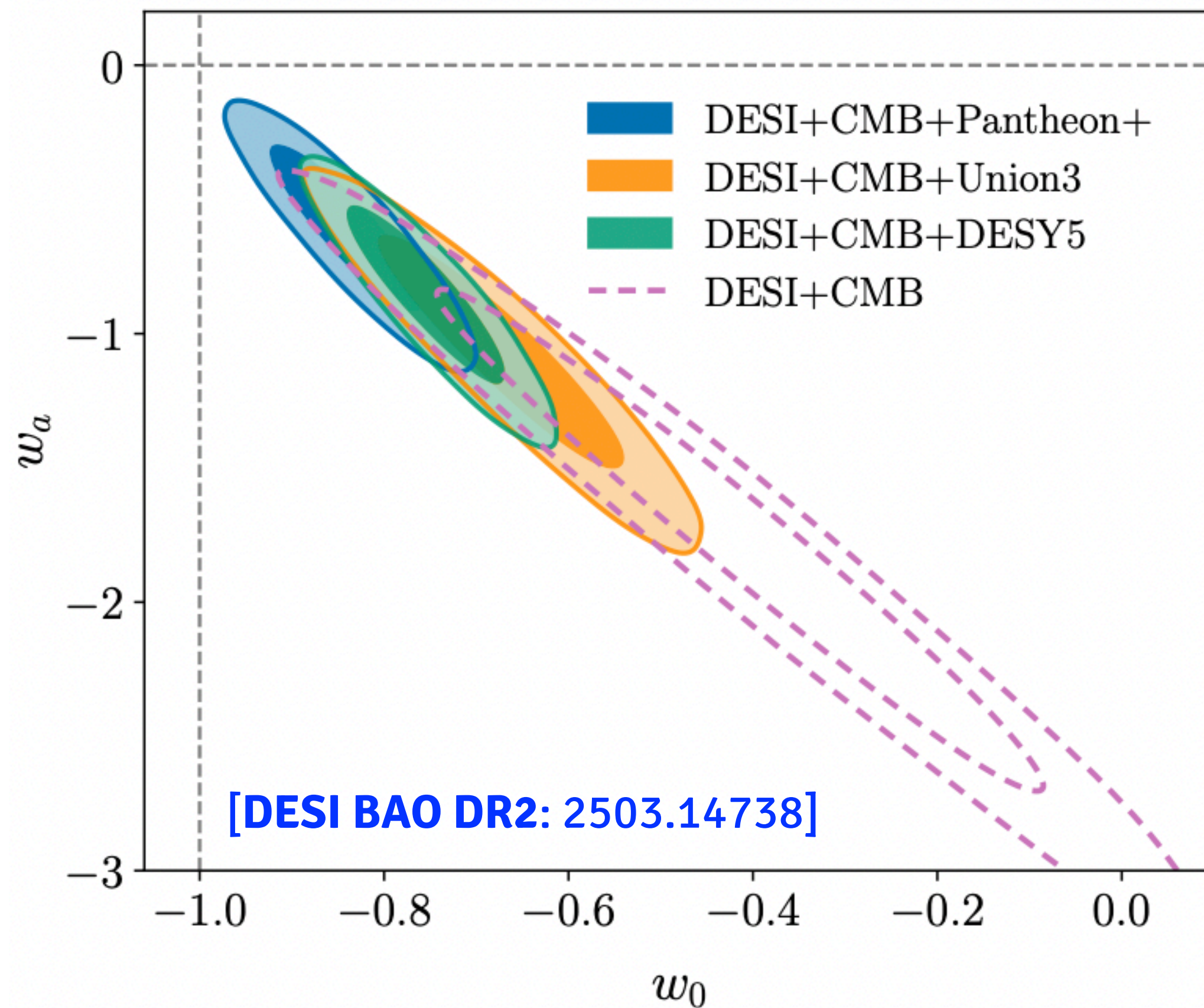


What can Euclid data (and its combination with current probes) tell us about this?



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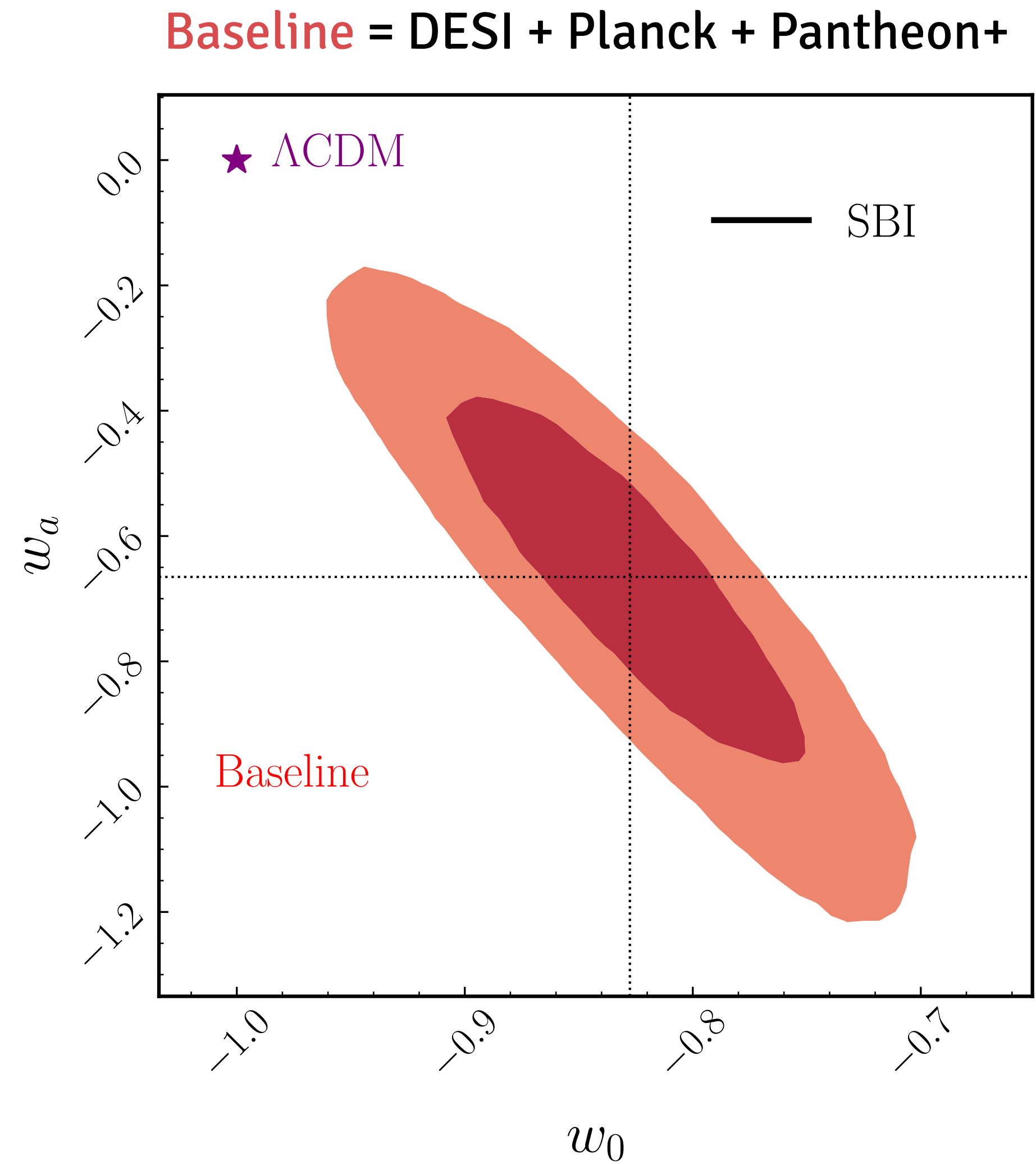


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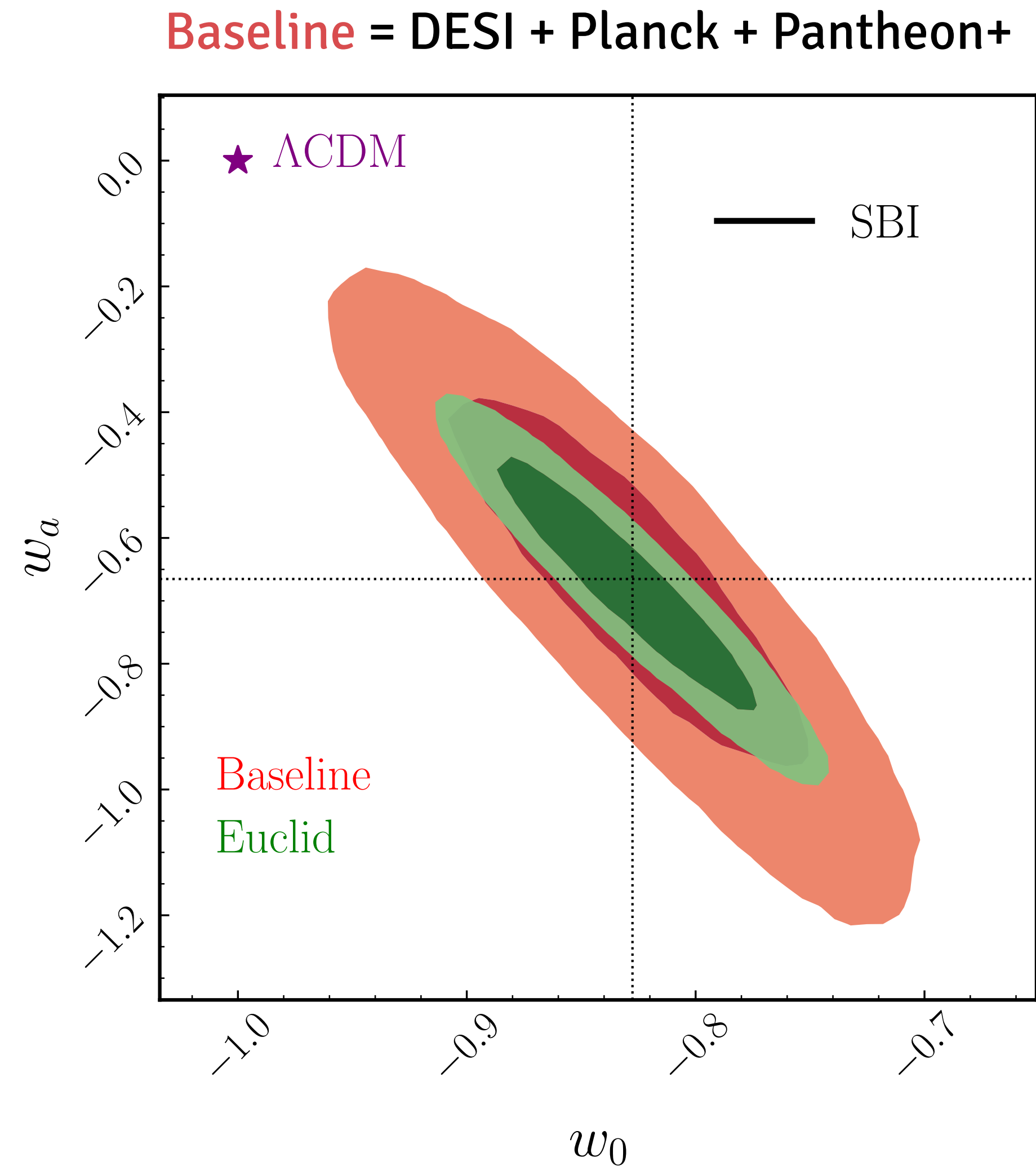


Perform forecast assuming the bestfit  $w_0 w_a$  CDM model hinted by DESI + CMB + Pantheon+

# Forecast $w_0w_a$ CDM posteriors

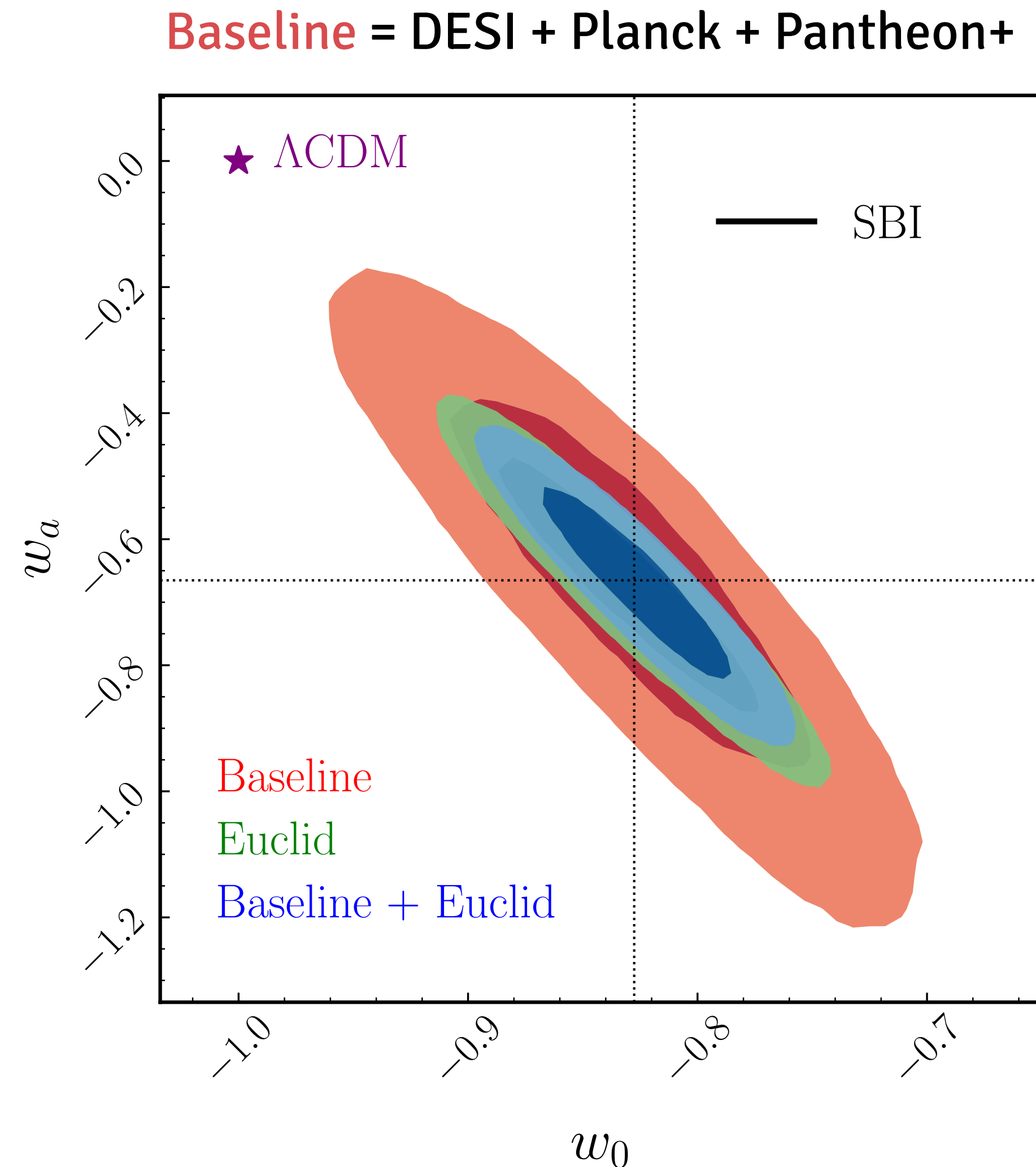


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Euclid alone could detect the fiducial  $w_0w_a$ CDM model at the  $\sim 5\sigma$  level

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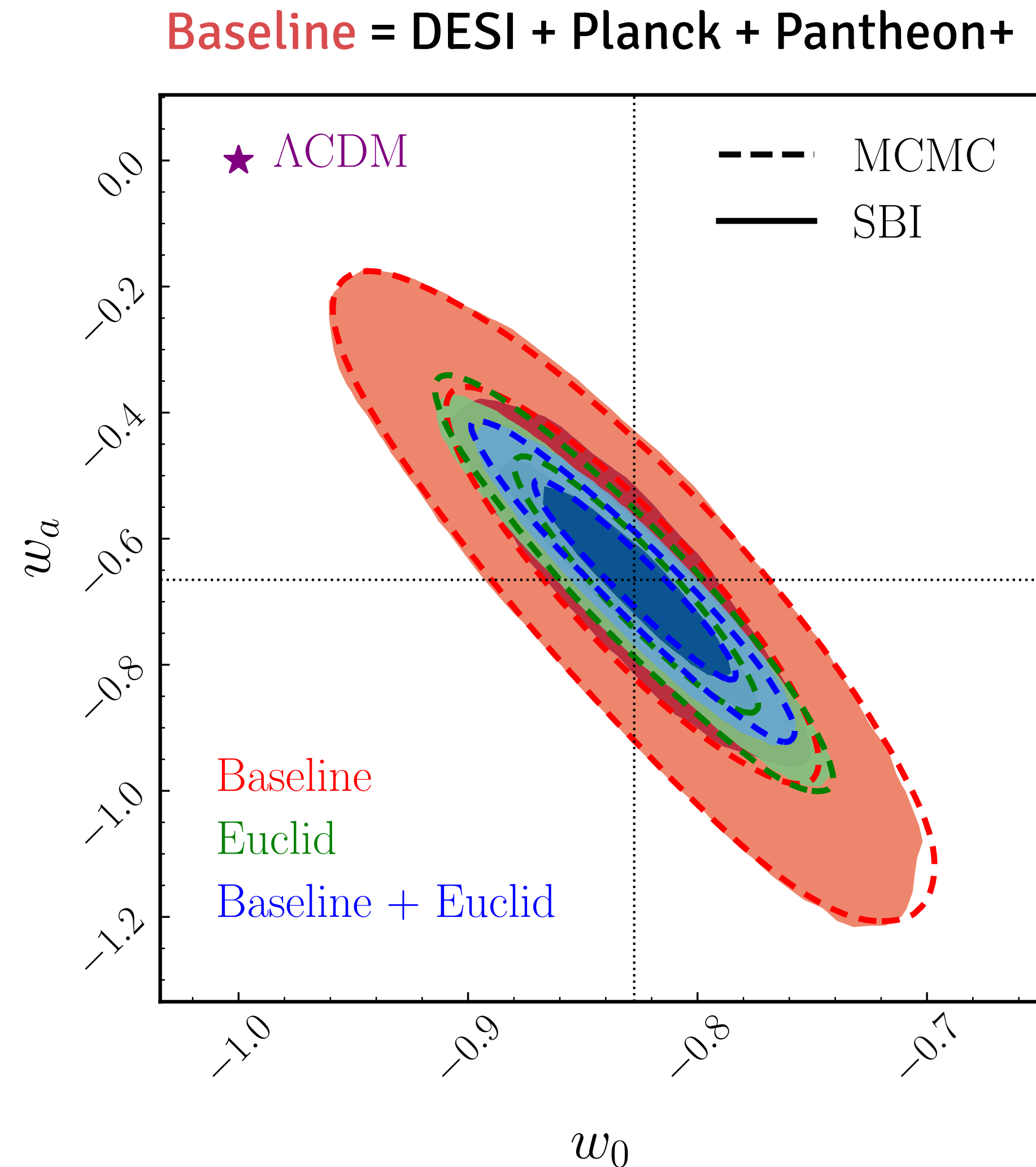


Euclid alone could detect the fiducial  $w_0w_a$ CDM model at the  $\sim 5\sigma$  level

The combination with Planck+DESI data would rise the detection to  $\sim 7\sigma$



# Forecast $w_0w_a$ CDM posteriors



SBI is in good agreement with MCMC, while requiring only **~3% of the number of model evaluations** used by MCMC



# Conclusions

- Modern **deep learning** techniques will be key to learn as much as we can about the dark sector and neutrinos from **future data**
- Emulators** achieve **ultra-fast** model evaluations  
→ applied to **decaying neutrino** models, these can relax current mass bounds up to  $\sum m_\nu < 0.24 \text{ eV}$
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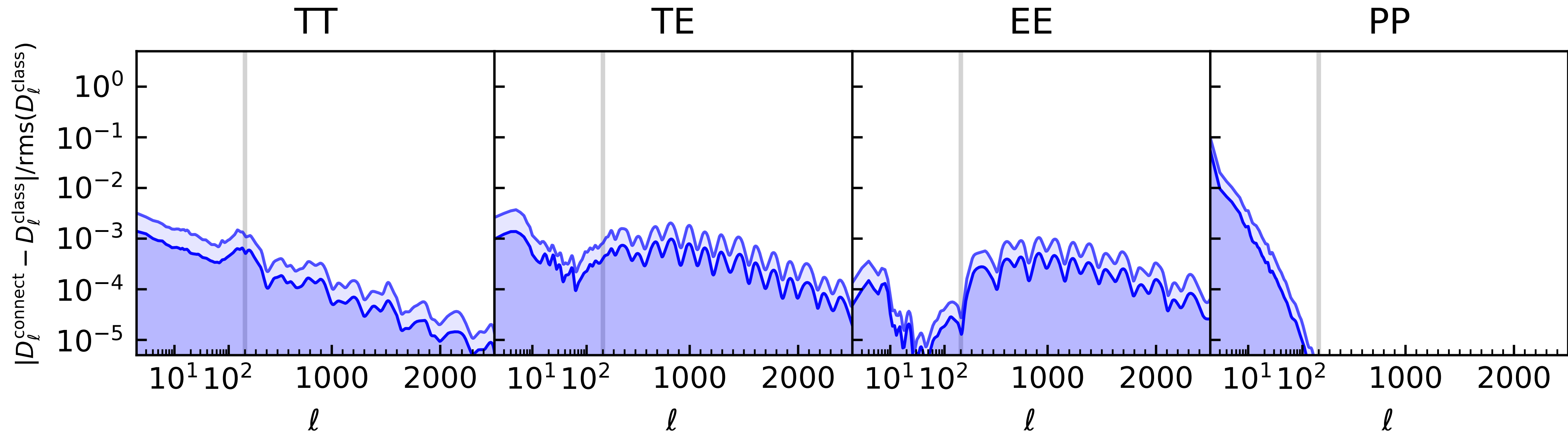
**THANK YOU!**  
[g.francoabellan@uva.nl](mailto:g.francoabellan@uva.nl)



**BACK-UP**



# Errors in emulated CMB spectra for neutrino decays



The  $1\sigma$  and  $2\sigma$  percentile **errors** in the CMB spectra (from the test set) are almost always **below 1%**

**Strategy:** train a neural network  $d_\phi(\mathbf{x}, \boldsymbol{\theta}) \in [0,1]$  as a binary classifier, so that

■  $d_\phi(\mathbf{x}, \boldsymbol{\theta}) \simeq 1$  if  $(\mathbf{x}, \boldsymbol{\theta}) \sim p(\mathbf{x}, \boldsymbol{\theta}) = p(\mathbf{x} | \boldsymbol{\theta})p(\boldsymbol{\theta})$

■  $d_\phi(\mathbf{x}, \boldsymbol{\theta}) \simeq 0$  if  $(\mathbf{x}, \boldsymbol{\theta}) \sim p(\mathbf{x})p(\boldsymbol{\theta})$

**Note:**  $\Phi$  denotes all the network parameters

We have to **minimise a loss function** w.r.t. the network params.  $\Phi$

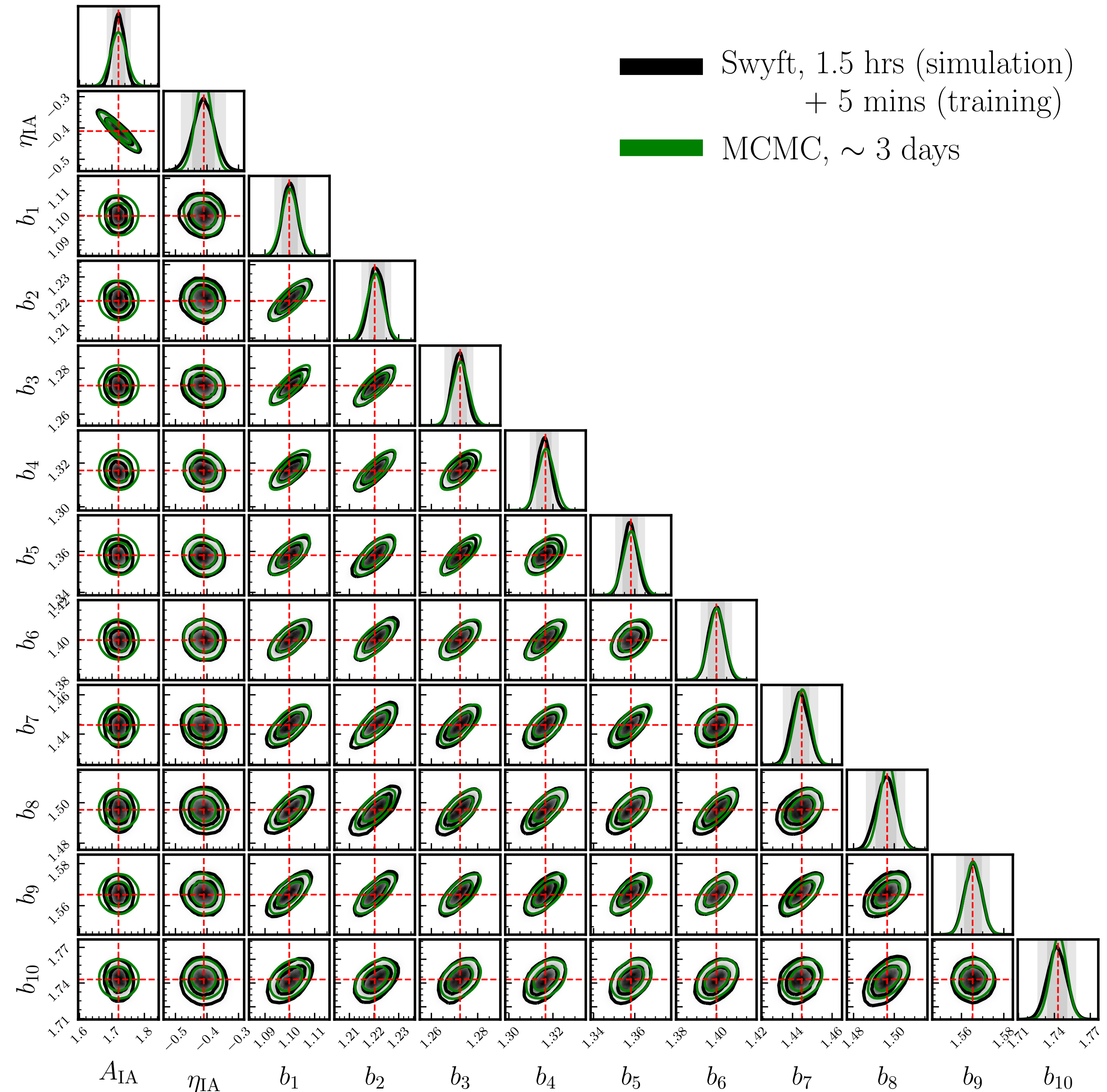
$$L[d_\phi(\mathbf{x}, \boldsymbol{\theta})] = - \int d\mathbf{x} d\boldsymbol{\theta} \left[ p(\mathbf{x}, \boldsymbol{\theta}) \ln(d_\phi(\mathbf{x}, \boldsymbol{\theta})) + p(\mathbf{x})p(\boldsymbol{\theta}) \ln(1 - d_\phi(\mathbf{x}, \boldsymbol{\theta})) \right]$$

which yields

$$d_\phi(\mathbf{x}, \boldsymbol{\theta}) \simeq \frac{p(\mathbf{x}, \boldsymbol{\theta})}{p(\mathbf{x}, \boldsymbol{\theta}) + p(\mathbf{x})p(\boldsymbol{\theta})} = \frac{r(\mathbf{x}; \boldsymbol{\theta})}{r(\mathbf{x}; \boldsymbol{\theta}) + 1}$$

# Posteriors for 3x2pt nuisance parameters

MNRE & MCMC are again  
in good agreement



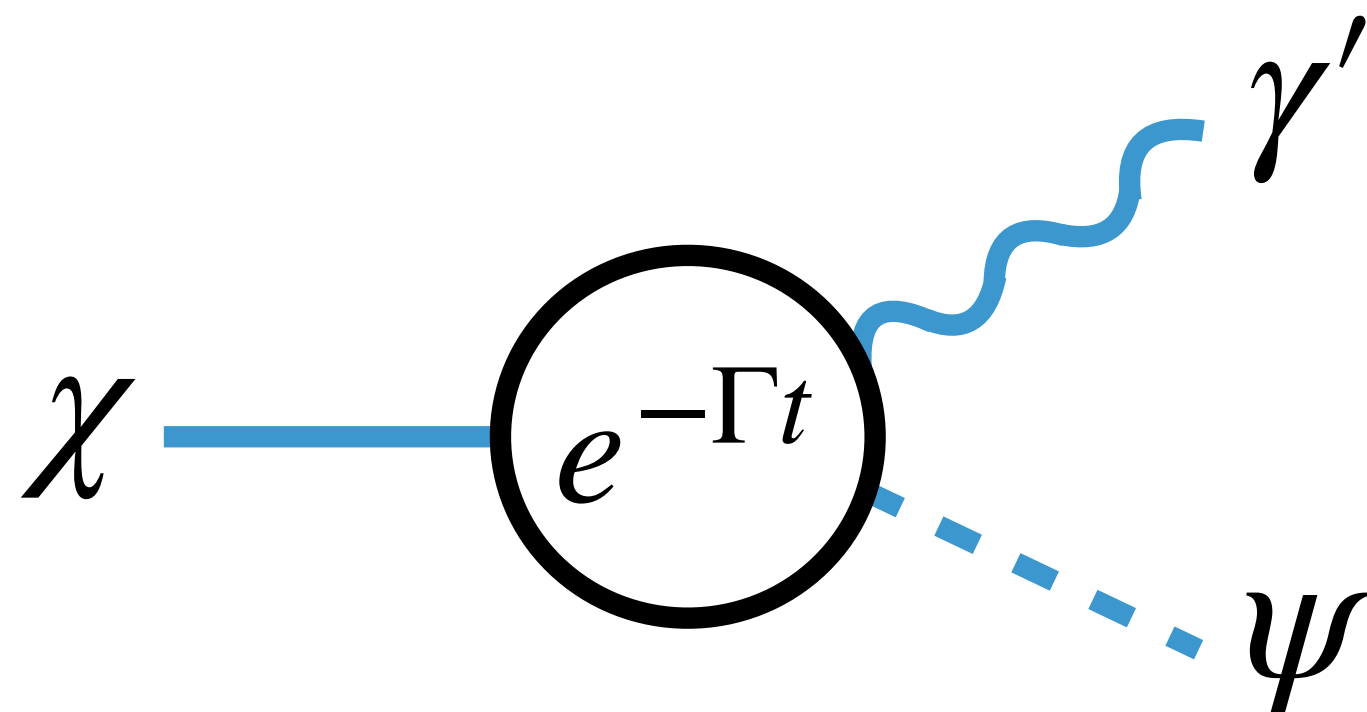


Does MNRE perform well with **highly non-Gaussian** posteriors?

As an example, we test a model of **CDM decaying to DR + WDM**  
(proposed to explain the  $S_8$  tension)

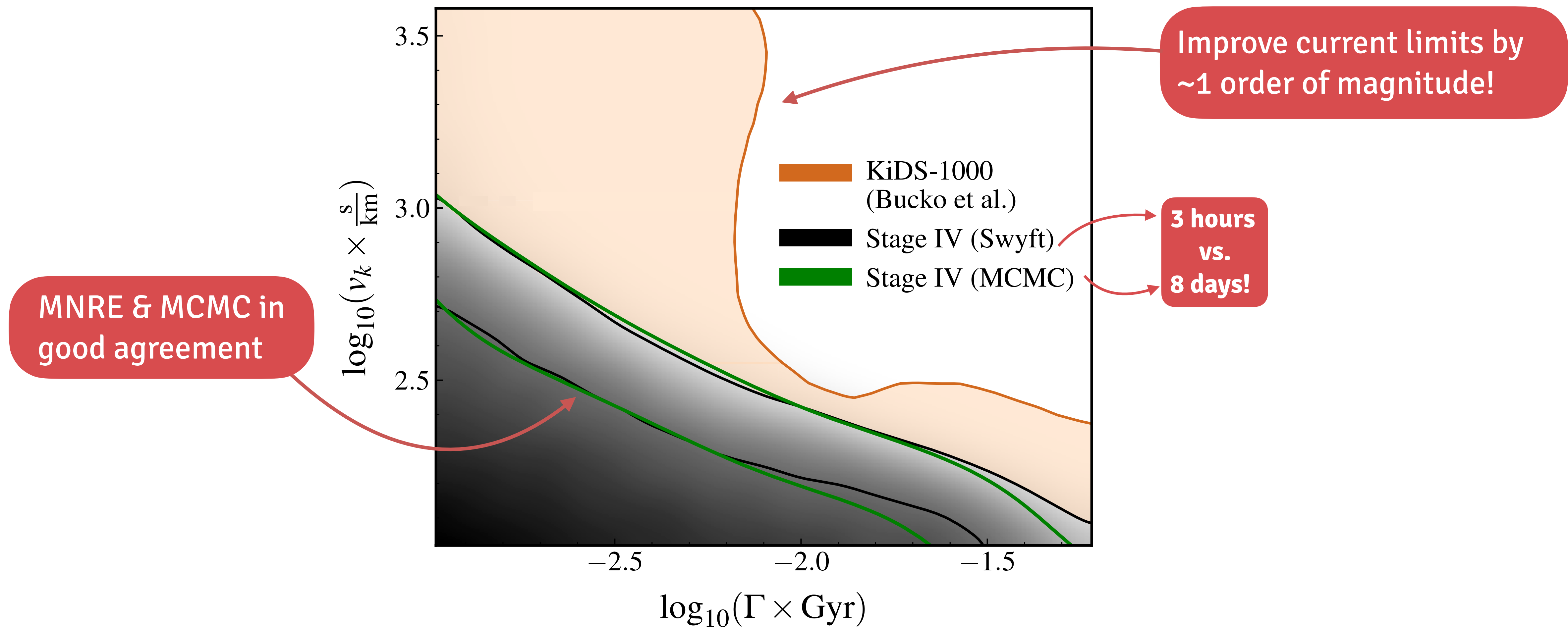
[Abellán et al. 2102.12498]

[Bucko et al. 2307.03222]



Decay rate  $\Gamma$   
WDM velocity kick  $v_k$

# Forecast constraints on decaying DM



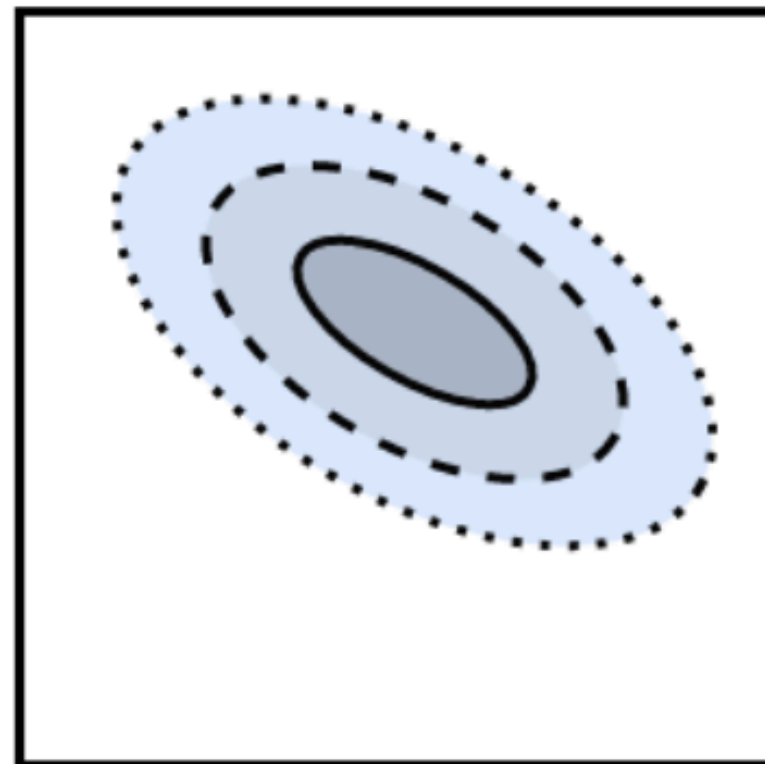
## But can we trust our results?



...even if NNs are often seen as "black boxes", it is possible to perform statistical consistency tests which are impossible with MCMC

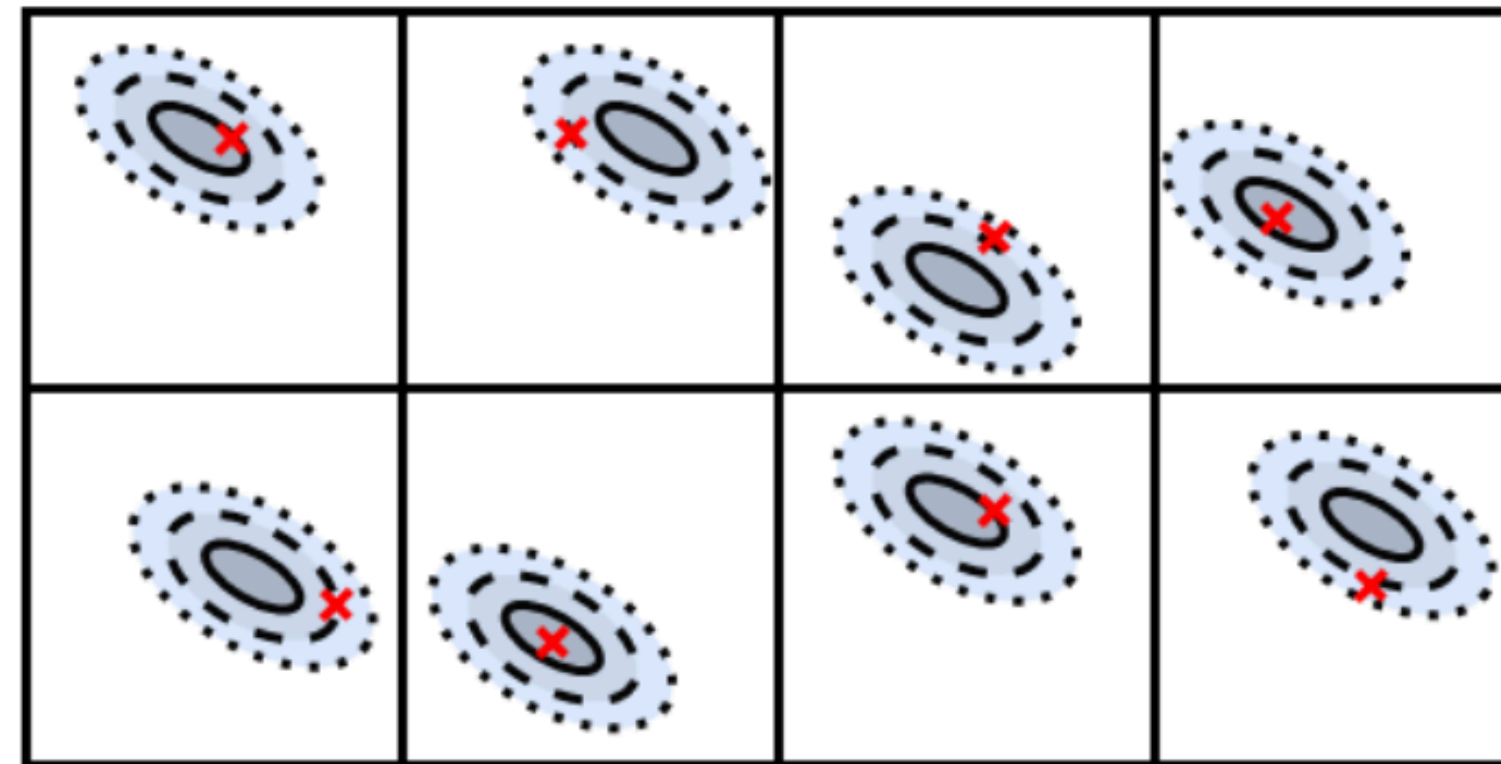
Trained networks can estimate effortlessly  
the posteriors for all simulated observations

MCMC



$$p(\theta|\mathbf{x}_o)$$

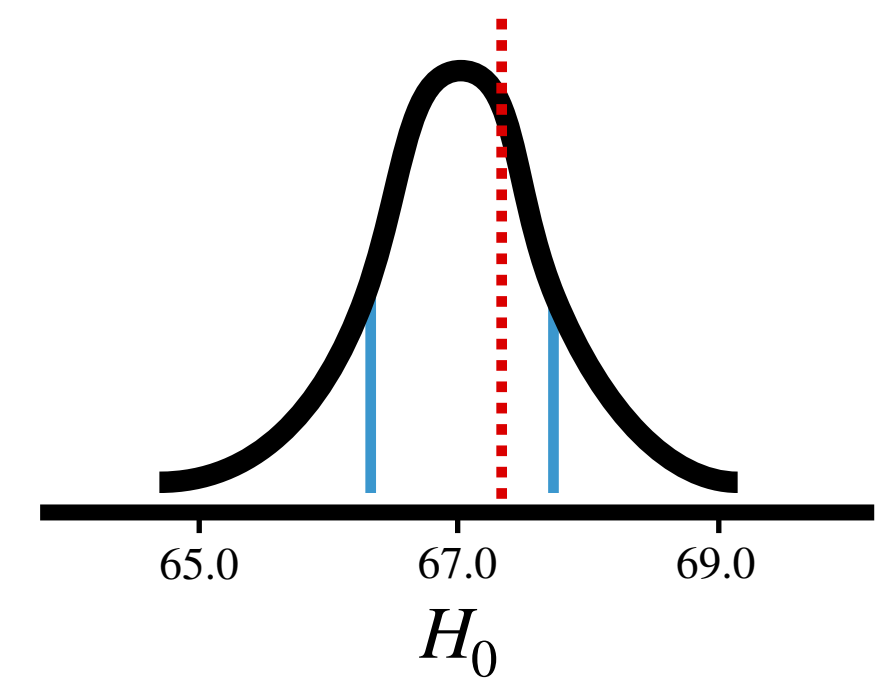
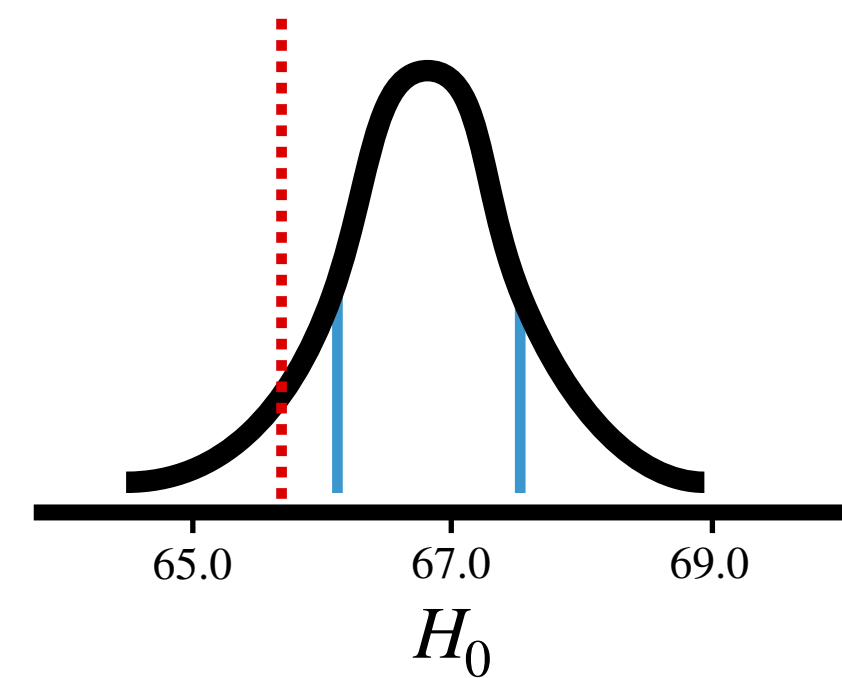
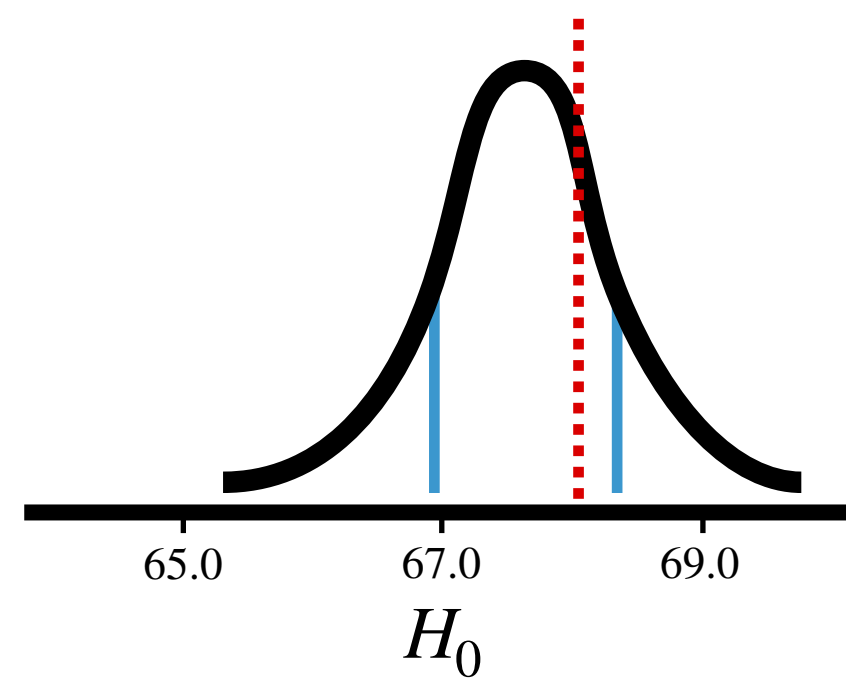
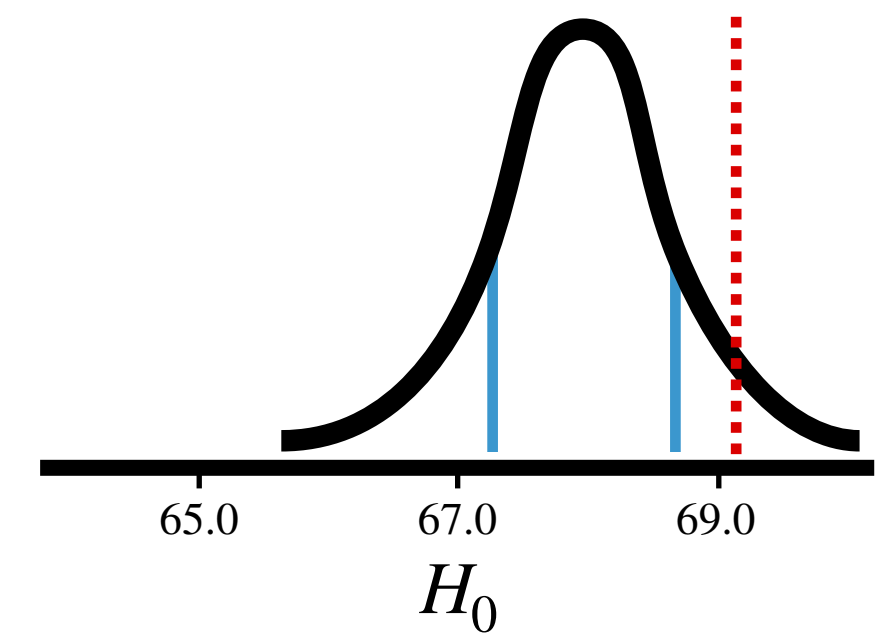
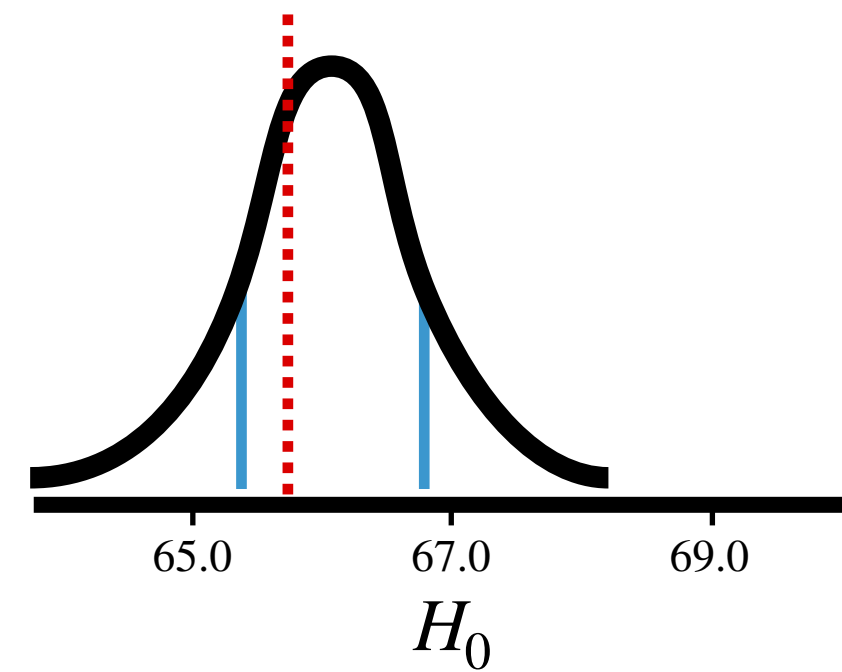
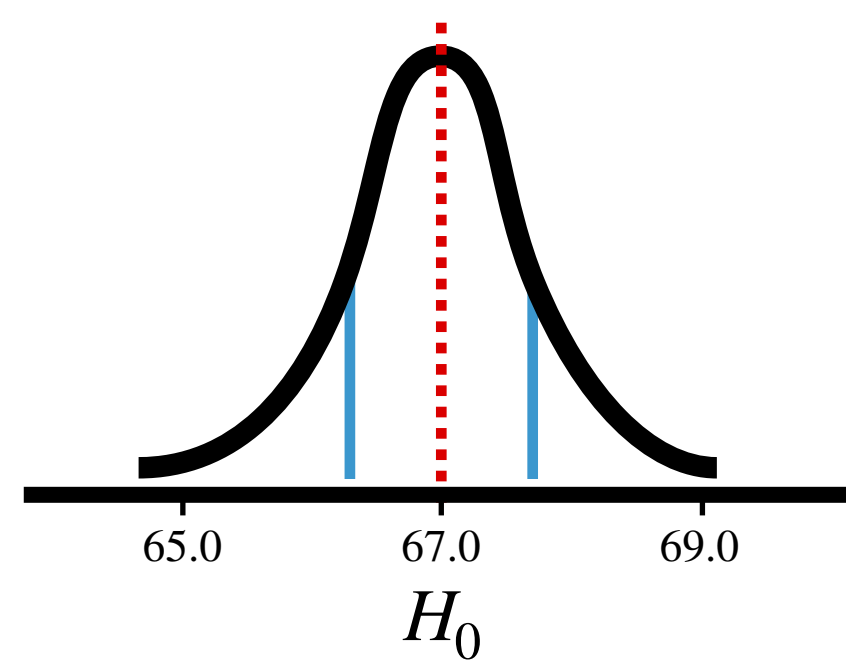
MNRE with swyft



$$p(\theta|\mathbf{x}) \quad \forall \mathbf{x} \sim p(\mathbf{x})$$

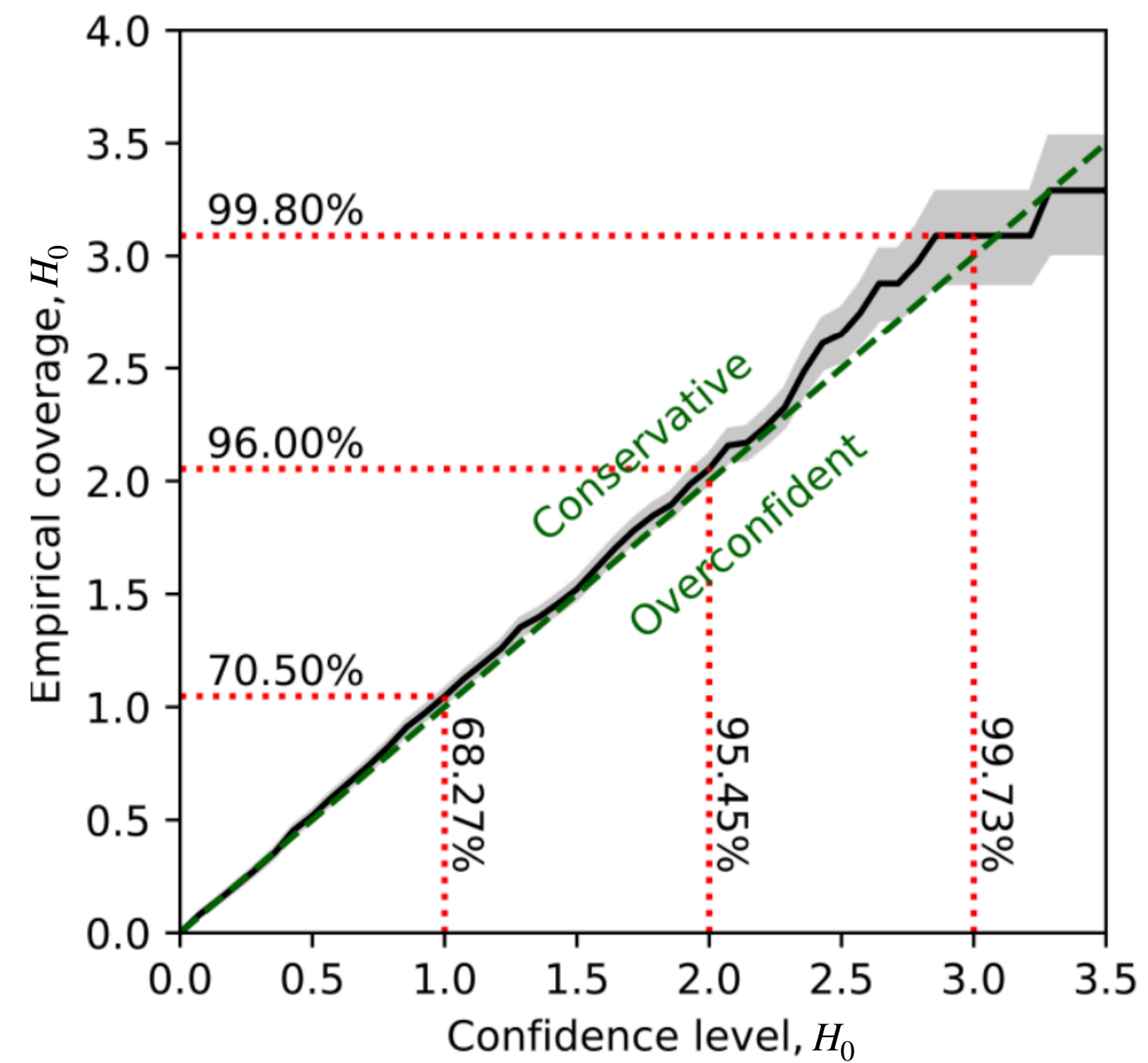


**Ex:** Is the estimated **68.27% interval** covering the **ground truth** in ~68% of the cases?

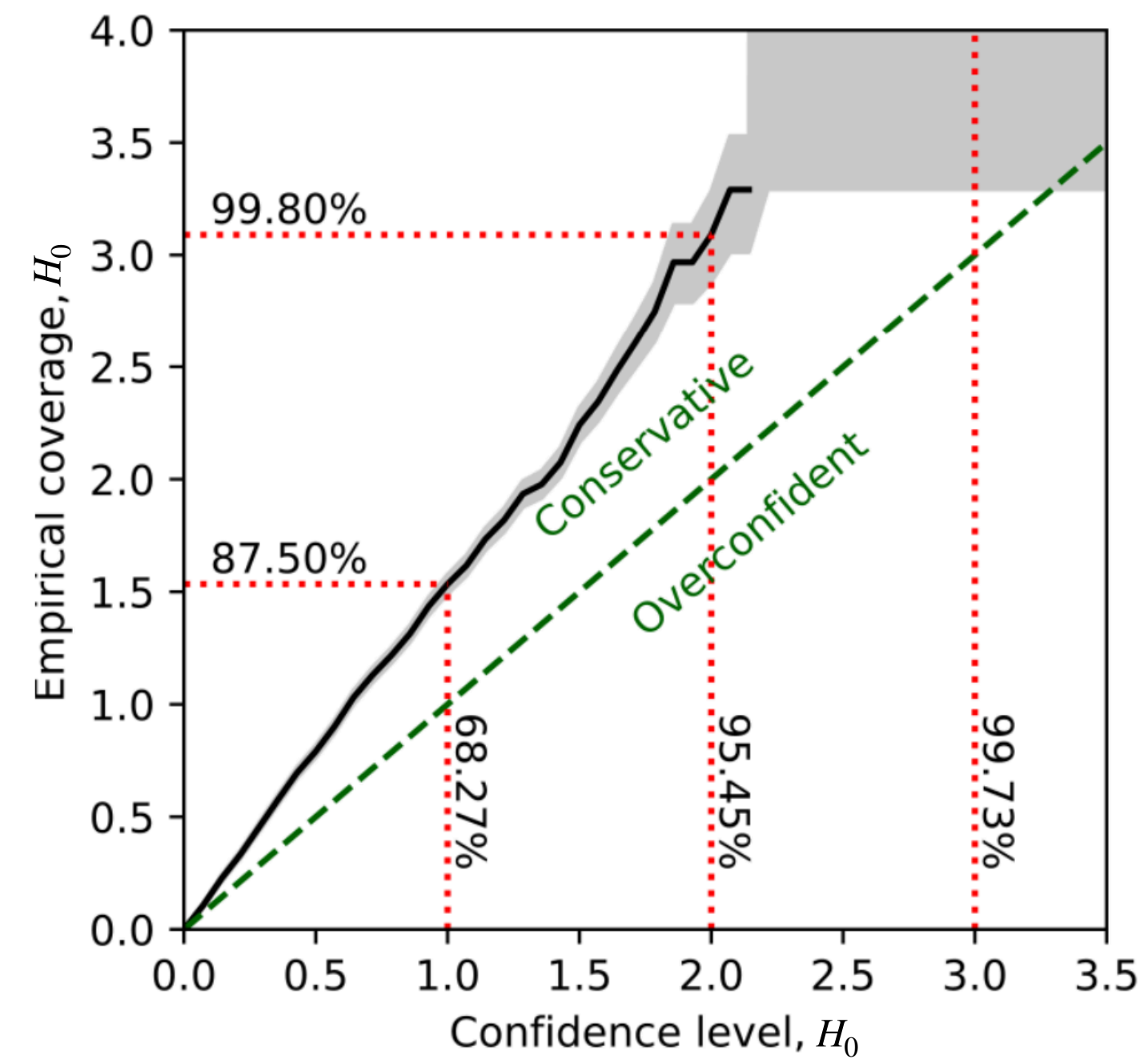


We can empirically estimate the Bayesian coverage

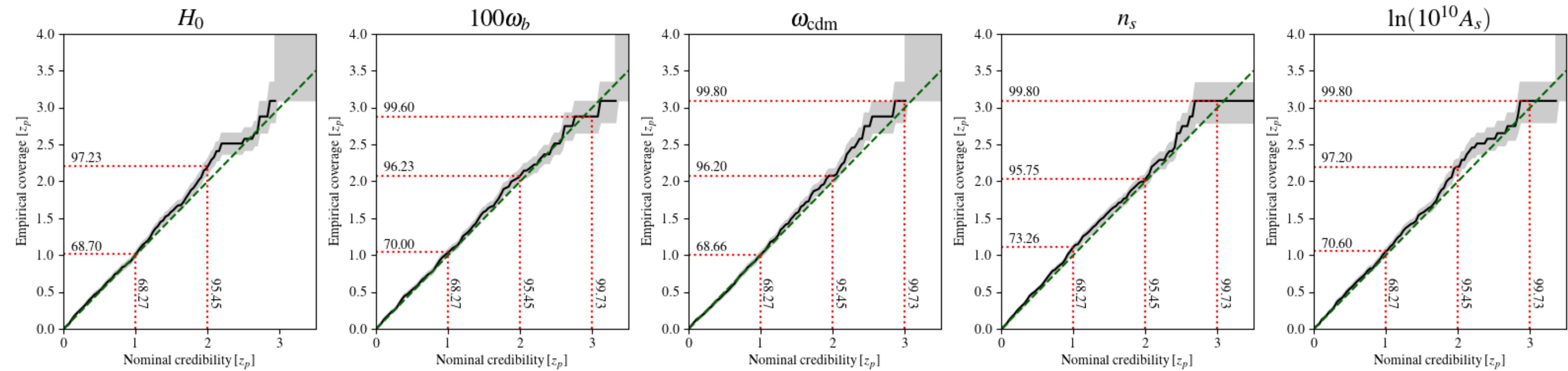
**Converged network**



**Non-converged network**



# Coverage test for Stage-IV 3x2pt



GFA++ 2403.14750

Empirical coverage and confidence level match to excellent precision!